



Theoretical Interpretation of Pass 8 *Fermi*-LAT $e^+ + e^-$ Data

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Abstract

The flux of positrons and electrons ($e^+ + e^-$) has been measured by the *Fermi* Large Area Telescope (LAT) in the energy range between 7 GeV and 2 TeV. We discuss a number of interpretations of Pass 8 *Fermi*-LAT $e^+ + e^-$ spectrum, combining electron and positron emission from supernova remnants (SNRs) and pulsar wind nebulae (PWNe), or produced by the collision of cosmic rays (CRs) with the interstellar medium. We find that the *Fermi*-LAT spectrum is compatible with the sum of electrons from a smooth SNR population, positrons from cataloged PWNe, and a secondary component. If we include in our analysis constraints from the AMS-02 positron spectrum, we obtain a slightly worse fit to the $e^+ + e^-$ *Fermi*-LAT spectrum, depending on the propagation model. As an additional scenario, we replace the smooth SNR component within 0.7 kpc with the individual sources found in Green's catalog of Galactic SNRs. We find that separate consideration of far and near sources helps to reproduce the $e^+ + e^-$ *Fermi*-LAT spectrum. However, we show that the fit degrades when the radio constraints on the positron emission from Vela SNR (which is the main contributor at high energies) are taken into account. We find that a break in the power-law injection spectrum at about 100 GeV can also reproduce the measured $e^+ + e^-$ spectrum and, among the CR propagation models that we consider, no reasonable break of the power-law dependence of the diffusion coefficient can modify the electron flux enough to reproduce the observed shape.

Key words: cosmic rays – astroparticle physics – ISM: supernova remnant – acceleration of particles

1. Introduction

Investigation of the leptonic component of cosmic rays (CRs) provides invaluable insight into the properties of CR sources and CR propagation. At present, the most accurate measurements of the different observables related to CR leptons have been performed by the AMS-02 experiment (Accardo et al. 2014; Aguilar et al. 2014a, 2014b). The data provided by AMS-02 have been interpreted within several theoretical models: e.g., Blum et al. (2013) discuss the possibility of a purely secondary origin of positrons, while Bergstrom et al. (2013), Gaggero et al. (2014), Mertsch & Sarkar (2014), Delahaye et al. (2014), Jin et al. (2017), Ibarra et al. (2014), Boudaud et al. (2015), Lin et al. (2015), Yuan et al. (2015), and Di Mauro et al. (2016) investigate the properties of additional positron sources (pulsars, dark matter, or acceleration within supernovae). Furthermore, CR leptons have been investigated in connection with other observables, such as hadronic CR fluxes (Kachelriess et al. 2015; Tomassetti & Donato 2015; Tomassetti 2015; Lipari 2017) or synchrotron emission across the Galaxy (Di Bernardo et al. 2013; Orlando & Strong 2013; Planck Collaboration 2016).

The *Fermi*-LAT Collaboration has recently reported a new measurement of the inclusive CR positron and electron ($e^+ + e^-$) spectrum between 7 GeV and 2 TeV, obtained with almost seven years of Pass 8 data (Abdollahi et al. 2017a, 2017b). The LAT spectrum suggests the presence of a break at about 50 GeV, but this feature is not statistically significant when the systematic uncertainty on the energy measurement is taken into account. In this work, we choose to

use the new LAT spectrum without taking into account this specific uncertainty. In that case, a fit to the LAT spectrum between 7 GeV and 2 TeV with a broken power law is reported to yield a break at $E_b = (53 \pm 8)$ GeV with spectral indices below and above the break $\gamma = (3.21 \pm 0.02)$ and $\gamma = (3.07 \pm 0.02)$. We refer to Abdollahi et al. (2017b) for a discussion of the difference between AMS-02 and *Fermi*-LAT $e^+ + e^-$ spectrum that is at the level of 1.7σ for $E > 30$ GeV.

Here we study the *Fermi*-LAT results, including the potential new feature of a spectral break, within the theoretical model proposed in Di Mauro et al. (2014, 2016) and Manconi et al. (2017), which has already been used to study the AMS-02 electron and positron spectra. In this model, electrons and positrons are either emitted by primary astrophysical sources, such as supernova remnants (SNRs) and pulsar wind nebulae (PWNe), or they are produced as a secondary CR component, due to collisions of protons and helium nuclei with the interstellar medium (ISM).

The paper is organized as follows. Section 2 describes the different contributions to the $e^+ + e^-$ flux, while Section 3 illustrates the model that we use for the propagation of electrons and positrons through the Galaxy. Sections 4 and 5 discuss our analysis and results, and we conclude in Section 6.

2. Contributions to the $e^+ + e^-$ Flux

Electrons and positrons can be products of a variety of processes that take place in the Galaxy. In this section, we briefly outline of the different production mechanisms and we describe

our modeling. More details can be found in Delahaye et al. (2010), Di Mauro et al. (2014, 2016), and Manconi et al. (2017).

2.1. Supernova Remnants

SNRs are commonly considered as main accelerators of Galactic CRs. Charged particles scatter repeatedly upstream and downstream of the shock wave that is generated by the stellar explosion and receive an increase in energy each time they cross the shock front. This mechanism of diffusive shock acceleration produces a spectrum of accelerated particles that we assume to be described in terms of a power law with an exponential cutoff:

$$Q(E) = Q_{0,\text{SNR}} \left(\frac{E}{E_0} \right)^{-\gamma_{\text{SNR}}} e^{-\frac{E}{E_c}}, \quad (1)$$

where $E_0 = 1$ GeV. The injection spectrum in Equation (1) is related to the total energy (in units of erg or GeV) emitted in electrons by SNRs (analogously can be written for electrons and positrons by PWN)

$$E_{\text{tot,SNR}} = \int_{E_{\text{min}}}^{\infty} EQ(E)dE, \quad (2)$$

where we fix $E_{\text{min}} = 0.1$ GeV. We fix the average Galactic supernova explosion rate (usually indicated with Γ_*) to 1/century. The spectrum of particles accelerated by SNRs is therefore completely described by three parameters: the normalization $Q_{0,\text{SNR}}$ or, equivalently $E_{\text{tot,SNR}}$, the spectral index γ_{SNR} , and the cut-off energy E_c . As mentioned in Di Mauro et al. (2014), radio measurements in the SNR region can provide insight into the values of $E_{\text{tot,SNR}}$ through the magnetic field and γ_{SNR} . As for the cut-off energy E_c , both theoretical considerations and observational evidence place it in the multi-TeV range. Radio and gamma-ray observations indicate that the energy cutoff should be in the TeV range (see, e.g., Reynolds & Keohane 1999; Aharonian 2001; Hoppe et al. 2008; Aharonian et al. 2008; Acciari et al. 2010). Throughout this paper, we assume $E_c = 5$ TeV, for the acceleration both by SNRs as well as PWNe (Equation (3)). One important aspect is that SNRs accelerate particles that are already present in the environment of the explosion, namely the ISM: since, in the ISM, electrons are much more abundant than positrons, SNRs can be considered to accelerate only electrons.

As explained in detail in Di Mauro et al. (2014), for the purposes of our analysis, we divide the SNRs into two categories. We define here $R \equiv |\mathbf{r} - \mathbf{r}_\odot|$, where r is the Galactocentric radial coordinate along the Galactic plane and r_\odot is the solar position. According to their distance from the Earth, we consider the following.

1. Far SNRs ($R > R_{\text{cut}}$): they are treated as a population of sources that are spatially distributed according to the Lorimer (2004; hereafter L04) or Green (2015; G15) distributions. The spatial distribution G15 is a new estimation based on the most-recent Galactic SNR catalog (Green 2014). The distribution L04 is for pulsars that can be used as tracers of the SNR distribution. Far SNRs are assumed to contribute to CR electron production as in Equation (1), with a common normalization $E_{\text{tot,SNR}}$ and spectral index γ_{SNR} . These are usually taken to be free parameters in our fits.

2. Near SNRs ($R \leq R_{\text{cut}}$): these sources are taken from Green's catalog (Green 2014), which provides information on their distance, age, magnetic field B , and γ_{SNR} . As in Di Mauro et al. (2016) and Manconi et al. (2017), we allow separate free normalization of the flux generated by the Vela SNR, which is the most powerful source among the nearby SNRs.

We can treat the cut as a cylinder centered at Earth, with a radius equal to R_{cut} . More details are given in Section 3.1. The motivation to separate SNRs into near and far components is due to the fact that far SNRs contribute to the electron flux mostly at low energies, while local sources likely dominate the high-energy tail. For the latter, we have more specific information from Green's catalog, which allows us to treat the nearby SNR component as individual sources with physical parameters based on observations at some wavelength (mostly radio). This allows us to investigate in greater depth the high-energy portion of the $e^+ + e^-$ spectrum. We perform dedicated analyses for different choices of the R_{cut} parameter, including $R_{\text{cut}} = 0$, which extends the average distribution of the SNR population to the whole Galaxy. In this case clearly no catalog sources are included.

2.2. Pulsar Wind Nebulae

Pulsars can produce a flux of electrons and positrons. As described, e.g., in Shen (1970), Ruderman & Sutherland (1975), Cheng et al. (1976), Cheng et al. (1986), Harding & Ramaty (1987), Arons (1996), Zhang & Cheng (2001), and Amato (2014), electrons stripped from the neutron star surface generate pair cascades in the pulsar magnetosphere. These electrons and positrons are further accelerated in the pulsar's stripped wind and/or at its termination shock, beyond which a nebula of very high-energy particles forms: the PWN. As for SNRs, we assume that the energy spectrum of electrons and positrons emitted by a PWN can be described by a power law with an exponential cutoff:

$$Q(E) = Q_{0,\text{PWN}} \left(\frac{E}{E_0} \right)^{-\gamma_{\text{PWN}}} e^{-\frac{E}{E_c}}. \quad (3)$$

In our modeling, we express the normalization of the PWN spectrum $Q_{0,\text{PWN}}$ in terms of the spin-down energy of the pulsar W_0 , which is the energy emitted by the pulsar as it slows down (Hooper et al. 2009):

$$W_0 \approx \tau_0 \dot{E} \left(1 + \frac{t_*}{\tau_0} \right)^2, \quad (4)$$

where t_* is the present age of the pulsar, τ_0 is the typical pulsar decay time, and \dot{E} is the spin-down luminosity. The normalization $Q_{0,\text{PWN}}$ is therefore obtained from the relation

$$\int_{E_{\text{min}}}^{\infty} dE E Q(E) = \eta_{\text{PWN}} W_0, \quad (5)$$

where η_{PWN} is the efficiency factor for the conversion of the spin-down energy into electrons and positrons.

