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COUPLED INVERSE MODELING OF A CONTROLLED IRRIGATION EXPERIMENT USING MULTIPLE HYDRO-GEOPHYSICAL DATA

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2	USING MULTIPLE HYDRO-GEOPHYSICAL DATA
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26 ABSTRACT

27 Geophysical surveys can provide useful, albeit indirect, information on vadose 28 zone processes. However, the ability to provide a quantitative description of the 29 subsurface hydrological phenomena requires to fully integrate geophysical data 30 into hydrological modeling. Here, we describe a controlled infiltration experiment 31 that was monitored using both electrical resistivity tomography (ERT) and 32 ground-penetrating radar (GPR). The experimental site has a simple, well-33 characterized subsoil structure: the vadose zone is composed of aeolic sand with 34 largely homogeneous and isotropic properties. In order to estimate the unknown soil hydraulic conductivity, we apply a data assimilation technique based on a 35 36 sequential importance resampling (SIR) approach. The SIR approach allows a simple assimilation of either or both geophysical datasets taking into account the 37 38 associated measurement uncertainties. We demonstrate that, compared to a 39 simpler, uncoupled hydro-geophysical approach, the coupled data assimilation process provides a more reliable parameter estimation and better reproduces the 40 41 evolution of the infiltrating water plume. The coupled procedure is indeed much 42 superior to the uncoupled approach that suffers from the artifacts of the 43 geophysical inversion step and produces severe mass balance errors. The 44 combined assimilation of GPR and ERT data is then investigated, highlighting strengths and weaknesses of the two datasets. In the case at hand GPR energy 45 46 propagates in form of a guided wave that, over time, shows different energy 47 distribution between propagation modes as a consequence of the evolving 48 thickness of the wet layer. We found that the GPR inversion procedure may

49 produce estimates on the depth of the infiltrating front that are not as informative

- 50 as the ERT dataset.
- 51

52 <u>KEYWORDS:</u> hydro-geophysical inversion, electrical resistivity tomography,
53 ground-penetrating radar, infiltration, vadose zone.

54

55 <u>1. INTRODUCTION</u>

56 Hydrological research increasingly requires detailed information to feed data-57 hungry numerical models. For this reason, geophysical data are increasingly called 58 into play to fill the lack of spatial and sometimes temporal resolution of traditional 59 hydrological data. This is particularly true for the vadose zone, where the difficulties for obtaining direct measurements, the general lack of knowledge and 60 61 the uncertainty on the soil parameters and their spatial heterogeneity often lead to 62 develop numerical models that cannot reproduce the behavior of the real systems, unless they are strongly constrained by multiple, extensive and complementary 63 64 data.

65 The vadose/unsaturated zone is home to a number of complex key processes 66 that control the mass and energy exchanges in the subsurface (soil water 67 migration) and between the subsurface and the atmosphere (rain infiltration, soil 68 evaporation and plant transpiration). The understanding of vadose zone fluid-69 dynamics is key to the comprehension of a large number of hydrologically-70 controlled environmental problems, with strong implications in water resources 71 management and subsurface contaminant hydrology. Unsaturated processes are 72 also key factors in a number of important issues, such as the availability of water

for agriculture, slope stability, and floods. The dependence of the hydrogeophysical response on changes in soil moisture content is the key mechanism that allows the monitoring of the vadose zone in time-lapse mode via non-invasive techniques. The use of these techniques can provide high-resolution images of hydro-geological structures in the shallow and deep vadose zones and, in some cases, a detailed assessment of dynamical processes in the subsurface.

The estimation of the time and space variations of water content using non-79 80 invasive methodologies has been the focus of intensive research over the past 81 three decades. Among the numerous techniques developed in literature for such a 82 goal, such as electromagnetic induction, off-ground ground-penetrating radar, surface nuclear magnetic resonance, in this work we consider electrical resistivity 83 tomography (ERT) and ground-penetrating radar (GPR). These techniques 84 measure the electrical resistivity ρ (Ω m) and the relative dielectric permittivity ε_r 85 86 (-) of the porous media, respectively. For both methods the determination of soil water content is based upon existing relationships that link water content to the 87 88 geophysical quantities measured (e.g., Archie, 1942; Topp et al., 1980; Roth et al., 89 1990; Brovelli and Cassiani, 2008, 2011).

When used to study hydrological dynamics, GPR surveys are often performed to detect changes in soil moisture content via the variation of dielectric permittivity, generally measured from GPR travel times in a variety of configurations (e.g., Huisman et al., 2003; Cassiani et al., 2006; Cassiani et al., 2008), such as boreholeto-borehole (e.g., Rucker and Ferré, 2004a, 2004b; Rossi et al., 2012) or boreholeto-surface (e.g., Vignoli et al., 2012). However, the most common setup uses GPR antennas from the the ground surface, even though only few studies with this

97 configuration have been focused on the understanding of the dynamics of the 98 water front during irrigation (e.g., Galagedara et al., 2005; Moysey, 2010; Mangel et 99 al., 2012; Lai et al., 2012) or using natural rainfall (Busch et al., 2014). When working solely from the ground surface, three approaches are possible to 100 101 determine soil moisture content: (a) use the velocity of the direct ground wave, (b) 102 estimating velocity from the reflected events, (c) estimating impedance and thus velocity from the reflected GPR signal. Approaches (a) and (b) share in fact the 103 104 same operational characteristics, needing the two antennas to be separated from 105 each other. Approach (c) does not require antenna separation and exploits the 106 physics of the reflection mechanism, with its own advantages and disadvantages 107 (e.g., Lambot et al., 2004; Schmelzbach et al., 2012), and with more limited applications so far. When the two antennas are separated from each other, the 108 109 survey can be conducted in wide angle reflection and refraction (WARR) mode 110 (e.g., van Overmeeren et al., 1997), where one antenna is kept fixed while the other is moved, or common mid point (CMP) (Fisher et al., 1992; Greaves et al., 1996; 111 112 Steelman et al., 2012), where both antennas are moved simultaneously to keep the 113 same mid-point. Both sounding techniques allow for a good identification of direct 114 waves through the air and the ground. These methods are also employed for the 115 estimation of velocity from the reflected events, even though for this use the 116 normal move-out approach, typical of seismic processing, may not be ideal (see 117 Becht et al., 2006 for a discussion). The estimation of velocity from the direct wave 118 through the ground is the most widely adopted approach for vadose zone 119 applications (e.g. van Overmeeren et al., 1997; Huisman et al., 2001; Hubbard et al., 120 2002). However, in some cases direct arrivals are not so straightforward to

121 identify and can be confused with other events. This can happen in the presence of 122 critically refracted radar waves (Bohidar and Hermance, 2002) or guided waves 123 (Arcone et al., 2003; van der Kruk et al., 2006; Strobbia and Cassiani, 2007). A water front that infiltrates from the surface can give rise to such ambiguous 124 125 situations, as the wet and consequently low velocity layer, lying on top of a faster (drier) media, can give rise to critically refracted waves (Bohidar and Hermance, 126 127 2002) as well as act as a waveguide confined between two faster layers: the air 128 above and the drier media below (Strobbia and Cassiani, 2007), the two situations 129 being defined by the ratio between the wavelength and the layer thickness. 130 Therefore, to study infiltrating fronts, maximum care must be given in 131 understanding the nature of the observed, multi-offset GPR signal, possibly exploiting the entire information content of the data (e.g. Busch et al., 2012). 132

ERT measurements (Binley and Kemna, 2005) have been widely employed to 133 monitor water dynamics, as variations of moisture content (Daily et al., 1992: 134 Binley et al., 1996) and salinity of pore water (Perri et al., 2012) leads to changes in 135 136 the electrical properties of the media (La Brecque et al., 2004; Cassiani et al., 137 2009a). However, it is well known that resolution limitations (Day-Lewis et al., 138 2005) can produce severe mass balance errors (Singha and Gorelick, 2005) even in 139 the most favorable cross-hole configurations. The problem is even more serious 140 when only surface ERT are used to monitor natural or artificial irrigation from the 141 ground surface (Michot et al., 2003; Clément et al., 2009; Caputo et al., 2012; 142 Cassiani et al., 2012; Travelletti et al., 2012) where resolution dramatically drops 143 with depth and a direct conversion of inverted resistivity values into estimates of 144 soil moisture content may prove elusive.