As in Di Mauro et al. (2014, 2016) and Manconi et al. (2017), we consider in our analysis all the pulsars in the continuously updated ATNF catalog,⁷ which provides the spin-down energy,

⁷ <http://www.atnf.csiro.au/people/pulsar/psrcat/>. We use catalog version 1.55.

age, and distance of each PWN. For definiteness, we select only PWNe with ages greater than 50 kyr. This is based on the fact that the release of electron and positron pairs in the ISM is estimated to occur at least 40–50 kyr after the formation of the pulsar (Blasi & Amato 2011). The efficiency η_{PWN} and the spectral index γ_{PWN} are our free parameters.

2.3. Secondary Positrons and Electrons

Electrons and positrons of secondary origin are produced by interactions of primary CR nuclei with the gas nuclei in the ISM. The source term for this contribution is

$$Q_{\text{sec}}(\mathbf{x}, E_e) = 4\pi \sum_{i,j} \int \Phi_{\text{CR},i}(\mathbf{x}, E_{\text{CR}}) \times \frac{d\sigma}{dE_e} \bigg|_{i,j} (E_{\text{CR}}, E_e) n_{\text{ISM},j} dE_{\text{CR}}, \quad (6)$$

where i runs over the primary CR species of flux density $\Phi_{\text{CR},i}$ and j over the target nuclei in the ISM of density $n_{\text{ISM},j}$ considered constant with $n_{\text{H}} = 0.9 \text{ cm}^{-3}$ for hydrogen and $n_{\text{He}} = 0.1 \text{ cm}^{-3}$ for helium. n_{ISM} is confined in a thin disk of half height 100 pc (see, e.g., Delahaye et al. 2009, and references therein). \mathbf{x} is the position vector in the Galaxy and $d\sigma/dE_e$ is the differential cross-section for electron and positron production in the spallation reaction under consideration (Kamae et al. 2006).

We determine the source term of Equation (6) following the same approach detailed in Di Mauro et al. (2014) and Di Mauro et al. (2016), where we adopt primary CR fluxes obtained by fitting the AMS-02 data on protons and helium. The parameters of the spectra determined in this fit are reported in Di Mauro et al. (2016).

3. Transport of Charged Particles in the Galaxy

Electron and positron transport in the Galaxy is treated by means of a semi-analytical model, following the same approach as Delahaye et al. (2010) and Di Mauro et al. (2014). The semi-analytical model is simplified compared to codes like GALPROP (Moskalenko & Strong 1998; Strong & Moskalenko 1998; Vladimirov et al. 2011) and DRAGON (Evoli et al. 2008, 2017); by numerically solving the transport equation, these codes can implement more complex features of the Galactic environment and its geometry (e.g., Galaxy spiral arms or small scale inhomogeneities).

However, we expect such complex features to have at most a mild impact on the problem at hand. This is, for example, the case of implementing spiral arms in the distribution of SNRs, as we discuss in the Appendix and in Section 4.2. In fact, as discussed in Delahaye et al. (2010), due to energy losses, both primary and secondary leptons that reach Earth are produced predominantly within a few kiloparsecs from the Sun. In this small region of the Galaxy, the considerations for evaluating CR transport (e.g., the magnetic field, the interstellar radiation field, and the diffusion coefficient) are unlikely to have a strong spatial dependence and therefore our semi-analytical approach is an acceptable approximation. In addition, relative to fully numerical methods, the semi-analytical model has faster execution times and allows for larger parameter-space scans.

Let us provide a brief summary of the model we employ. For details, we refer to Delahaye et al. (2010). Independent of the production mechanism, charged CRs propagate through the

Galactic magnetic field irregularities and experience a number of different physical processes. CRs are confined by Galactic magnetic fields of mean value $B \sim 1\text{--}5 \mu\text{G}$ in a propagation zone called the diffusive halo, which we model as a thick disk, which matches the structure of our Galaxy. The radial extension of the disk is fixed to $r_{\text{disc}} = 20 \text{ kpc}$, while its vertical half height is quite uncertain, $L \simeq 1\text{--}15 \text{ kpc}$. The electron number density per unit energy $\psi = \psi(E, \mathbf{x}, t)$ is linked to the electron flux $\Phi = \frac{v}{4\pi} \psi$, where v is the electron velocity (de facto $v = c$). The transport of electrons with energy E in the diffusive halo is described through the transport equation:

$$\partial_t \psi - \nabla \cdot \{K(E) \nabla \psi\} + \partial_E \{b(E) \psi\} = Q(E, \mathbf{x}, t), \quad (7)$$

which accounts for the main processes that charged leptons experience while propagating to the Earth. Above a few GeV of energy the propagation of electrons is dominated by spatial diffusion, parameterized through a diffusion coefficient $K(E)$, and energy losses $b(E)$. Specifically, synchrotron emission and inverse Compton (IC) scattering dominate over ionization, adiabatic, and bremsstrahlung energy losses (see, e.g., Delahaye et al. 2009). Diffusion in momentum space due to motions of the turbulent magnetic field, as well as the effect of the Galactic convective wind, are sub-dominant for electrons that reach the Earth with energies $E \gtrsim 5 \text{ GeV}$ (Delahaye et al. 2009). We recall that in our model a fully relativistic description of IC energy losses and a mean value of $B_{\text{sync}} = 3.6 \mu\text{G}$ are used (Delahaye et al. 2009). The diffusion coefficient can be, in general, a function of position in the Galaxy $K(E, \mathbf{x})$, as done, e.g., in Tomassetti (2015). However, the propagation scale (see Equation (16) below) for high-energy electrons is a few kiloparsecs (Delahaye et al. 2010). Furthermore, the diffusion structure of our Galaxy is still not well known. We therefore assume a spatially uniform $K(E)$ throughout the diffusive halo, which permits a full semi-analytical solution:

$$K(E) = \beta K_0 (R/1\text{GV})^\delta \simeq K_0 (E/1 \text{ GeV})^\delta, \quad (8)$$

where the right-hand side is valid because the rigidity of electrons is $R \sim E$ and $\beta \simeq 1$ at the energies under consideration.

The propagation parameters (δ, K_0, L) are generally constrained by means of the secondary-to-primary ratio B/C computed within the same model and confronted with CR data. Specifically, we will use the MED and MAX sets of parameters (Donato et al. 2004; $\delta = 0.70$, $K_0 = 0.0112 \text{ kpc}^2/\text{Myr}$, and $L = 4 \text{ kpc}$ for MED and $\delta = 0.46$, $K_0 = 0.0765 \text{ kpc}^2/\text{Myr}$, and $L = 15 \text{ kpc}$ for MAX), since the MIN model has been disfavored by studies of positrons at low energies (Lavalley et al. 2014). We also verified that the new parameter sets recently obtained by Kappl et al. (2015; hereafter Kappl2015) and Genolini et al. (2015; hereafter Genolini2015) from the preliminary AMS-02 B/C data (Oliva 2015) give electron fluxes that fall between our MED and MAX results. As we will discuss in the sections of the results, using other propagation models would slightly modify the values of some parameters in our models without, however, changing our conclusions.

Equation (7) is solved according to the semi-analytical model extensively described in Delahaye et al. (2010) and Di Mauro et al. (2014). The solutions for a smooth and steady

distribution of sources and for a discrete and time-dependent case are outlined in the next two subsections. The solutions for secondary electrons and positrons is computed as described in Delahaye et al. (2009), to which we refer for details.

3.1. Smooth Distribution of Sources in the Galaxy

One of the components of our models is electrons produced by a smooth distribution of SNRs. Specifically, this component is from the SNRs located at $R > R_{\text{cut}}$ (where R_{cut} can be allowed to go to zero). The spatial distribution of these sources is taken from existing distribution models, built from the catalogs of Galactic sources. Samples are usually corrected for observational selection effects, depending on the nature of the source data, for example, radio or gamma-rays. Most of SNR-based models separate the vertical and the radial dependencies as

$$\rho(r, z) = \rho_0 f(r) e^{-\frac{|z|}{z_0}}, \quad (9)$$

where $z_0 = 0.1$ kpc, r is the distance from the Galactic center along the Galactic plane, and z indicates the location in the vertical (away from the plane) direction. In what follows, we fix the normalization coefficient ρ_0 to 0.007 kpc^{-3} such that the spatial distribution is normalized to unity within the diffusive halo. Our benchmark radial distribution model is G15, based on the ‘‘bright’’ sample of 69 SNRs above the nominal surface brightness limit of $\Sigma_{1\text{GHz}} = 10^{-20} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1}$, for which the Green’s catalog of Galactic SNR is thought to be nearly complete. The G15 distribution can be parameterized as

$$f(r)_{\text{G15}} = \left(\frac{r}{r_\odot}\right)^{a_1} e^{-a_2 \frac{r-r_\odot}{r_\odot}}, \quad (10)$$

where $a_1 = 1.09$ and $a_2 = 3.87$, the Galactocentric distance of the Earth is fixed to $r_\odot = 8.33$ kpc (Gillessen et al. 2009). For comparison, we also consider the widely used radial distribution model L04 derived from the ATNF Galactic pulsar sample and given by

$$f(r)_{\text{L04}} = r^a e^{-\frac{r}{r_0}}, \quad (11)$$

where $a = 2.35$ and $r_0 = 1.528$ kpc.

In the semi-analytical approach, steady-state solutions of Equation (7) can be solved by replacing the energy dependency E with a pseudo-time $\tilde{t}(E)$. This leads to an inhomogeneous heat equation, whose solutions are given in terms of a Green’s function formalism (Baltz & Edsjo 1998). For a complete discussion of solutions and different approximations, see Baltz & Edsjo (1998), Delahaye et al. (2010), and Salati et al. (2010). The steady-state solution for the electron flux at Earth $\mathbf{x}_\odot = (r_\odot, 0, 0)$ is then the convolution

$$\psi(\mathbf{x}_\odot, E) = \int dE_s \int d^3\mathbf{x}_s \mathcal{G}(\mathbf{x}_\odot, E \leftarrow \mathbf{x}_s, E_s) Q(E_s, \mathbf{x}_s), \quad (12)$$

where the Green’s function $\mathcal{G}(\mathbf{x}_\odot, E \leftarrow \mathbf{x}_s, E_s)$ represents the probability for an electron injected at \mathbf{x}_s to reach the Earth with degraded energy $E < E_s$. The spatial integral is performed over the finite extent of the diffusive region. Hence, Green’s functions have to account for boundary conditions. However, the radial boundary at $r_{\text{disc}} = 20$ kpc has been shown to be irrelevant at the Earth location, when $r_{\text{disc}} - r_\odot$ is of the same order, or larger than, L (Delahaye et al. 2010). In this case, the Green’s function can be split into radial and vertical terms as

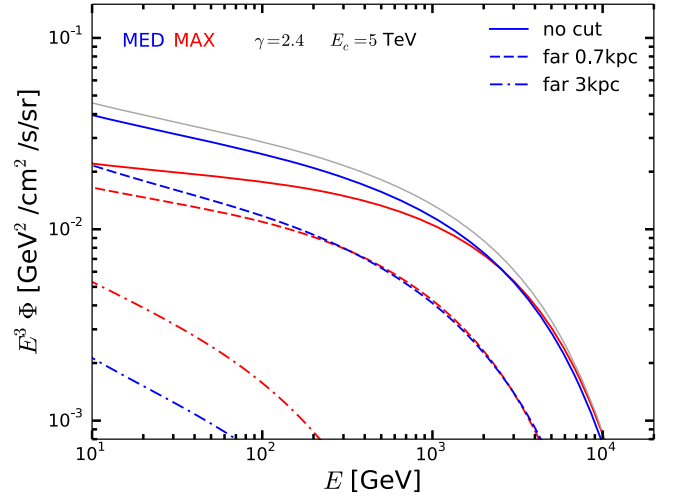


Figure 1. Electron fluxes at Earth, originated from a smooth SNR distribution with different cuts on distance from the Sun R_{cut} , propagation models and SNR spatial distribution models. Blue (red) lines refer to the MED (MAX) propagation model, while different styles show the results when a cut on the distribution of SNRs is applied: the dotted–dashed line shows the results when only far SNRs are considered ($R > R_{\text{cut}} = 3$ kpc), the dashed lines stand for $R > R_{\text{cut}} = 0.7$ kpc and solid lines show the case when the full smooth SNR distribution is taken ($R_{\text{cut}} = 0$). In all cases, the SNR distribution is G15. The solid pale gray line shows the result for L04, without a radial cut and an MED propagation model. For all fluxes, the spectral index is $\gamma_{\text{SNR}} = 2.4$ and $E_{\text{tot,SNR}} = 10^{49}$ erg.

$\mathcal{G} = (\mathcal{G}_r \times \mathcal{G}_z)/b(E)$, where \mathbf{r} is the projection of the electron position in the $z = 0$ plane. In what follows, we will account for vertical boundary conditions only. Depending on the propagation scale, we will use the image method (Baltz & Edsjo 1998) or the Helmholtz eigenfunctions (Lavallo et al. 2007) to expand the vertical Green’s functions \mathcal{G}_z (Delahaye et al. 2010).

Inserting the spatial distribution of SNRs from Equation (9) and the energy spectrum $Q(E)$ of Equation (1) in (12), the solution for the electron flux can be written as

$$\begin{aligned} \Phi(\mathbf{x}_\odot, E) &= \frac{v}{4\pi} \frac{\rho_0 \Gamma_*}{b(E)} \int dE_s Q(E_s) \\ &\times \int dx_s dy_s \mathcal{G}_r(x_\odot, y_\odot, E \leftarrow x_s, y_s, E_s) f(r_s) \\ &\times \int dz_s \mathcal{G}_z(z_\odot, E \leftarrow z_s, E_s) e^{-\frac{|z|}{z_0}}, \end{aligned} \quad (13)$$

where $r_s = \sqrt{x_s^2 + y_s^2}$. As noted above, the Green’s functions are taking into account the vertical boundary only. When the radial cut on the SNR position is applied, we implement it as a hollow cylindrical region around the Earth position in the source distribution, i.e., we set a hole in $\rho(r, z)$ defined by the condition $R \equiv |\mathbf{r} - \mathbf{r}_\odot| = R_{\text{cut}}$. Inside this hole, cataloged sources replace the smooth electron distribution from SNRs (and the resulting fluxes are obtained as discussed in the next subsection).

In Figure 1, we show an example of the electron flux that reaches the Earth, obtained from a smooth distribution of SNRs with an injection spectral index $\gamma_{\text{SNR}} = 2.4$ and $E_{\text{tot,SNR}} = 10^{49}$ erg. The results for both the MED and MAX propagation models are shown, as well as various choices of the cut-off

Table 1
A Summary of the main Hypotheses and of the Free Parameters Used in This Work

Analysis	R_{cut} (kpc)	e^+ priors	$\gamma_{\text{PWNe}}, \eta_{\text{PWNe}}$	$\gamma_{\text{SNR}}, E_{\text{tot,SNR}}$	q	B_{Vela}	γ_{Vela}	B_{near}	$\gamma_{1,2\text{SNR}}, E_b^Q$
1	0	...	✓	✓	✓	n.a.	n.a.	n.a.	n.a.
2	0	✓	✓	✓	✓	n.a.	n.a.	n.a.	n.a.
3a	0.7, 3	✓	✓	✓	✓	✓	...	✓	n.a.
3b	0.7	✓	✓	✓	✓	...	✓	✓	n.a.
4	0	✓	✓	✓	✓	n.a.	n.a.	n.a.	✓

Note. For each analysis (1, 2, 3a, 3b, 4), we show the value for R_{cut} used for the SNR component and a check mark for the different parameters and priors that we use. For example, the priors from the AMS-02 positron spectrum have been used for all analyses except *Analysis-1*. The free parameters are the spectral index (γ_{PWNe}) and the efficiency (η_{PWNe}) for the PWNe, the Spectral Index (γ_{SNR}) and the normalization ($E_{\text{tot,SNR}}$) for the smoothly distributed SNRs, the overall normalization for the secondary component (q), the value of the magnetic field (B_{Vela}) and of the spectral index (γ_{Vela}) for the Vela SNR, the value of the magnetic field for the near SNRs (B_{near}), and the parameters connected to the break in the spectral index for the SNR component ($\gamma_{1,2\text{SNR}}, E_b^Q$). When the parameter is not applicable, we indicate it as n.a.

value R_{cut} . We note that the reason to have a cut-off distance in the smooth distribution of SNRs is to allow us to introduce nearby discrete sources, as discussed in the next subsection. Notice that the MED (blue lines) fluxes are higher than the MAX (red lines) in the no-cut (solid lines) and $R_{\text{cut}} = 0.7$ kpc (dashed) cases, while the situation reverses for $R_{\text{cut}} = 3$ kpc (dotted-dashed). This is because, in the MAX propagation model, the diffusion exponent δ is lower, and the half thickness of the diffusive halo L is greater than in the MED case. For a small cut around the Earth, this means that electrons diffuse more in the Galaxy, losing more energy. In contrast, when the value of R_{cut} becomes comparable to the half thickness of the diffusive halo, electrons have less probability to reach the Earth. In this case, even if the diffusion exponent is higher, the MAX setup with $L \gg R_{\text{cut}}$ allows more electrons to reach us. We note also that the L04 distribution (solid gray) predicts more electrons than the G15 model. This is because the L04 radial distribution predicts more sources in the solar circle.

3.2. Discrete Distribution of Sources from Catalogs

Our model contains discrete sources, whose position and properties are taken from catalogs. Recently, evidence for the existence of local CR sources (< 1 kpc) has been found with the detection of the Iron-60 isotope in CRs (Binns et al. 2016). We use catalogs both to specify the SNRs that are inside a cylinder around the Earth position of radius R_{cut} , for which we use the Green’s catalog (Green 2015), and the PWNe, which we take from pulsars in the ATNF catalog. In the two cases, the injection spectra are those defined in Equation (1) for SNRs and in Equation (3) for PWNe. Including sources from catalogs is especially important in electron and positron fluxes for energy greater than 100 GeV, where local sources dominate (Delahaye et al. 2010; Di Mauro et al. 2014, 2016; Manconi et al. 2017).

We solve the time-dependent diffusion equation in the point-source approximation. In this case, the propagation equation admits the analytical solution:

$$\psi(\mathbf{x}_\odot, E, t) = \frac{b(E_s)}{b(E)} \frac{1}{(\pi\lambda^2)^{\frac{3}{2}}} e^{-\frac{|\mathbf{x}_\odot - \mathbf{x}_s|^2}{\lambda^2}} Q(E_s), \quad (14)$$

where \mathbf{x}_s is the position of the source, and E_s is the injection energy of electrons that cool down to E because of energy losses $b(E)$ in a loss time of

$$\Delta\tau(E, E_s) \equiv \int_E^{E_s} \frac{dE'}{b(E')} = t - t_s, \quad (15)$$

depending on the source age t_s . Therefore, the energy E of an electron detected at Earth for a source with age t_s that emits an electron with energy E_s can be found from Equation (15). The propagation scale λ is defined as usual:

$$\lambda^2 = \lambda^2(E, E_s) \equiv 4 \int_E^{E_s} dE' \frac{K(E')}{b(E')}. \quad (16)$$

4. Analysis and Results

The features of the $e^+ + e^-$ spectrum are known to be dominated by the electron component produced by far SNRs at low energies, while at intermediate and high energies the components arising from local sources (either SNRs or PWNe) become important. Moreover, while nearby SNRs contribute only electrons, PWNe produce equal fluxes of positrons and electrons. Secondary positrons are comparable to PWN positrons below 10 GeV; though, they never become a dominant component in the total $e^+ + e^-$ (except, maybe, at very high energies, beyond the cut-off energy of the source spectrum). For further details on these properties see, e.g., Delahaye et al. (2010), Di Mauro et al. (2014, 2016), and Manconi et al. (2017; where the analyses are performed in the same framework of Galactic transport we are using here), and references quoted therein.

We investigate the role of the far and near SNR sources, the impact of PWNe on the high-energy tail of the *Fermi*-LAT spectrum, and we discuss whether a break in the injection spectrum or in the diffusion coefficient is required. The analysis is performed by fitting the new *Fermi*-LAT spectrum over their full energy range, by considering the whole set of leptonic contributions: primary electrons from SNRs, primary electrons and positrons from PWNe, and secondary electrons and positrons. We use the *Fermi*-LAT $e^+ + e^-$ spectrum as reported in Abdollahi et al. (2017a), and we consider the errors as given by the sum in quadrature of statistical and systematic uncertainties.