145 Geophysical measurements can be informative of the hydrological response of the 146 soil and subsoil if applied in time-lapse monitoring mode: some geophysical 147 quantities (in this case, ρ and ε_r) are useful indicators of changes in the 148 hydrological state variables, such as moisture content or pore water salinity. 149 However, in order to extract this hydrological information, the assimilation of 150 measurements in a hydrological model is needed. Two different approaches may 151 be applied, named respectively "uncoupled" and "coupled" hydro-geophysical inversions (Ferré et al. 2009; Hinnell et al., 2010). The procedure for an uncoupled 152 153 *inversion* can be summarized by the following steps:

154 1. the spatial distribution of the geophysical quantity of interest (e.g. electrical

resistivity for ERT) is derived from the inversion of geophysical field data;

the application of a petro-physical relationship leads to obtaining, from the
 geophysical quantity, an estimation of moisture content distribution;

the estimated hydrologic state variable, in its spatio-temporal distribution,
 is used to calibrate and constrain a hydrological model, thus identifying the
 corresponding governing parameters.

The inversion of geophysical measurements is usually an ill-posed inversion problem that can be tackled introducing prior information. If no solid independent information is available, the most common approach is the introduction of a regularizing functional, commonly a smoothness constraint (Menke, 1984). As a consequence of ill-posedness and regularization, the inversion procedure can lead to artifacts, misinterpretations and unphysical results, especially in the subsurface regions where the sensitivity of the measurements is low (consider e.g. Day Lewis

- 168 et al., 2005). To overcome these problems, a coupled hydro-geophysical modeling169 can be applied:
- a hydrological model is used to predict the evolution of hydrological state
 variables e.g. moisture content on the basis of a set of hydrological
 governing parameters, the identification of which is the final aim of the
 inversion;
- a suitable petrophysical relationship (same as for point (2) above)
 translates hydrological state variables into geophysical quantities, such as
 resistivity or dielectric permittivity;
- 177 3. the simulated geophysical quantities are used to predict the geophysical178 field measurements;
- 4. a comparison between predicted and measured geophysical field
 measurements allows a calibration of the complex of hydrological and
 geophysical models (thus the name "coupled inversion"), leading to the
 identification of the hydrological parameters, that is the key objective of the
 study.

184 In this work we follow a coupled approach within the framework of data 185 assimilation (DA). DA schemes are mathematical tools of common use in 186 hydrological applications. The main idea behind DA is using the field 187 measurements to correct numerical simulations obtained with a hydrological 188 model, thus modifying their governing parameters. This is possible by the 189 recursion of forecast steps, which simulate the time-evolution of the probability 190 density function (pdf) of the hydrological process, and analysis (or update) steps, 191 which compute a posterior pdfs of the model parameters and state variables by

assimilating the measurements (e.g., McLaughlin, 2002; Moradkhani et al., 2005). A
few examples of coupled hydro-geophysical inversion exist in the literature (e.g.,
Busch et al., 2014) but the use of DA techniques is less widespread (Rings et al.,
2010; Tran et al., 2014).

196 The present work focuses on a field experiment where artificial irrigation is 197 monitored in time-lapse mode from the surface via both ERT and GPR. The 198 homogeneous nature of the site, made of aeolic sand deposits, provides a 199 simplified case study suitable to evaluate the performance of coupled hydro-200 geophysical inversion and test the information content of different geophysical 201 data. Both GPR and ERT geophysical measurements are assimilated into the 202 hydrological model CATHY (Camporese et al., 2010), that is employed for the numerical simulation of the experiment. We elected to use the iterative sequential 203 204 importance resampling (SIR) proposed by Manoli et al. (2015) as a DA technique to 205 estimate the model saturated hydraulic conductivity. This technique is particularly 206 designed to assimilate geophysical measurements in a coupled hydro-geophysical 207 model: the geophysical measurements are blended in the simulation to update the 208 state of the system, estimate the model parameters and quantify the model 209 uncertainties.

210

The specific goals of this work are:

to analyze in detail the nature of the WARR GPR data collected during the
 irrigation experiment, verifying whether or not complex refraction and
 waveguide phenomena occur during the progression of the wetting front,
 and how and to what extent this type of data can be processed and inverted;

215 2. to assess the effectiveness of incorporating ERT and GPR data in a coupled
hydro-geophysical inversion procedure that, using the unsaturated flow
equations, point directly at the estimation of the saturated hydraulic
conductivity, and to compare this approach with the results of a classical
uncoupled inversion approach;

3. to evaluate to what extent the information that can be obtained from GPR
and ERT data corroborate each other, how the independent assimilation of
each data type performs, if the assimilation of both geophysical techniques
adds information with respect to separate procedures, and finally what is
the value of using both techniques to monitor the infiltration process.

The paper is organized as follows: Section 2 is dedicated to the description of the hydrological model and the DA procedure used for the coupled inversion of the geophysical data. After presenting the hydrological experiment taken into consideration (Section 3), in Sections 4 and 5 we analyze the GPR and ERT data, respectively. In Section 6 we describe the setup for the DA procedure in this experiment. The benefits of the coupled inversion are presented in Section 7. The major conclusions of this work are summarized in Section 8.

232

233 2. DATA ASSIMILATION

Data Assimilation methods are typically made of three components: 1) a forward model describing the dynamics of the physical process under study, 2) an observation model that links the simulated system variables to the observed data, and 3) the update procedure, that changes the simulated variables on the basis of the observations. This section describes these three components for our particular

- application, i.e., the assimilation of ERT and GPR data to calibrate an unsaturated
- 240 hydrological model with the iterative SIR method.
- 241

242 **2.1 Hydrological model**

243 The infiltration process in a variably-saturated isotropic porous medium is

244 described by the Richards' equation:

$$S_s S_w(\psi) \frac{\partial \psi}{\partial t} + \phi \frac{\partial S_w(\psi)}{\partial t} = \vec{\nabla} \cdot \left[\mathbf{K}_s K_r(\psi) (\vec{\nabla} \psi + \eta_z) \right] + q \tag{1}$$

where S_s is the elastic storage term [m⁻¹], S_w is water saturation [-], ψ is water 245 pressure head/suction [m], t is time [s], ϕ is porosity [-], K_s is the saturated 246 247 hydraulic conductivity [m s⁻¹] tensor, K_r is the relative hydraulic conductivity [-], $\eta_z = (0, 0, 1)^T$ with z the vertical coordinate directed upward, and q is a 248 249 source/sink term [s⁻¹]. Eq. (1) is highly nonlinear due to the dependencies of soil 250 saturation and relative hydraulic conductivity on pressure head. These terms are modeled using the water retention curves proposed by van Genuchten and Nielsen 251 252 (1985).