Since we are studying the total $e^+ + e^-$ spectrum, it may happen that a good agreement with the data is found for a set of parameters that corresponds to a large positron flux, in excess of what is known from the PAMELA (Adriani et al. 2013) and AMS-02 (Aguilar et al. 2014b) measurements of this observable (and we will show in Section 4.2 that this can indeed occur). In order to prevent this, we “calibrate” our model by performing a fit to the AMS-02 positron-only flux, in order to determine priors on the parameters of the positron

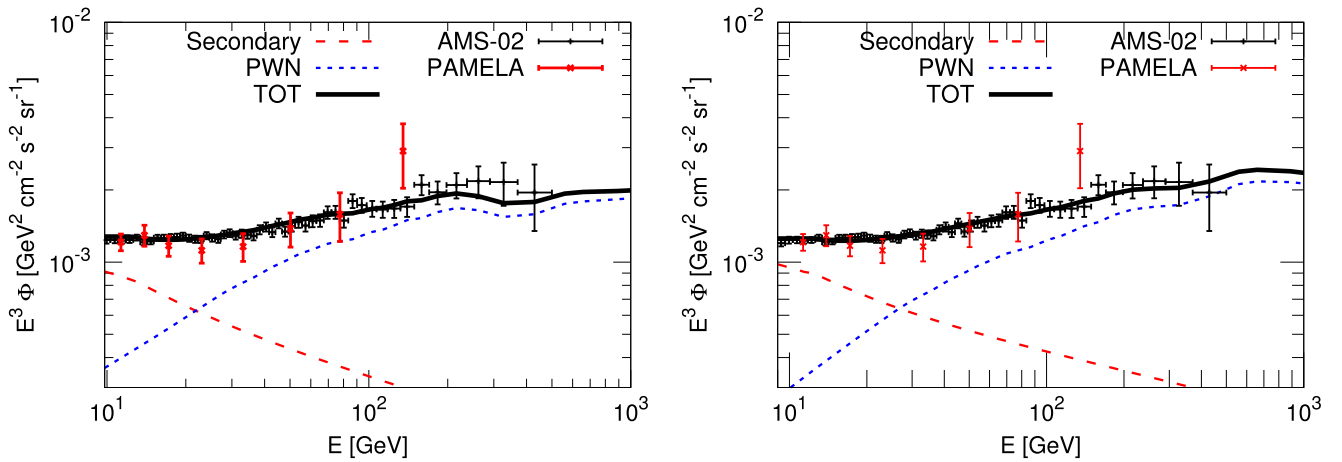


Figure 2. Best fit to the AMS-02 positron flux, for energies greater than 10 GeV, for the MED (left panel) and MAX (right panel) propagation parameters. The black points are the AMS-02 data. The solid black line shows the best-fit model. The dotted blue line and the dashed red line show the PWN and secondary contributions. The red points are the PAMELA data for the same observable.

Table 2

Best-fit Parameters for the AMS-02 Positron Flux (Aguilar et al. 2014b)

	η_{PWN}	γ_{PWN}	q
MED	$0.0456^{+0.0012}_{-0.0011}$	$1.80^{+0.04}_{-0.04}$	$0.96^{+0.06}_{-0.06}$
MAX	$0.074^{+0.004}_{-0.003}$	$1.90^{+0.04}_{-0.04}$	$1.72^{+0.08}_{-0.08}$
Kappl2015	$0.072^{+0.003}_{-0.002}$	$1.91^{+0.04}_{-0.04}$	$1.85^{+0.07}_{-0.08}$
Genolini2015	$0.053^{+0.002}_{-0.002}$	$1.90^{+0.04}_{-0.04}$	$1.49^{+0.06}_{-0.06}$

Note. The first/second/third/fourth row refers to the MED/MAX/Kappl2015/Genolini2015 CR propagation parameters.

Table 3

Priors on the Parameters that Rule Define Positron Emission from PWN and Secondary Production

	η_{PWN}	γ_{PWN}	q
MED	[0.0437, 0.0476]	[1.72, 1.88]	[0.866, 1.063]
MAX	[0.0693, 0.0826]	[1.83, 1.97]	[1.55, 1.84]
Kappl2015	[0.0672, 0.0770]	[1.83, 1.99]	[1.71, 1.99]
Genolini2015	[0.0493, 0.0563]	[1.82, 1.98]	[1.37, 1.61]

emission, that we then use in most of our analyses of the *Fermi*-LAT spectrum.

A summary of the different analyses that we perform with the corresponding free parameters and main hypotheses is presented in Table 1.

4.1. Calibration of Positron Emission with AMS-02 Data

We establish sensible values for the parameters that define the positron emission in our model by analyzing the AMS-02 positron flux (Aguilar et al. 2014b) at energies above 10 GeV. This is the same energy range for which the *Fermi*-LAT measured the $e^+ + e^-$ spectrum, and it is a choice that minimizes the impact of solar modulation on the determination of the model parameters. Notice that in all of our analyses, solar modulation is included (a residual impact is also present at these high energies): we adopt a force-field approximation, and the Fisk potential is treated as a nuisance parameter. In this analysis, the relevant free parameters are the efficiency η_{PWN} of the PWN for emission of positrons (see Equation (5)), the

spectral index γ_{PWN} (see Equation (3)), and a normalization q of the secondary positron emission.

Figure 2 shows the results for the best fit in the case of the MED (left panel) and MAX (right panel) transport parameters. Our model reproduces the AMS-02 positron spectrum, yielding a reduced chi-square $\chi_{\text{red}}^2 = \chi^2/N_{\text{d.o.f}} = 0.51$ for the MED and $\chi_{\text{red}}^2 = 0.61$ for the MAX propagation parameters. The corresponding parameters are reported in Table 2, while Table 3 lists the ensuing priors that we will adopt in the rest of our analyses (they correspond to the 2σ intervals from the AMS-02 fit, and the priors are assumed to be flat in these intervals). We report in Tables 2 and 3, respectively, the best-fit values and priors for secondary and PWN production for Kappl2015 and Genolini2015 propagation models that we will use in the rest of the paper to check how the choice of these more up-to-date propagation parameters affects our results. This allows us to evaluate the implications of the *Fermi*-LAT $e^+ + e^-$ spectrum, while remaining compatible with the AMS-02 (and PAMELA) measured positron flux.

4.2. Smooth Distribution of SNRs in the Galaxy

The first analysis we perform on the Pass 8 *Fermi*-LAT $e^+ + e^-$ spectrum considers a model where SNRs are treated as a smooth population in the whole Galaxy, and for the moment we do not assume the AMS-02 priors of Table 3 for the positron modeling. This is done in order to investigate the direct implications of the *Fermi*-LAT on the modeling of the cosmic leptonic components. For reference, we call this *Analysis-1*. In this case, the parameters that we leave free to vary in the fit are the PWN efficiency η_{PWN} , the PWN index of the spectrum γ_{PWN} , the normalization of the SNR spectrum $E_{\text{tot,SNR}}$ (in units of 10^{48} erg), the SNR index of the spectrum γ_{SNR} , and the normalization factor q of the secondary contribution. For this last quantity and for the SNR spectral index, we assume the following uniform priors: $q = [0.5, 2.0]$ in order to allow some freedom for the calculated secondary positron spectrum and $\gamma_{\text{SNR}} < 2.5$, as expected for typical SNRs.

Results are shown in Figure 3 and Table 4. We obtain good agreement with the data both for the MED and MAX cases, with moderate and quite reasonable PWN efficiencies around 5%. We note that the model positron component is in

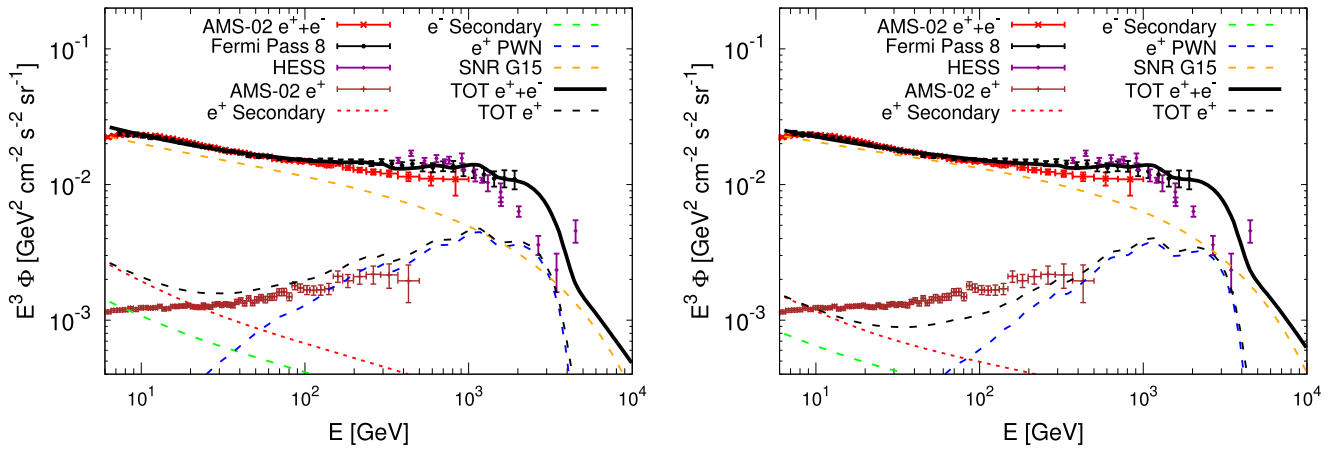


Figure 3. *Analysis-1.* Best fit to the *Fermi*-LAT $e^+ + e^-$ spectrum, obtained for the smooth SNR distribution with $R_{\text{cut}} = 0$ (i.e., no discrete local SNRs). Left (right) panels refer to the MED (MAX) cases. The fit assumes $q = [0.5, 2.0]$ and $\gamma_{\text{SNR}} < 2.5$. The black points are the *Fermi*-LAT $e^+ + e^-$ spectrum. The black solid line shows the best-fit result. This is decomposed into the SNR electron contribution (orange dashed line), secondary electrons (green dashed line) and positrons (red dotted line), and positrons from PWNe (blue double-dot-dashed line). For comparison, the plot also shows the AMS-02 positron flux (brown points), which can be compared with the total positron flux (dashed black line). The red and purple points are, respectively, the AMS-02 and H.E.S.S $e^+ + e^-$ spectrum.

Table 4
Analysis-1

	η_{PWN}	γ_{PWN}	$E_{\text{tot,SNR}}$	γ_{SNR}	q	χ^2_{red}
MED	0.059 ± 0.009	1.45 ± 0.03	$5.67^{+0.3}_{-0.3}$	$2.44^{+0.05}_{-0.04}$	2.0	0.68
MAX	0.049 ± 0.003	1.39 ± 0.02	$12.5^{+0.2}_{-0.3}$	2.50	2.0	0.94

Note. Best-fit parameters for the fit to the *Fermi*-LAT $e^+ + e^-$ spectrum for q constrained to be in the range $[0.5, 2.0]$ and $\gamma_{\text{SNR}} < 2.5$ in the case of MED and MAX propagation models and the G15 SNR distribution. $E_{\text{tot,SNR}}$ is quoted in units of 10^{48} erg. The number of degrees of freedom is 38.