253

254 **2.2 Geoelectrical and GPR models for data assimilation**

255 The electrical potential field induced in the soil by current injection during the 256 ERT survey, Φ [V], can be modeled as:

$$-\vec{\nabla} \cdot \left[\rho^{-1}\vec{\nabla}\Phi\right] = I[\delta(\vec{r} - \vec{r}_{S^+}) - \delta(\vec{r} - \vec{r}_{S^-})] \tag{2}$$

where ρ is the electrical resistivity of the soil [Ω m], *I* is the applied current [A], δ is the Dirac function, $\vec{r} = (x, y, z)$, and \vec{r}_{S+} and \vec{r}_{S-} are the source and sink electrode

positions, respectively. Here, the geophysical model is linked to the hydrologic
model by the petrophysical relationship proposed by Archie (1942):

$$\rho(t_i) = \rho(t_0) \left(\frac{S_w(t_0)}{S_w(t_i)}\right)^n \tag{3}$$

where $S_w(t_0)$ is the background water saturation degree and $\rho(t_0)$ is the corresponding bulk electrical resistivity of the soil. In Eq. (2) the bulk electrical resistivity at *i*-th measurement time, $\rho(t_i)$, can be predicted by the knowledge of the saturation degree at the same time step, $S_w(t_i)$, and vice-versa. Thanks to Eqs. (2) and (3), we can write the ERT measurements, here indicated with $y_{\text{ERT}}(t_i)$, as a nonlinear function H_{ERT} of the water saturation:

$$y_{\text{ERT}}(t_i) = H_{\text{ERT}}(S_w(t_i)) + v_{\text{ERT}}(t_i)$$
(4)

267 where $v_{ERT}(t_i)$ represents a Gaussian measurement error with variance $R_{ERT}(t_i)$, 268 $v_{ERT}(t_i) \sim N(0, R_{ERT}(t_i))$.

269 For linking the GPR data to the hydrological model we adopt a simplified 270 approach. The observation model that links the numerical simulations to the GPR 271 measurements consists in the estimation of the infiltration front depth from the 272 simulated vertical profiles of water saturation. When the considered porous media 273 can be considered spatially uniform and the irrigation rate is nearly constant in 274 time, at any assimilation time $(t_1, t_2 \text{ or } t_3)$ the water saturation can be considered 275 uniform from the surface down to a certain depth d_1 , while from d_1 to a depth d_2 it 276 decreases to the initial saturation value according to the soil water retention curve, 277 and finally the water content remains practically constant from d_2 to the bottom of 278 the domain (considering that the water table is much deeper than the vertical 279 extent of the infiltration domain). The average value of the two depths d_1 and d_2 is

an approximation of the depth of the simulated infiltration front. Indicating the estimated infiltration front with $y_{\text{GPR}}(t_i)$, from the described procedure we have that:

$$y_{\text{GPR}}(t_i) = H_{GPR}(S_w(t_i)) + v_{GPR}(t_i)$$

(5)

where H_{GPR} is nonlinear operator and $v_{GPR}(t_i)$ is a Gaussian measurement error 283 with with variance $R_{GPR}(t_i)$, $v_{GPR}(t_i) \sim N(0, R_{GPR}(t_i))$. In the DA process $y_{GPR}(t_i)$ is 284 285 compared with the average thickness estimated from GPR measurements. More accurate (and more complex) GPR modeling could be conducted to 286 construct a forward model e.g. based upon a full-waveform approach (see e.g. 287 288 Klotzsche et al., 2012, 2013). However we do not deem this is necessary for this 289 case study, where the key information that is derived from GPR resides in the 290 depth of the infiltration front and the electromagnetic (EM) wave propagation is

dominated by guided waves (see Section 4).

292

293 2.3 Iterative SIR algorithm for Data Assimilation

294 In Manoli et al. (2015) the hydrological and geophysical models are coupled in a 295 DA framework to simulate ERT surveys and update the physical state variable (soil 296 saturation) and the model parameters whenever a geophysical measurement is 297 available. DA methods allow the incorporation of real system observations onto 298 the dynamical model to automatically correct the model forecast (i.e., the solution 299 of Eq. 1) and the model parameters (e.g., the saturated hydraulic conductivity K_s) 300 thus reducing the uncertainties related to the model prediction. In the following 301 we indicate with λ the set of time-independent model parameters in Eq. (1) and 302 with $p_0(\lambda)$ its prior pdf.

303 The SIR algorithm uses a weighted Monte Carlo (MC) approach to perform the 304 state and parameter update (e.g., Moradhkani et al., 2005). The MC realizations, 305 which are also called particles, are initialized by sampling the parameter values from the prior distribution, $\{\lambda_0^j\}_{j=1}^N$, where *N* is the total number of MC realizations 306 and j is the realization index. SIR associates a weight to each realization, w_0^j , which 307 308 is initialized to 1/N. The forecast step is given by the numerical solution of 309 Richards's equation (1) for each set of parameters, thus describing the space and time evolution of the infiltration process. Note that weights and parameters are 310 invariant during the forecast step. At a general time t, each realization is described 311 by its particular set of parameters, state variables and weight $\{\lambda_t^j, S_w^j(t), w_t^j\}_{i=1}^N$. 312

In an assimilation step t_i , with the idea that the weight represent the 'closeness' 313 of a realization to the real process, the SIR algorithm changes the weights 314 according to the Bayes' formula: new weights are assigned to each particle on the 315 basis of the likelihood function of the measured data with respect to the simulated 316 data, e.g., $p(y_{ERT}(t_i)|S_w^j(t_i))$ for ERT data. The likelihood functions for the ERT and 317 GPR data can be obtained from the measurement error pdfs described Eqs. 4 and 5. 318 319 respectively. Then, the weights are changed with the following formula (here 320 written for a general observation y):

$$\widetilde{w}_{t_i}^j = w_{t_{i-1}}^j p(y(t_i)|S_w^j(t_i))$$
(6)

$$w_{t_i}^j = \frac{\widetilde{w}_{t_i}^j}{\sum_{j=1}^N \widetilde{w}_{t_i}^j} \tag{7}$$

where (7) is a normalization of the weights. Since some of the updated weightsmay be negligible, meaning that the corresponding particles are not representative

323 of the physical process, the SIR introduces a resampling step after the update. In 324 the resampling step, the particles with negligible weights are discarded, while 325 those with large weights are duplicated, in order to retain only the particles that are more representative of the filtering probability. Manoli et al. (2015), similarly 326 327 to Moradhkani et al. (2005), adapted this step to update also the model 328 parameters: the weighted empirical distribution of the parameters is adopted to 329 sample new parameter values the duplicated particles. The SIR method continues 330 with a repetition of forecast and update steps, and terminates in correspondence 331 of the last geophysical measurement. Since bias may be present in the initial model parameters, and since the hydraulic conductivity distribution may not converge 332 333 during the sequential assimilation, the posterior distribution computed with the SIR method may not be optimal for the whole simulation. For this reason it is 334 fundamental to iterate the described procedure until the parameter distribution is 335 336 unchanged during the simulation. At each iteration the procedure initializes the parameters with an averaged posterior distribution, computed on the ensemble of 337 338 the hydraulic conductivities computed after all the previous updates.