Table 5
Analysis-2

	η_{PWN}	γ_{PWN}	$E_{\text{tot,SNR}}$	γ_{SNR}	q	χ^2_{red}
MED	0.0476	1.72	$5.18^{+0.21}_{-0.20}$	$2.410^{+0.009}_{-0.009}$	1.06	3.0
MAX	0.0826	1.83	$14.0^{+0.6}_{-0.6}$	$2.542^{+0.009}_{-0.009}$	1.84	1.6
Kappl2015	0.0770	1.83	$15.5^{+0.8}_{-0.8}$	$2.560^{+0.010}_{-0.010}$	1.99	1.6
Genolini2015	0.0563	1.82	$10.9^{+0.5}_{-0.5}$	$2.532^{+0.010}_{-0.010}$	1.61	2.8

Note. Best-fit parameters for the fit to the *Fermi*-LAT $e^+ + e^-$ spectrum for the MED, MAX, Kappl2015, and Genolini2015 propagation models and a smooth G15 SNR distribution throughout the Galaxy. $E_{\text{tot,SNR}}$ is quoted in units of 10^{48} erg. The number of degrees of freedom is 38.

agreement with the AMS-02 data, except in the MED case for energies below 30 GeV, a regime where solar modulation also might require a more refined analysis. These solutions, obtained by fitting the *Fermi*-LAT $e^+ + e^-$ spectrum alone without prior information on the positron contribution, are therefore quite satisfactory. However, the normalization q of the secondary production and the SNR spectral index lies mostly at the upper bounds of their priors, suggesting that if we allowed them to freely vary they would have unreasonable values. We have explicitly tried a fit without constraining their ranges, observing that in this case the secondary contribution is driven to be quite large (of the order of 10): this has the consequence of greatly exceeding the AMS-02 measurements on the positron spectrum. For this reason, from here on we consistently adopt throughout all our analyses the AMS-02

priors derived in the previous section. By looking at the best-fit configurations reported in Table 4 (this will also be the case for the results reported in the next sections) one can see that the best-fit values that we obtain for the parameter $E_{\text{tot,SNR}}$ are rather large. In fact, having $E_{\text{tot,SNR}} \approx 10^{49}$ erg implies that a fraction 10^{-2} of the typical kinetic energy that is released in a supernova explosion is converted into e^\pm pairs. This is in tension with typical values that are assumed for this fraction, which are around 10^{-5} – 10^{-4} (see the discussion in Delahaye et al. 2010). While an accurate study on this point would represent an important addition to our investigations, it is also important to point out that $E_{\text{tot,SNR}}$ is inversely proportional to the rate of supernova explosions R . In this work, we are assuming $R = 1$, which is a rather low value if compared to the ones that are often quoted in the literature (as an example in Delahaye et al. 2010 it was assumed $R = 4$). In addition, $E_{\text{tot,SNR}}$ strongly depends on the behavior of the spatial distribution of SNRs, which, as discussed in Delahaye et al. (2010), can exhibit large fluctuations (for example, by around a factor of 2 in the local neighborhood). Lastly, as manifest from Table 5, the best-fit value of $E_{\text{tot,SNR}}$ depends significantly on the Galactic propagation setup that is used. Such dependence could be even stronger if one were to consider propagation models where the assumption of a uniform and isotropic diffusion is relaxed.

The results obtained by enforcing the AMS-02 priors are shown in Figure 4. The best-fit parameters are reported in Table 5. We call this *Analysis-2*. First, we note that the efficiency of PWNe lies at the upper bound of the priors and the PWNe index is close to its lower bound. This is because, for

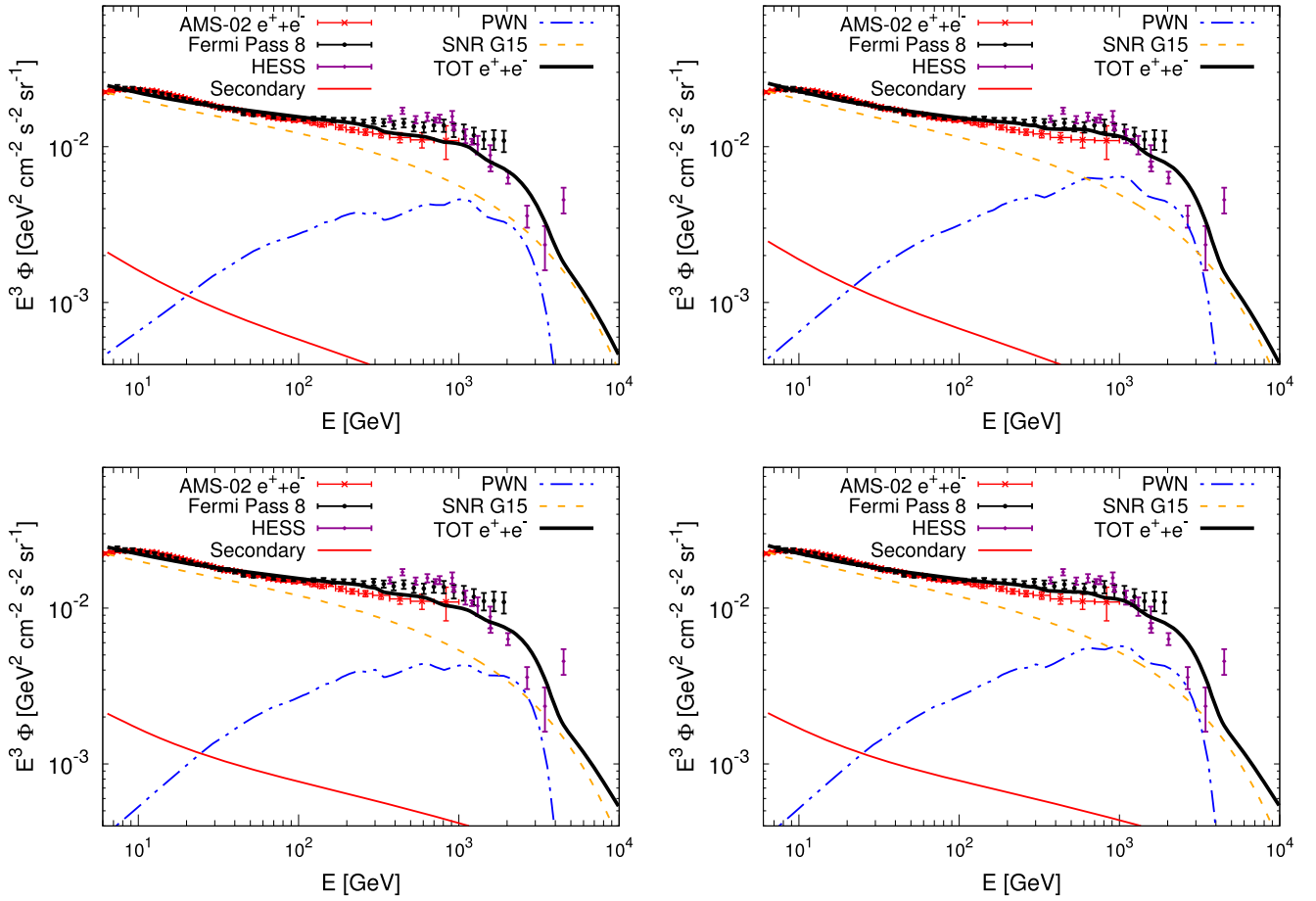


Figure 4. Analysis-2. Best fit to the *Fermi*-LAT $e^+ + e^-$ spectrum, obtained for the smooth SNR distribution with $R_{\text{cut}} = 0$ (i.e., no discrete local SNRs), assuming the priors informed by fitting the AMS-02 positron spectrum for the parameters that drive the positron contribution. The top left (top right) panel refers to the MED (MAX), while the bottom left (right) are for the [Genolini2015](#) ([Kappl2015](#)) transport model, respectively. The $e^+ + e^-$ spectrum points are *Fermi*-LAT (black), AMS-02 (red), and H.E.S.S. (purple). The black line is the best fit to the *Fermi*-LAT spectrum. The orange dashed line shows the SNR electron contribution, the blue double-dot-dashed line stands for the PWN $e^+ + e^-$ and the red solid line shows the secondary positrons.

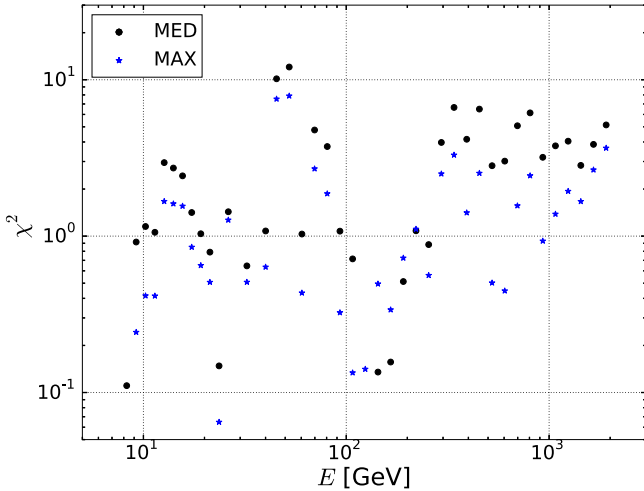


Figure 5. Analysis-2. Contribution to the χ^2 in each *Fermi*-LAT energy bin, for the analyses reported in Figure 4.

energies around a few hundred GeV, this model has a deficit with respect to the measurements; therefore, the fit tends to fill this gap by increasing η_{PWN} and adopting the hardest γ_{PWN} . Moreover, the spectral index of SNRs is 2.41 for MED and

2.54 for MAX, values consistent with the expectations for Fermi acceleration.

χ_{red}^2 is 3.0 for the MED and 1.6 for the MAX model and the energies where the fit does not provide a good representation of data are around 40–90 GeV and for $E > 250$ GeV. This can be seen in Figure 5, where we break down the contributions to χ^2 from the different energy bins. The MAX propagation model is significantly better than the MED model ($\Delta\chi^2 = 54$). However, Figure 5 shows that the MAX model also does not reproduce well the $e^+ + e^-$ in some energy ranges, especially at high energies.

We repeated Analysis-2 using [L04](#) instead of [G15](#) for the SNR distribution (in the MED case) finding very similar results as those reported in Table 5 for [G15](#), except for the $E_{\text{tot,SNR}}$ parameter, which now is $(4.49 \pm 0.19) \times 10^{48}$ erg. Indeed the spatial distribution in [L04](#) does not change the spectral shape of the SNR contribution and only predicts a 15% lower flux because the [L04](#) density of SNRs is slightly greater than the [G15](#) profile at the Earth position. As discussed in the [Appendix](#), this picture does not seem to change if we include a spiral arm pattern in the distribution of SNRs to account for the presence of the Milky Way arms. In fact, when passing from the smooth distributions considered above to a more realistic one, where sources are located along the arms, the electrons emitted by SNRs have to cover a larger distance before reaching Earth. As

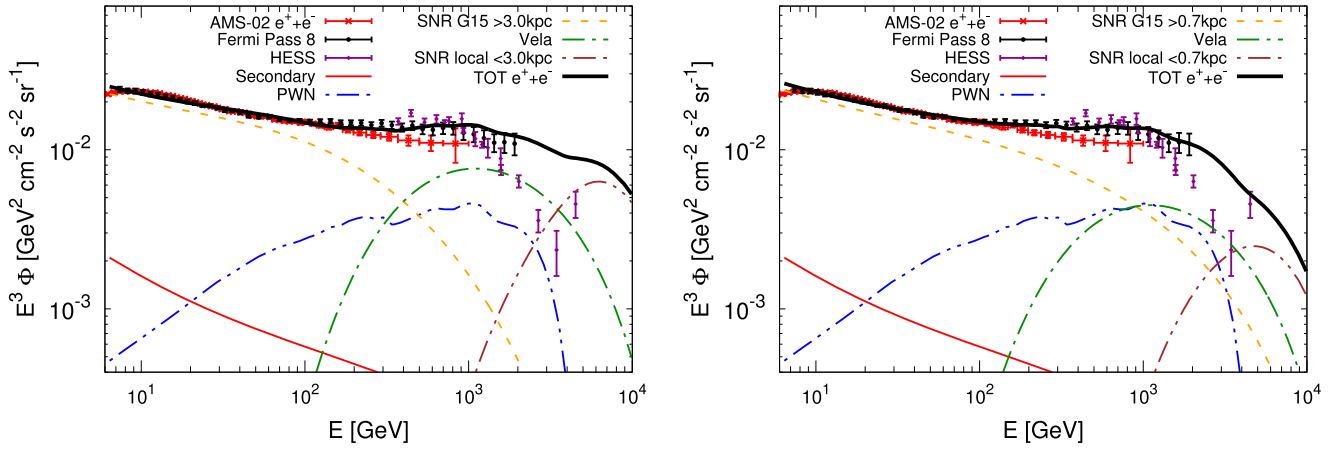


Figure 6. Analysis-3a. Best fit to the *Fermi*-LAT $e^+ + e^-$ spectral measurement, obtained for an SNR distribution composed of a near component ($R \leq R_{\text{cut}}$) and a far ($R > R_{\text{cut}}$) component, the latter being a smooth G15 distribution. The left panel refers to $R_{\text{cut}} = 3$ kpc, and the right panel to $R_{\text{cut}} = 0.7$ kpc. In both cases, the propagation framework is MED. The $e^+ + e^-$ spectral points are *Fermi*-LAT (black), AMS-02 (red), and H.E.S.S. (purple). The black line is the best fit to the *Fermi*-LAT spectral points. The orange dashed line shows the smooth SNR electron contribution, the blue double-dot-dashed line stands for the PWNe $e^+ + e^-$ and the red solid line shows the secondary positrons. The green dotted-dashed line shows the contribution of Vela and the purple double-dotted-dashed line, which emerges at the highest energies is the contribution of the near SNRs from Green’s catalog.

a consequence, their spectrum is softened by energy losses and therefore the tension with the potential hardening at high energies suggested by *Fermi*-LAT data becomes even stronger.

We also tested the alternative propagation models Kapp12015 and Genolini2015. The best-fit parameters that we find with these models are reported in Table 5, while in Figure 4, we show the plot of the flux of the different components compared to *Fermi*-LAT data. The results we obtain with the Kapp12015 model are very similar to the ones we have with MAX model with the same χ^2 and γ_{SNR} and with a slightly greater $E_{\text{tot,SNR}}$. On the other hand, the Genolini2015 propagation setup gives a worse χ^2_{red} of 2.8 with γ_{SNR} similar to the MAX and Kapp12015 cases.

In general, the model with a smooth distribution of SNRs appears inadequate, especially above 50 GeV, where the *Fermi*-LAT data suggest a potential break. This might suggest that the *Fermi*-LAT spectral measurement requires a more detailed investigation of the mid-/high-energy range, where nearby SNRs (including the powerful Vela SNR) might have a role.

4.3. Electrons from Far and Near SNRs

We found in the previous section that a smoothly distributed population of SNRs is not able to provide a good fit to the $e^+ + e^-$ spectrum over the entire energy range measured by *Fermi*-LAT, once constraints on parameter ranges derived from the AMS-02 positron spectrum are taken into account. Therefore, we now allow for more freedom in our treatment of the SNR contribution, by considering far and near SNRs as separate kinds of sources in our fitting procedure. As detailed in Section 2, this is realized by setting the parameter R_{cut} to values different from zero. The properties of the local SNRs are taken from Green (2014). Green’s catalog includes only a few sources able to shape the high-energy flux, with the Vela SNR in a dominant position. The normalization of the injection spectrum $Q_{0,\text{SNR}}$ (see Equation (1)) for the Vela SNR can be related to the synchrotron emission of the electrons propagating

in the magnetic field:

$$Q_{0,\text{Vela}} = \left(\frac{1.2 \cdot 10^{47}}{\text{GeV}} \right) \cdot (0.79)^{\gamma_{\text{Vela}}} \left(\frac{d_{\text{Vela}}}{\text{kpc}} \right)^2 \times \left(\frac{\nu}{\text{GHz}} \right)^{(\gamma_{\text{Vela}}-1)/2} \left(\frac{B_{\text{Vela}}}{100 \mu\text{G}} \right)^{-(\gamma_{\text{Vela}}+1)/2} \left(\frac{B_r^\nu}{\text{Jy}} \right), \quad (17)$$

where d_{Vela} is the distance to Vela, which we assume to be $d_{\text{Vela}} = 0.293^{+0.019}_{-0.017}$ kpc (Dodson et al. 2003), and B_r^ν is the differential intensity measured at radio frequency ν . The spectral index γ_{Vela} can be written in terms of the index of the synchrotron emission $\gamma_{\text{Vela}} = 2\alpha_r + 1$.

Early observations of Vela (Rishbeth 1958) detected three regions of intense radio emission: Vela X, interpreted as the radio source associated with the Vela PWN, Vela Y, and Vela Z, which, because of their steeper radio spectrum than that of Vela X, are assumed to be part of the shell-type SNR.

As shown by Alvarez et al. (2001), the emission from Vela Y and Z has a radio spectral index of $\alpha_r = 0.70 \pm 0.10$ and $\alpha_r = 0.81 \pm 0.16$, respectively, while the radio fluxes at 960 MHz are (588 ± 72) Jy and (547 ± 83) Jy. We consider for the radio flux the sum of the fluxes from Vela Y and Z, $B_r^\nu = (1135 \pm 110)$ Jy, and for the index the average of the spectral indices of Vela Y and Z $\gamma_{\text{Vela}} = 2.50 \pm 0.30$ (since they are very similar). We apply the same Equation (17) to the Cygnus Loop and the other near SNRs. For those sources, we take the parameters from Green’s catalog.

We leave free the normalizations of the fluxes emitted by the two most powerful local SNRs, Vela and the Cygnus Loop. A change in the normalization of the flux can be interpreted as a change in the magnetic field of the remnant: $Q_{0,\text{SNR}} \propto (B/100 \mu\text{G})^{-(\gamma_{\text{SNR}}+1)/2}$, where B is the intensity of the magnetic field. We start by assuming the two magnetic fields to be in the range of $10 < (B_{\text{Vela}}/\mu\text{G}) < 200$ and $20 < (B_{\text{near}}/\mu\text{G}) < 60$ for the magnetic field of Vela and the Cygnus Loop (Katagiri et al. 2011), respectively. For definiteness, we also take the magnetic fields of all the other

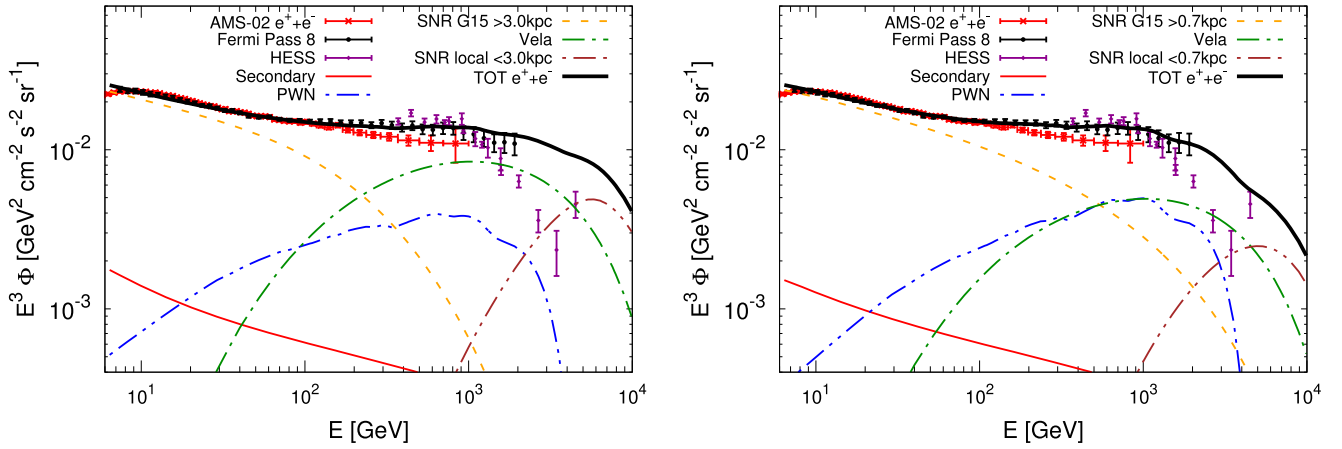


Figure 7. *Analysis-3a*. Same as in Figure 6, for the MAX propagation model.