339

340 **<u>3. FIELD SITE AND IRRIGATION EXPERIMENT</u>**

The experimental site is located in the campus of the Agricultural Faculty of the University of Turin, Italy, in Grugliasco (45° 03' 52" N, 7° 35' 34" E, 290 m a.s.l.) (Fig.1). The depth of interest is the top 1 m from the ground surface, where the lithology is homogeneous. The stratigraphy is composed of a regular sequence of sandy soil (mesic Arenic Eutrudepts) and the sediments in this area are largely aeolic sands with extremely low organic content. The aeloic sand grains are

relatively homogeneous in size with a mass median diameter (d_{50}) of about 200 µm and porosity ranging between 0.35 and 0.4 (Cassiani et al., 2009c). According to the Comprehensive Soil Classification System, the horizon down to about 1-1.5 meter depth is an A-horizon made of mineral matter (80% sand, 14% silt and 6% clay).

The water table is located around 20 m below the ground surface and therefore the shallow vadose zone, where our experiment took place, is not practically influenced by the underlying saturated zone. At the moment of the survey the vegetation was composed only of natural grass, no cultivation is present (Fig. 1b).

356 An infiltration experiment was performed at the site on August 28, 2009. The 357 irrigation was provided by a 17 m line of sprayers. The soil surface covered by irrigation was approximately a rectangle of 18 m by 2.6 m (Fig. 1). The irrigation 358 359 lasted for 5 hours and 45 minutes and was performed in 3 steps (Table 1), 360 separated by intervals when a break of the irrigation allowed ERT and GPR acquisitions to be performed (see Fig. 1c for the geometry of the geophysical 361 362 surveys). At the center of the ERT profile, along the sprinkler line, two Time Domain Reflectometry (TDR) probes were vertically placed in the soil with a 363 364 length of 0.15 and 0.30 cm.

The irrigation intensity was always lower than the infiltration capacity of the soil, so no ponding was observed at the soil surface. The ERT and GPR measurements were performed with the schedule summarized in Table 2, where the time is referred to the starting of the irrigation.

369

371 4. GPR DATA ANALYSIS

The infiltration test was monitored by GPR using a PulseEkko Pro radar system (Sensors and Software Inc., Canada) with 100 MHz antennas. The surveys were repeated in time (Table 2) using a WARR scheme. The WARR profiles were acquired along the sprinkler line (Fig. 1c); the time sampling interval was 0.2 ns and the offset increment between transmitting and receiving antennas was equal to 0.1 m over a 10.5 m line, starting from an initial offset (minimal distance between transmitter and receiver) of 1 m.

379 The background WARR radargram before the irrigation is shown in Fig. 2, where we can clearly recognize the direct ground wave with a velocity of about 380 381 0.14 m/ns. The evolution of WARR surveys over time (Fig. 3) shows that the infiltration front modifies substantially the appearance of the GPR signal. The 382 radargrams in Fig. 3 are distinctly different from each other: the direct radar wave 383 in air is obviously unaltered over time, while the signal from the soil is 384 progressively delayed. This phenomenon is due to the presence of a wet low-385 velocity layer, between the surface and the dry sandy soil, which becomes 386 387 increasingly thicker over the irrigation period. At a first glance, the interpretation 388 of the data may be conducted by identifying the first soil arrival as a critically 389 refracted GPR wave that comes from the –wet - dry interface and arrives at larger 390 intercept times as infiltration progresses, consistently with a deeper wetting front. 391 Although, this event must be present in the data, it is likely to be masked by guided 392 modes of GPR wave propagation as described by Strobbia and Cassiani (2007). The 393 establishment of guided EM waves is the consequence of the geometry of the 394 dielectric properties of the materials involved in the wave propagation. The energy

395 radiated from the transmitting antenna is spread out into the low-velocity layer 396 and reaches the underlying faster layer (dry sand) with an angle greater than the 397 corresponding Snell critical angle, in such a way that the energy is totally reflected. 398 The same phenomenon happens when the reflected energy reaches the boundary 399 between the air and the wet sandy media. The total internal reflections guide the 400 GPR waves horizontally inside the low-velocity layer, while outside of the wet layer 401 there are only evanescent waves with no radiation in the dry material and in the 402 air. A simpler interpretation of the radargrams (Fig. 3A) as a simple consequence 403 of refracted events - albeit possible (see Cassiani et al., 2009b) - would lead to 404 unclear event identification.

We analyzed the frequency-wavenumber (f-k) spectra of the radargrams with 405 the aim of recognizing guided modes of wave propagation (Fig. 4A). The *f-k* spectra 406 are obtained by a preprocessing involving several filtering procedures. The first 407 408 preprocessing step consists in the application of a *de-wow* filter, following the procedure of Gerlitz et al. (1993). The *wow* effect is due to the air-ground pulse 409 410 interference. In fact, electrostatic and inductive fields near the transmitter lead to 411 the saturation of the receiver electronics and generate a low frequency 412 contribution that decays with distance. The consequence of the *wow* is to move 413 trace amplitude towards positive (or negative) values, resulting in a non-zero-414 mean trace. Removing the *wow* frequencies should reconstruct a zero-mean trace, 415 where small amplitudes are easier to identify. This filter is based on the 416 subtraction of the median amplitude, calculated inside a mobile window in the 417 time domain. The window size is determined from the maximum *wow* frequency,

418 achieved from the frequency spectra of all unfiltered traces (*f-x* spectra – i.e. one
419 frequency spectrum for each offset x).

420 The second processing step is a *muting* of the portions of the radargram that are 421 not relevant in the guided mode propagation, so as to highlight the signal of the 422 supposed guided waves. The *muting* process has the aim of cleaning those portions of the radargrams that are not useful in the present study: events that may be 423 424 considered as noise in a guided wave analysis. So *muting* is applied to remove the 425 air direct wave as well as the reflected events at later times. We applied a Tukey 426 window in time, to prevent ringing in the *f*-*k* domain that may be due to an abrupt 427 signal step in the time domain. The Tukey window is set to obtain half of the entire window length as a flat plateau, while the two marginal sectors consist of segments 428 of a phase-shifted cosine. 429

The final filtering process is the application of a finite impulse response (FIR) filter to remove signal noise at low and high frequencies. The FIR filter has a structure that can maintain the true intensity of the signal between 20 and 250 MHz. This is a broad window for a signal centered around 100 MHz, since the guided propagation shows apparent frequencies that can be higher than the acquisition capabilities of the receiving antenna. This fact is the consequence of the limitation of our array, that records the GPR echoes only at the ground surface.