Table 6
Analysis-3a

	R_{cut} (kpc)	η_{PWN}	γ_{PWN}	$E_{\text{tot,SNR}}$	γ_{SNR}	q	B_{Vela}	B_{near}	χ^2_{red}
MED	3.0	0.0476	1.72	$42.8^{+1.9}_{-1.8}$	$2.144^{+0.019}_{-0.019}$	1.06	$4.7^{+0.2}_{-0.2}$	20	2.0
MED	0.7	0.0476	1.72	$9.4^{+0.7}_{-0.6}$	$2.392^{+0.006}_{-0.005}$	1.06	$6.3^{+0.3}_{-0.3}$	20	0.75
MAX	3.0	0.0826	1.97	$25.0^{+0.3}_{-0.2}$	$2.244^{+0.003}_{-0.002}$	1.84	$4.0^{+0.2}_{-0.2}$	20	0.67
MAX	0.7	0.0693	1.83	$23.6^{+0.3}_{-0.2}$	$2.563^{+0.002}_{-0.002}$	1.55	$5.7^{+0.3}_{-0.3}$	20	0.39

Note. Best-fit parameters for the fit to the *Fermi*-LAT $e^+ + e^-$ spectral measurement for the MED propagation model, when the SNR distribution is separated into a far component ($R > R_{\text{cut}}$) for which the smooth source distribution is G15, and a near component where the contribution from the individual SNRs of Green’s catalog with a distance less than R_{cut} are added. $E_{\text{tot,SNR}}$ is quoted in units of 10^{48} erg, while magnetic field intensities are in μG . The number of degrees of freedom is 38.

local SNRs to be equal to the magnetic field of the Cygnus Loop.

The free parameters in this analysis are η_{PWN} , γ_{PWN} , $E_{\text{tot,SNR}}$, γ_{SNR} , q , B_{Vela} , and B_{near} , while γ_{Vela} is fixed to 2.5 (*Analysis-3a*). The best-fit configurations for two different values of the parameter $R_{\text{cut}} = 0.7$ kpc and 3 kpc are shown in Figure 6 for MED and in Figure 7 for MAX. The best-fit parameters are reported in Table 6. For $R_{\text{cut}} = 0.7$ kpc, the agreement with data is remarkably good, both in the MED and MAX cases. On the other hand, setting R_{cut} to 3 kpc gives a much worse fit in the MED case, while it is still quite good for the MAX case. The situation for the MED propagation setup and $R_{\text{cut}} = 3$ kpc can be seen in the left panel of Figure 6; in this case, the model underpredicts the data around a few hundred GeV. This is probably because Green’s catalog of SNRs, from which we select the local sources, contains only the nearest and brightest objects that contribute to $E > 1$ TeV. The catalog is probably incomplete for those sources that are older and fainter and which should contribute at a few hundred GeV. Setting the radial cut at 0.7 kpc alleviates the tension with the data because all the fainter and older sources are incorporated into the smooth distribution of SNRs and the nearby component is dominated by Vela and the Cygnus Loop SNRs, which we are including explicitly in the model.

We also test values for SNR cut-off energies different from 5 TeV, the benchmark value in our analysis. The values $E_c = [0.6, 1.0, 2.0, 3.0]$ TeV are also used with the MAX and MED propagation parameters with the result that the goodness of fit and the values of the best-fit parameters are consistent with those found for 5 TeV (reported in Table 6) if $E_c > 2$ TeV. On the other hand, for $E_c < 2$ TeV, the fit worsens significantly because the nearby SNRs, mainly Vela

and the Cygnus Loop, do not explain the highest-energy spectral points due to the low energy of the cutoff. In Figure 8, we show the result of a fit as in Figure 7 but with $E_c = 1$ TeV for the MED (right panel) and MAX propagation parameters (left panel). It is evident from these two plots that setting the cut-off energy of the SNR emission at 1 TeV results in a sizeable reduction of the flux from local SNRs such as the Cygnus Loop. This happens because these sources have ages and distances for which the peak of their fluxes is expected to be at higher energies (around 5 TeV), as shown in Figure 7.

In the fits, the magnetic field of the Cygnus Loop takes the lowest value allowed by the prior ($B_{\text{near}} = 20 \mu\text{G}$), while B_{Vela} is found to be in the range of (5–6) μG when $R_{\text{cut}} = 0.7$ kpc. The magnetic field of the Vela SNR is significantly smaller than the value derived in Sushch & Hnatyk (2014). In that paper, based on the modeling of the synchrotron emission from Vela using an advanced hydrodynamical framework, the magnetic field of Vela Y and Z is found to be 46 μG and 30 μG , respectively. In Sushch & Hnatyk (2014), the index of the injection spectrum has been derived to be $\gamma_{\text{Vela}} = 2.47 \pm 0.09$ and the total energy emitted by Vela in the form of electrons to be $E_{\text{tot,Vela}} = (2.4 \pm 0.2) \cdot 10^{47}$ erg. This last quantity is directly related to our modeling of Vela, and in particular to $Q_{0,\text{Vela}}$, by Equation (2). We therefore try a final fit to *Fermi*-LAT spectrum (*Analysis-3b*) by fixing the Vela magnetic field to $B_{\text{Vela}} = 38 \mu\text{G}$, which is the average of the magnetic fields of Vela Y and Vela Z, and vary $Q_{0,\text{Vela}}$ and γ_{Vela} within the 2σ intervals of these parameters as given by Sushch & Hnatyk (2014).

The results of this fit are shown in Figure 9 for the MED (left panel) and MAX (right panel) propagation parameters. The best-fit parameters are in Table 7. The χ^2_{red} values with either

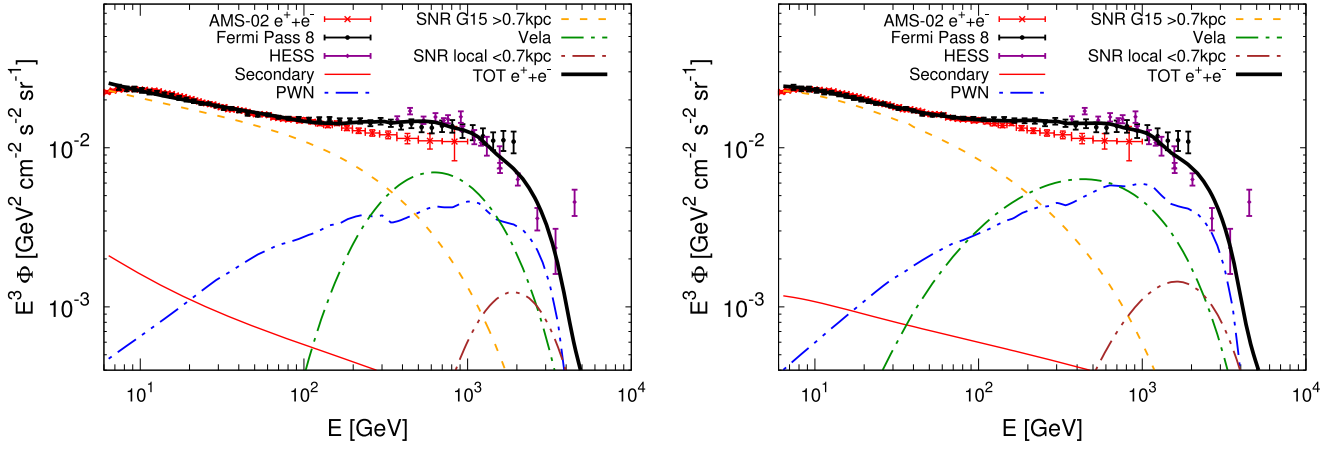


Figure 8. *Analysis-3a.* Same as in Figure 6 for the MAX and MED propagation model with $E_c = 1$ TeV.

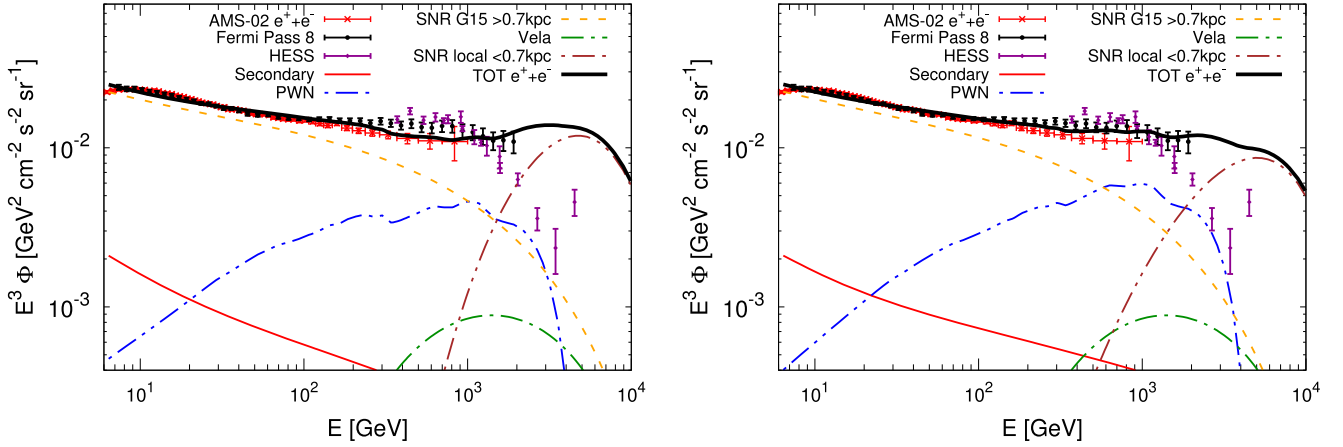


Figure 9. *Analysis-3b.* As in Figures 6 and 7, but for the MED (left panel) and MAX (right panel) propagation parameters and using as priors on Q_0 of Vela and γ_{Vela} the 2σ intervals of the values derived in Sushch & Hnatyk (2014).

MED or MAX propagation parameters are much worse than in the previous case, for which the Vela SNR parameters were free to vary. This is primarily because fixing the parameters B_{Vela} , $E_{\text{tot,Vela}}$, and γ_{Vela} fixed to the values derived in Sushch & Hnatyk (2014) implies an electron flux much smaller than obtained with the Vela SNR parameters specified in Table 6. This value of B_{Vela} makes the spectrum lower by about one order of magnitude, creating a deficit of electrons around a few hundred GeV. Indeed, making the same fit but without considering any prior on $E_{\text{tot,Vela}}$, we find $E_{\text{tot,Vela}} = 32 \cdot 10^{48}$ erg, which is more than an order of magnitude larger than in Sushch & Hnatyk (2014).

5. Interpretations with a Break in the Injection Spectrum or in the Diffusion Coefficient

In the previous sections, we interpreted the *Fermi*-LAT $e^+ + e^-$ spectrum by using different models for the spatial distribution of electron and positron sources. In this section, we study whether the apparent hardening around 50 GeV could be explained by a break in the injection spectrum or in the diffusion coefficient. In this analysis, we will use the G15 smooth SNR distributions for the whole Galaxy, without considering a separate near component ($R_{\text{cut}} = 0$).