The filtered radargrams are shown in Fig. 3B. The corresponding *f*-*k* spectra (Fig. 438 4A) show the signal evolution over time. The color scale of the power spectral 439 density is the same for the different time-steps, in order to show the differences of 440 energy distribution over time. The energy peaks at times t_1 and t_3 have much 441 higher amplitudes than at time t_2 , when energy peaks are relatively weak as energy

442 is spread over several modes of propagation, while at times t_1 and t_3 a dominant 443 mode is clearly recognizable. This may be the consequence of our spatial sampling 444 that is not able to record with enough intensity the prevailing mode of resonance 445 induced by that particular subsoil geometry, but can also be a symptom of the 446 energy shifting between fundamental (at time t_1) and first higher mode (at time t_3). 447 The positions of the absolute maxima, detected for each frequency, are plotted as 448 magenta dots (Fig. 4A), while the white dots represent the local maxima.

449 Maxima picking in spectral amplitudes leads to obtaining the dispersion curves of Fig. 4B, showing the dependence of phase velocity on frequency. Here red dots 450 correspond to the absolute maxima, while blue dots show local maxima. The 451 dispersion curves at times t_1 show a clearly identifiable fundamental mode, while 452 at time t_3 the first higher mode is much more energetic than the fundamental mode. 453 The switch of the highest energy to higher modes of propagation may lead to the 454 455 transient step which involves time t_2 , where the power spectral density is spread upon different modes (Fig. 4A). 456

In order to give a hydrological meaning to these results, we need to translate the 457 458 spectral analysis of guided waves into an estimate of the evolution of the hydraulic 459 process. In particular we are interested in the location of the wetting front at depth, 460 as this information is suitable for the calibration of hydrological models. The depth 461 of this front corresponds to the thickness of the guiding high dielectric permittivity 462 layer. The identification of the layer thickness and dielectric properties requires 463 inversion of the dispersion curves (van der Kruk et al., 2006; Strobbia and Cassiani, 464 2007). We adopted as a forward model the description of the asymmetric slab waveguide given by Strobbia and Cassiani (2007). The approximation of 1-465

466 dimensional waveguide is valid as long as we assume that irrigation is practically uniform along the sprinklers' line, and the soil is largely homogeneous. The 467 468 inversion of dispersion curves was performed using a MC approach. We sampled the controlling parameters, i.e.: velocity of the shallower wet layer, velocity of the 469 470 deeper dry layer and thickness of the wet layer. The velocity of air can be 471 considered a constant equal to 0.3 m/ns. To reduce the number of ensembles of parameters combinations, we fixed the value of the velocity of the deeper and 472 473 faster layer to about 0.14 m/ns, i.e. we set it equal to the velocity of the soil before 474 irrigation (Fig. 2). This choice is also in accordance with the TDR measurements (0.3 m prongs) performed before the irrigation, showing a dielectric permittivity of 475 476 4.55, which corresponds to a EM wave velocity of 0.141 m/ns. The forward model of EM wave propagation assumes the presence of only two ground layers, so we 477 are not able to simulate a smoothed wetting front, that is approximated as a sharp 478 discontinuity of dielectric permittivity. The thickness range is fixed, for all times, 479 between 0.3 m and 1 m, with an increment of 0.05 m. The velocity of wet layer is 480 481 sampled in the interval from 0.065 m/ns to 0.1 m/ns, at steps of 1.05×10^{-4} m/ns. 482 Both fundamental and first modes are simulated, setting all possible combinations 483 of the parameter space for a total of about 47000 simulations.

Fig. 5 shows the results of the inversion procedure, where the goodness of fit between experimental and simulated dispersion curves is calculated using the Nash-Sutcliffe index (NSI) (Nash and Sutcliffe, 1970). Fig. 5A reproduces the experimental curve (black dotted line) plotted together with the best-fitting synthetic curves: the light gray lines have NSI values between 0.85 and 0.95, while the dark gray lines show NSI>0.95. At time t_1 1035 curves of the fundamental

490 mode have a NSI>0.95. At time t_2 the fitting of the measured dispersion curve for 491 the fundamental mode is poor, as NSI does not exceed, for any curve, the value of 492 0.87. For this reason we consider in Fig. 5 only the 1124 simulations with NSI>0.85. 493 The 1232 synthetic curves of the first higher mode are used to represent the 494 experimental first mode at time t_3 , where the NSI is greater than 0.95. We inverted 495 the first higher mode for time t_{3} , as at this time the higher mode is much more energetic than the fundamental mode, as shown by Fig. 4. Fig. 5B-C show the 496 497 distribution of the parameters linked to the best simulations: wet layer thickness 498 and wet layer velocity, respectively.

We averaged the parameters of the best simulations to achieve an estimated value for both the velocity and the thickness of the wet layer, at all times. Statistics and ranges of the considered best simulations are summarized in Table 3. The velocity of the wet layer changes slightly over time, with values confined in a narrow range, in all cases very far from the value of the dry sand (0.14 m/ns).

We are less confident in the inversion of time t_2 for two reasons: (1) the fitting between measured and calculated data is poor respect to the other time-steps that show high values of NSI; (2) the experimental dispersion curve is derived from the f_{k} domain, that shows that energy is smeared between fundamental and first higher mode. Therefore, the dispersion curve at time t_2 may be heavily affected by the unfavorable signal to noise ratio for both the fundamental and the first higher mode.

511 It should also be noted that our MC inversion provides a view of the degree of 512 correlation of the two governing parameters (thickness and velocity of the wet 513 layer). Fig. 6 shows the levels of NSI>0.85 plotted in the parameter space,

514 highlighting some degree of positive correlation. However, at times t_1 and t_3 the 515 best fitting simulations (NSI>0.984 for t_1 , NSI>0.987 for t_3), marked as a green area, 516 are centered around small parameter ranges. At time t_2 the green area highlights 517 the simulations with NSI>0.886. Table 3 reports the standard deviations of the 518 parameters associated to the best-fitting simulations that are quite small with 519 respect to the average values.

520

521 <u>5. ERT DATA ANALYSIS</u>

522 The ERT data were collected at the surface using a Syscal-Pro resistivimeter (IRIS Instruments, France). Twenty-four electrodes spaced 20 cm were placed on a 523 524 transect perpendicular to the sprinklers' line, for a total length of 4.6 m (Fig. 1). The acquisition scheme was a dipole-dipole skip zero (dipoles with minimal 525 526 distance equal to one electrode spacing). Reciprocal measurements were acquired 527 and processed to estimate data errors. All the reciprocal measures with the 528 statistical operator RSD (Relative Standard Deviation) exceeding the 5% were 529 removed from the dataset. This reciprocal error analysis leads to a different 530 dataset for each time step. For this reason and to have comparable results, we 531 performed the inversions considering only the quadripoles that are present in all 532 datasets. The common datasets preserve 200 measurements over a total of 231 533 quadripoles, thus data quality is particularly good. We inverted the data as the 534 ratio of electrical resistances at a specific time with respect to the resistance values 535 at the background measurement (in our case the time-step before the irrigation):

$$R = \frac{R_i}{R_0} \cdot R_{hom} \tag{8}$$

536 Where R_i is the electrical resistance at the *i*-th time-step, R_0 is the electrical 537 resistance at the background measure and R_{hom} is the electrical resistance for a homogenous space of 100 Ω m. All the electrical resistances are referred to the 538 539 same quadripole and R is calculated for each measurement in the dataset. As data errors are difficult to estimate in terms of resistance ratios, some degree of 540 541 arbitrary choice is present in ratio inversion. Fig. 7A shows the inversion of the 542 resistivity ratios with respect to background (Eq. 8) applying a smoothness 543 constrain of 3%.

544 This time-lapse ratio inversion clearly shows the variation of the electrical resistivity during the experiment (Fig. 7A). The results of the inversion are sections 545 of the percentage variation of resistivity respect to the background values: values 546 equal to 100 Ω m correspond to unchanged resistivity, while values less or more 547 548 than 100 Ω m show a decreasing or an increasing resistivity, respectively. The 549 inversions were performed using the 2D code developed by Andrew Binley (http://www.es.lancs.ac.uk/people/amb/Freeware/Freeware.htm; Slater et al. 550 551 2000; Cassiani and Binley, 2005; Linde et al., 2006).

Fig. 7B shows the results of the ratio of the inverted absolute profiles with respect to the inversion of the background survey. In this case the profiles are inverted with a data error set at 5%, consistent with the reciprocal error removal procedure, and then a pixel by pixel ratio is computed. From the comparison between Fig. 7A and 7B it is apparent that the two approaches are, in this case, essentially equivalent at showing the evolution of the infiltration process. This similarity corroborates the hypothesis of the 2D symmetry of the infiltration

process along the sprinkler line, since the ERT monitoring is performed on 2Dprofiles, assuming a homogeneous resistivity distribution on the third direction.

In Fig. 7 the infiltration process is clearly visible. The plume of injected fresh water increases moisture content and consequently reduces resistivity. The shape of the plume is the consequence of a non-uniform distribution of irrigation in the direction perpendicular to the sprinklers' line. The distribution of the artificial precipitation is more likely Gaussian in shape, with considerably more water dropping close to the sprinklers. Time-steps t_5 and t_7 are not shown, as only modest variations are present at these late times after the end of the irrigation.

568

569 6. SETUP OF THE COUPLED INVERSION

In this work the modeling based on the coupled-inversion described in Section 2 is 570 571 aimed specifically at the estimation of soil saturated hydraulic conductivity. The physically-based hydrological model CATHY (Camporese et al., 2010) is employed 572 for the numerical solution of Eq. (1) and the simulation of the infiltration 573 experiment. The van Genuchten's parameters necessary for the setup of the 574 575 numerical model were derived from laboratory experiments: residual saturation is 576 fixed at 0.003 and α (the inverse of the air entry suction) is equal to 5.4 m⁻¹. These 577 values are derived from laboratory experiments and are not considered of 578 paramount importance in the context of the given infiltration experiment. Of 579 course a more complete parameter identification scheme could also include them, 580 as described by Manoli et al. (2015) in the context of using ERT data alone.

A careful analysis of Fig. 7 reveal that irrigation was not uniformly distributed inthe direction orthogonal to the sprinkler line, probably due to the presence of

wind. This was taken into account in order to properly simulate the top boundary conditions: the irrigation is modeled with a Gaussian distribution centered at 2.5 m, with variance equal to 0.6 m, both values calculated such that the total flux equals the real irrigation rate. The parameters of the Gaussian distribution are fixed after a trial procedure where we matched the shape of the measured and modeled plume (Fig. 7 and Fig. 10).

589 The parameters of Archie's law (Eq. 3), which are necessary to define the ERT observation operator, are spatially uniform for considered field study. The 590 591 exponent *n* is set to 1.27 as reported in Cassiani et al. (2009c), where the value is 592 obtained from laboratory calibration on the site's sediments. The initial soil 593 electrical resistivity $\rho(t_0)$ is set equal to 1300 Ω m, based on the averaged value obtained by the inversion of background ERT measures. In order to apply Eq. (3), 594 595 we need also an estimation of the initial volumetric water content, $\theta(t_0)$. For our 596 field experiment this is estimated from background GPR and TDR measurements. A value $\theta(t_0) = 0.07$ is obtained by applying the petrophysical relationship of Topp et 597 598 al. (1980):

599

$$\theta = (-530 + 292\varepsilon_r - 5.5\varepsilon_r^2 + 0.043\varepsilon_r^3) \cdot 10^{-4}$$
(5)

600 where ε_r is the bulk soil dielectric permittivity. A moisture content value of 7% 601 corresponds to $S_w(t_0)$ of 0.212 assuming a porosity of 0.33 as estimated by 602 Cassiani et al. (2009b) for the considered field sediments.

In this particular case, we are interested in the value of the saturated hydraulic conductivity K_s , that is difficult to identify in unsaturated conditions by direct measurements. The methodology presented in Manoli et al. (2015) describes K_s with a lognormal probability distribution which mean and variance are updated

at each assimilation time. Here, the prior values of the hydraulic conductivity meanand variance are summarized in Table 5.

The iterative procedure is particularly advantageous when geophysical measurements of different nature (e.g. ERT and GPR) are available for the assimilation, as in the case we consider here. In fact, the independent assimilation of different measurements is to prefer to the joint assimilation of the measurements, since the latter requires the introduction of an artificial normalization to weight the measurements.

In this paper the procedure is used to provide the "best possible" estimate of K_s for the site using both ERT and GPR data. We adopt a strategy that is particularly clear in assessing the information content of each dataset and of the two datasets together. In particular, we produce the following four assimilation schemes:

A. a scheme assimilating only ERT data (similar to the one proposed by Manoli
et al., 2015);

B. a scheme assimilating only GPR data, based on the depth of the infiltration
front estimated from the guided wave analysis (see section 3);

624 C. a scheme that assimilates alternatively ERT and GPR leading to a final625 estimate that accounts for both;

626 D. a scheme analogous to C, but using GPR and ERT in the reverse order - to
627 check convergence stability (the first iteration starts assimilating GPR data,
628 instead of ERT data).

629 The advantage of assimilating both ERT and GPR measurements is the 630 integration of different information. In this kind of experiment (irrigation

631 monitored on the ground surface), the low sensibility of the ERT array at large 632 depths may be a disadvantage; so the infiltration front may be spread over a broad 633 area, since the most part of the energy is focalized along current paths that cross 634 the wet zone. GPR WARR surveys may be a useful addition to the information 635 obtained from ERT, as GPR can constrain the location of the water front at depth.

636

637 **<u>7. MODELLING RESULTS</u>**

The particle filter algorithm assimilates the geophysical data with four different 638 639 schemes (Fig. 8). Each assimilation scheme leads to a probability distribution of the simulated parameters: in this case K_s is the objective of the coupled inversion. 640 641 The evolution of the K_s distribution during the assimilation procedures is summarized in Fig. 8. For each assimilation scheme, 3 different prior K_s -642 643 distributions are tested to verify the stability of the inversion procedure. It evinces that the convergence towards the estimated K_s value, at the end of the iteration 644 process, is not depending on the initial parameter's range. 645

646 The estimated values of K_s are only slightly different from scheme to scheme: for case A: 1.010⁻⁵ m s⁻¹, for case B: 2.6 10⁻⁵ m s⁻¹, for case C: 1.1 10⁻⁵ m s⁻¹, for case 647 D: 1.1 10^{-5} m s⁻¹. Note that the differences in the estimated K_s are almost negligible 648 649 for practical applications. Assimilating both ERT and GPR we obtain the same 650 $K_{\rm s}$ value, irrespective of the order of assimilation. The assimilation of only ERT 651 data (Fig. 8A) provides a K_s estimate that is very similar to the ERT-GPR 652 assimilations. The assimilation of the GPR waterfront depths provides a value of K_s about two times larger than the other estimates (Fig. 8B). We attribute this 653

results to the large uncertainty associated to the GPR measurement and analysis,

655 in particular at the time *t2*.

Forward hydrological models are then run with the estimated parameters and
the results are compared to the geophysical measurements (Tables 4 and 6).
Schemes *C* and *D* provide essentially the same hydrological model. The mean and
standard deviations of the posterior distributions for the four cases are listed in
Table 5 (together with the prior parameters).

661 In Table 4 the waterfront position inverted from the GPR signal is compared to the simulated location of the saturation front. Note that the water front locations 662 estimated from the coupled inversions with the GPR assimilation leads to slightly 663 664 deeper water front estimations, while ERT and ERT-GPR assimilations conduct to very similar results. The GPR contribution in the combined inversion with ERT 665 drives the estimated waterfront slightly deeper than estimated by ERT only. The 666 waterfront depths from GPR data alone are definitely more problematic to 667 interpret (see also Fig. 9), with uneven penetration speed between time intervals 668 669 1-2 and 2-3. Note that, as discussed in Section 3, time 2 is a problematic acquisition 670 for GPR, with energy spread over two modes and a more difficult estimation of 671 infiltration front depth.

The forward hydrological models are also compared against the ERT field (resistance) dataset (Tab. 5). In this case the simulated hydrological states are converted into geophysical quantities via Eq. 4, and a geophysical forward model (Eq. 3) is run to obtain simulated ERT resistance data. Not surprisingly, the forward model that best matches the field measurements is derived from the assimilation of the sole ERT data. Anyway the assimilation of both ERT and GPR

678 shows a very good fit to the measured ERT, while the assimilation scheme of only

679 GPR-derived waterfronts is distant from the information achieved from ERT680 survey.

Fig. 9 shows the distribution of moisture content predicted by the flow models
with the parameters obtained from data assimilation. These saturation profiles are
compared against:

the moisture content profiles one could obtain by translating directly the
resistivity inverted images (Fig. 7) using the known Archie's law
parameters (Eq. 4).

687 2. the locations of the infiltration front as estimated from GPR inversion688 (Section 3).

the estimation of the degree of saturation measured by TDR probes placed
at the mid-point of the ERT profile; relative dielectric permittivity is
translated into water content using Eq. (5).

There is no doubt that the data assimilated simulations are superior at providing
estimates of moisture content profiles that, while slightly different from each other,
are both consistent with data and model assumptions (most of all, mass balance
and hydraulic conductivity homogeneity).

The TDR data are used as validation of the modeled water saturation curves (Fig. 9). The values are consistent with the hydrological models, that show a rapidlymoving saturation front at the first time steps. Unfortunately the TDR probes reach the maximum depth of only 0.3 m, so no information is available for the deeper portions.

701 For the sake of completeness, we also inverted the synthetic ERT data (Fig. 7C) 702 to provide a direct comparison with the ρ distributions achieved by field 703 measurements (Fig. 7A). In addition, Fig. 10 shows the "true" resistivity structure 704 as simulated by the hydrological model in the combined ERT-GPR data 705 assimilation case. Comparing Figs. 7 and 10, note how inverted and "true" 706 resistivity images tend to diverge at late times, when the front reaches the deeper 707 zones where ERT has the lowest sensitivity, and inversion regularization takes 708 over and smears the images at depth. Consistently, the mass balance derived from 709 ERT data as calculated for the coupled and the uncoupled hydro-geophysical 710 inversions (Table 7) shows the weaknesses of the uncoupled approach for the 711 problem at hand. The uncoupled approach leads to a cumulative volume of injected water over time that strongly overestimates the effective amount of irrigated 712 713 water.

Note that in the literature underestimation of mass balance is more commonly observed (e.g., Singha and Gorelick, 2005), but this fact is dependent primarily on the acquisition scheme and electrode geometrical configuration (e.g. cross-hole versus surface measurements, as in this work).

718

719 <u>8. CONCLUSIONS</u>

Hydro-geophysical techniques are extremely useful in monitoring the hydrological processes acting in the vadose zone and the data can be effectively translated into hydrological quantities, particularly state variables such as moisture content. The presented field case study analyzes a controlled irrigation

test in an unsaturated subsoil with a plain terrain and nearly homogeneous sandysoil.

726 The adopted hydro-geophysical methodology may strongly affect the results of 727 the hydro-geophysical inversion and consequently the hydrological parameter estimations. An approach, that fully couples hydrological modeling and 728 geophysical measurements in a data assimilation procedure, leads to more 729 730 accurate results. Avoiding the geophysical inversion of the data, we reduce the 731 uncertainty in the hydrological quantities estimation, since no artifacts are 732 inserted in the method by solving an inverse problem. The errors that may be 733 present are due only to data acquisition and model choosing, as in any hydro-734 geophysical issue. Of course an analysis of the inverted data is generally necessary, not only to ascertain the data quality, but also to direct a correct choice of the 735 736 hydrological model needed to explain the data (see, e.g., discussion in Camporese 737 et al., 2011). One of the advantages of the coupled approach, that includes a 738 stochastic process, is the proper conservation of mass. This aspect is often a key issue of the uncoupled approach, where the calibration of hydrological models via 739 740 geophysical inverted data may lead to inconsistent results that may jeopardize the 741 user's confidence in the method.

742 In the present field case both ERT and the infiltration front estimated with the 743 GPR data are considered in the data assimilation process, using a Sequential 744 Importance Resampling (SIR) that allows a flexible assimilation of either or both 745 datasets in a natural, non-subjective manner (i.e. without arbitrary weighting of 746 one dataset with respect to the other). From this procedure the information 747 content of each dataset in the assimilation procedure emerges naturally.

748 In this particular case study, it is apparent that ERT data provide most of the 749 information needed to a robust hydraulic conductivity estimation. GPR, albeit 750 being apparently of easy interpretation in its time-lapse evolution (see Figure 3), at a more in-depth quantitative analysis shows its intricacies linked to the inversion 751 752 of multi-modal dispersion guided waves. As the energy distribution over different modes changes over time due to the changing geometry of the wet layer, the 753 inversion of GPR data requires particular attention and ultimately delivers weak 754 755 information on the infiltration process.

756 The comparison between coupled and uncoupled hydro-geophysical inversions 757 shows that, in this particular case, the latter is superior. This happens primarily because the monitoring of type of experiment that we consider (irrigation and 758 infiltration from the ground surface) depends strongly on our ability to image the 759 760 processes honoring mass balance. In this respect, the uncoupled approach is not 761 capable of reproducing the real state of the system and consequently the mass 762 balance. The uncoupled approach may therefore lead to erroneous parameter 763 estimate. It should be noted how other problems may be less prone to suffering 764 from an uncoupled approach (see e.g. Camporese et al., 2011).

765

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TABLES

Irrigation	Irrigation start	Irrigation end	Cumulative water		
steps	[min]	[min]	volume [m ³]		
1	0	115	2.509		
2	146	233	4.127		
3	264	327	5.652		

MAS

Table 1. *Time schedule and irrigated volumes for the infiltration experiment.*

Geophysical	Starting time of the survey [min]								
techniques	Background								
	t _o	t 1	t2	t3	t4	t₅	t ₆	t7	t ₈
GPRWARR	-10	115	233	327	-	-	-	-	-
ERT	-5	120	240	335	1030	1150	1420	1480	1540

983

t in the second se Table 2. Time schedule of the geophysical acquisitions; time is referred to the

Time step	Averaged thickness [m]	Standard deviation of thickness [m]	Averaged velocity [m/ns]	Standard deviation of velocity [m/ns]	Number of averaged simulations	NSI range of averaged simulations
<i>t</i> ₁	0.46	0.031	0.091	0.0013	197	0.984-0.987
<i>t</i> ₂	0.49	0.019	0.074	0.0006	106	0.886-0.889
<i>t</i> ₃	0.74	0.016	0.081	0.0007	83	0.987-0.990

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Table 3. Statistics of the GPR slab waveguide simulations that best fit the

989

measured dispersion curves.

Time-step	t_1	t_2	t_3	Mean Error
	(m)	(m)	(m)	(m)
GPR inversion	-0.46	-0.49	-0.74	
Posterior ERT	-0.32	-0.52	-0.66	0.083
Posterior GPR	-0.38	-0.61	-0.79	0.083
Posterior ERT-GPR	-0.34	-0.54	-0.70	0.070

991

992 Table 4. Infiltration front depth for the first three time-steps, obtained from GPR-

993 *EM-waveguide inversion and from posterior hydrological forward models. The last*

994 column is the average absolute error between the waterfront positions measured

, rt , logical ; with the GPR and those estimated with the posterior hydrological forward models.

Prior distribution		Posterior distribution									
		ERT		GPR		ERT+GPR		GPR+ERT			
Mean	St. dev.	Mean	St. dev.	Mean	St. dev.	Mean	St. dev.	Mean	St. dev.		
m/s	m/s	10 ^{-₅} m/s	10 ⁻⁵ m/s	10 ⁻⁵ m/s	10 ⁻⁵ m/s	10 ⁻⁵ m/s	10 ⁻⁵ m/s	10 ⁻⁵ m/s	10 ⁻⁵ m/s		
1×10 ⁻⁷	1×10 ⁻⁷	0.99	0.014	2.50	0.148	1.15	0.014	1.11	0.015		
1×10⁵	1×10⁻⁵	1.02	0.008	2.63	0.083	1.14	0.076	1.08	0.018		
1×10 ⁻³	1×10 ⁻³	0.90	0.018	2.86	0.053	1.17	0.032	1.06	0.012		

Table 5: Prior and posterior distributions of the hydraulic conductivity **K**_s for the

different data assimilation schemes

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Time-step	t_1	t_2	t_3	t_4	t_5	t_6	<i>t</i> 7	t_8	Mean
Posterior ERT	3.5	4.3	3.7	3.1	3.1	3.4	3.5	3.6	3.525
Posterior GPR	3.6	4.4	3.7	4.4	4.5	5.1	5.3	5.4	4.550
Posterior ERT- GPR	3.5	4.2	3.6	3.2	3.2	3.6	3.7	3.8	3.600

1007

1008 Table 6. Root mean square relative error between the field measured electric 1009 resistance value sand those simulated with the posterior hydrological forward 1010 models (results in %). The last column is the mean in time of these errors. The 1011 relative error is adopted because the electric resistances vary over several orders of

		Cumulative water volume						
Irrigation	Irrigation	Effective	Coupled	d model	Uncouple	ed model		
steps	time [min]	injected volume[m ³]	Volume [m ³]	% error	Volume [m ³]	% error		
1	115	2.509	2.354	6.2	4.181	66.6		
2	233	4.127	3.997	3.1	7.713	86.9		
3	327	5.652	5.564	1.6	9.559	69.1		

Table 7. *Mass balance achieved with coupled and uncoupled hydro-geophysical*

inversions.

1019 **FIGURES**



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1021

Figure 1. Scheme and location of the experiment: (a) aerial view of the field with the
irrigated zone highlighted in blue; (b) the sprinkler line during the irrigation; (c)
scheme of the geophysical surveys and position of the irrigated soil.

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1028 Figure 2. Background WARR survey with the identification of the direct wave
1029 through the ground.



1033Figure 3. Field measured WARR radargrams at the times t_1 , t_2 and t_3 . A) On the left,1034the radargrams are filtered only by the "dewow" procedure (traces are normalized).1035B) On the right, the same radargrams are displayed after the preprocessing (muting1036and FIR filter).



1038Figure 4. Analysis of the GPR soundings in the frequency domain. (a) On the left, the1039f-kdomain are displayed with the superimposition of the maxima of the spectral1040density (magenta dots for main maxima, white dots for local maxima). Power1041spectrum density scale in V^2 /Hz. (b) On the right, the dispersion curves inferred from1042f-k maxima: red and blue dots correspond to absolute and local maxima, respectively.1043



1044 1045

1046Figure 5. Parameterizations of the simulations of slab waveguides that best fit the1047measured dispersion curves. (a) Superposition of the field-derived dispersion curves1048(black dotted lines) and of the best simulated dispersion curves: light gray lines with10490.85<NSI>0.95 and dark gray lines with NSI>0.95. (b) Wet layer thickness from the1050best simulations plotted against NSI>0.85. (c) Wet layer velocity from the best

- 1051 simulations plotted against NSI>0.85.
- 1052





Figure 6. Correlation between the simulated parameters: velocity and thickness of 1055 Gre .eps: M3. the layer that guides EM waves; color bar is NSI value. Green polygon highlights the 1056 simulations with highest NSI values for each time-steps: NSI>0.984 for t₁, NSI>0.886



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Figure 7. Time-lapse of inverted electrical resistivity profiles displayed as percentage of variation respect to background. A) Inversion of the ratio of apparent resistivities, measured at the field, respect to background survey. B) Ratio of the inverted profiles related to background inversion. C) Inversion of the ratio of synthetic apparent resistivities, simulated through the hydrological model, respect to the assumed homogeneous background state.

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 $\begin{array}{c} 1070\\ 1071 \end{array}$

Figure 8. K_s-distributionduring the iteration of the data assimilation framework. 1072 The lines of different colors (blue, red and green) point out different initial 1073 1074 distribution of the parameter: solid line is the mean of the distribution, dashed lines 1075 are the maximum and minimum vales in the range. (a) sequential assimilation of the 1076 ERT data. (b) sequential assimilation of the waterfront position from GPR data. (c) 1077 sequential assimilation of ERT and GPR information. (d) sequential assimilation of 1078 GPR and ERT information. The vertical lines, including the graph extremes, indicate 1079 the 9 measurement instants (t_0 to t_8). 1080



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1083 **Figure 9.** Vertical profiles of water saturation, extrapolated on the position of the 1084 sprinklers line. Solid lines of red, blue and green colors are the results of forward 1085 hydrological models obtained with the K_s estimation assimilating only ERT, only GPR 1086 and both techniques, respectively. Gray solid line is the result of the uncoupled ERT 1087 inversion. The horizontal black dot-dashed line is the estimation of waterfront 1088 location from GPR-EM-waveguide inversion. The vertical black dashed lines are the 1089 estimated water saturation achieved by TDR probes (15 and 30 cm length).

1090



1093 **Figure 10.** Electrical resistivity sections at different time steps, derived by the 1094 hydrological model inferred from the assimilation of both ERT and GPR datasets.