In order to account for a break related to the injection of electrons, the SNR spectrum is now modeled as a broken

power law:

$$Q(E) = \begin{cases} Q_{0,\text{SNR}} \left(\frac{E}{E_0} \right)^{-\gamma_{1,\text{SNR}}} & E \leq E_b^Q, \\ Q_{0,\text{SNR}} \left(\frac{E}{E_0} \right)^{-\gamma_{2,\text{SNR}}} \left(\frac{E_b^Q}{E_0} \right)^{\Delta\gamma_{\text{SNR}}} & E > E_b^Q, \end{cases} \quad (18)$$

where $\Delta\gamma_{\text{SNR}} = \gamma_{2,\text{SNR}} - \gamma_{1,\text{SNR}}$. The free parameters of our model are now η_{PWN} , γ_{PWN} , q , $E_{\text{tot,SNR}}$, $\gamma_{1,\text{SNR}}$, $\gamma_{2,\text{SNR}}$, and E_b^Q . The best-fit model for this case (*Analysis-4*) is shown in Figure 10 and the corresponding parameters are listed in Table 8. We find that this option reproduces the spectral measurement very well, making the possibility of a broken power law for the injection spectrum of SNRs viable. For both the MED, MAX, Kappl2015, and Genolini2015 models, the implications are that the break in the injection spectrum would occur at an energy of $E_b^Q = 100$ GeV, larger than the effective energy of the break in the $e^+ + e^-$ spectrum. This difference between the position of the break at injection and at the Earth can be due to the propagation history. Electrons diffuse and cool radiatively from the sources to the Earth. The change in the spectral index is $\Delta\gamma_{\text{SNR}} = -0.42 \pm 0.02$. This spectral hardening could be due to the physics of the SNR shocks

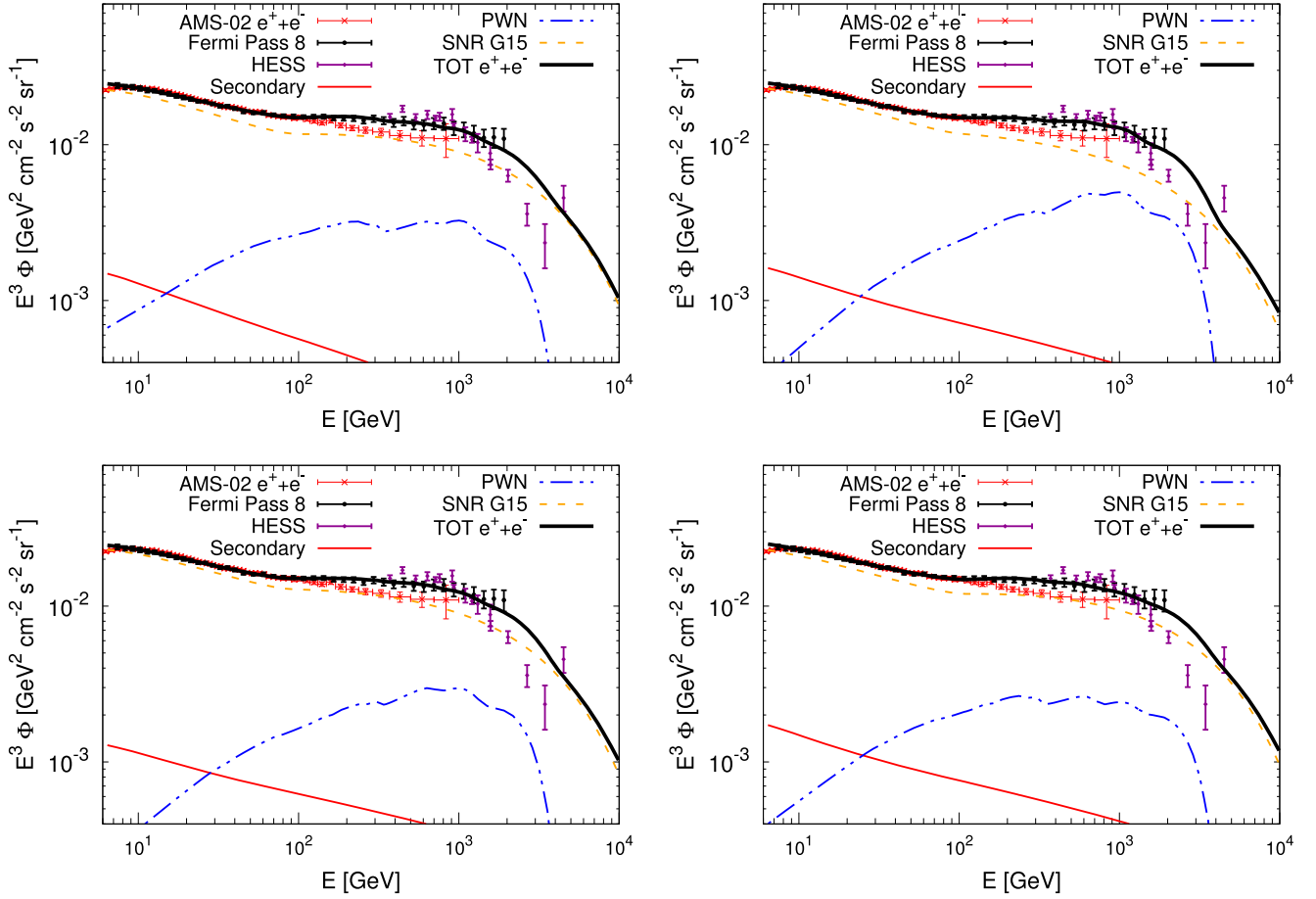


Figure 10. Analysis-4. Best-fit to the *Fermi*-LAT $e^+ + e^-$ spectral measurement, obtained from a SNR smooth population with a break in the injection spectrum, using the MED (top left panel), the MAX (top right panel), [Kappl2015](#) (bottom left panel), and [Genolini2015](#) propagation model (bottom right panel).

Table 7
Analysis-3b

	η_{PWN}	γ_{PWN}	$E_{\text{tot,SNR}}$	γ_{SNR}	q	γ_{Vela}	B_{near}	χ^2_{red}
MED	0.0476	1.72	$8.26^{+0.45}_{-0.40}$	$2.358^{+0.009}_{-0.008}$	1.06	2.29	43 ± 3	2.6
MAX	0.0830	1.83	$14.7^{+0.8}_{-0.7}$	$2.462^{+0.011}_{-0.010}$	1.84	2.29	53 ± 4	1.52

Note. Best-fit parameters for the fit to *Fermi*-LAT $e^+ + e^-$ spectral measurement in the case of MED (top panel) or MAX (bottom) propagation model with SNRs divided into a smooth component for objects with $R > 0.7$ kpc and near sources taken from Green's catalog. $E_{\text{tot,SNR}}$ is quoted in units of 10^{48} erg and the magnetic field B_{near} in μG . The number of degrees of freedom is 38.

Table 8
Analysis-4

	η_{PWN}	γ_{PWN}	$E_{\text{tot,SNR}}$	$\gamma_{1,\text{SNR}}$	$\gamma_{2,\text{SNR}}$	E_b^Q	q	χ^2_{red}
MED	0.0476	1.72	$12.5^{+0.9}_{-0.8}$	$2.608^{+0.011}_{-0.010}$	$2.185^{+0.018}_{-0.016}$	100^{+15}_{-15}	1.063	0.28
MAX	0.0693	1.83	$26.6^{+0.4}_{-0.4}$	$2.673^{+0.008}_{-0.007}$	$2.378^{+0.017}_{-0.016}$	100^{+15}_{-15}	1.84	0.24
Kappl2015	0.0672	1.91	$37.1^{+0.5}_{-0.5}$	$2.744^{+0.011}_{-0.010}$	$2.410^{+0.019}_{-0.018}$	95^{+15}_{-15}	1.99	0.25
Genolini2015	0.0493	1.97	$27.2^{+0.2}_{-0.2}$	$2.665^{+0.008}_{-0.007}$	$2.410^{+0.022}_{-0.022}$	105^{+15}_{-15}	1.61	0.28

Note. Best fit to the *Fermi*-LAT $e^+ + e^-$ spectral measurement, obtained for best-fit parameters in the case of the MED (top) and MAX (bottom) propagation model, obtained with SNRs with a break in the injection spectrum $E_{\text{tot,SNR}}$ is quoted in units of 10^{48} erg. The number of degrees of freedom is 38.

(Caprioli et al. 2011) or to an emerging SNR population with a harder injection index.

A change in the spectral shape of electron and positron fluxes could also be due to a spectral break in the diffusion

coefficient $K(E)$. Such an effect has been proposed to account for the hardening in the CR proton and helium fluxes at high rigidities (Evoli et al. 2012), and might originate from a change in the turbulence power spectrum of the ISM. To investigate

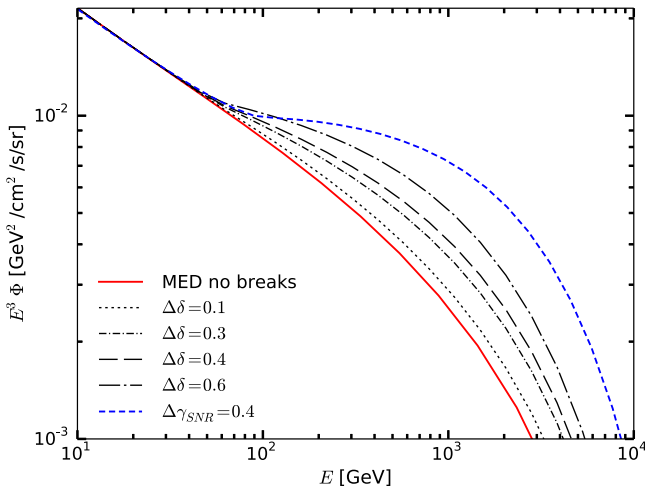


Figure 11. Electron flux from the G15 smooth population distribution for SNRs with a break in the diffusion coefficient at $E_b^K = 60$ GeV (black lines) compared with the standard case with no breaks (red lines), and with the case of a break in the injection spectrum at $E_b^O = 100$ GeV (blue line). Propagation is computed using the MED parameters.

the implications of a change of this kind in $K(E)$, we insert a break in the diffusion coefficient:

$$K(E) = \begin{cases} K_0(E)^{-\delta_1} & E \leq E_b^K, \\ K_0(E)^{-\delta_2}(E_b^K)^{-\Delta\delta} & E > E_b^K, \end{cases} \quad (19)$$

The diffusion coefficient below the break energy is taken as in the standard case, i.e., K_0 and δ_1 are those that refer either to the MED or the MAX case. The break acts above E_b^K , where the spectral index changes by an amount of $\Delta\delta = \delta_1 - \delta_2$. To investigate whether a spectral break in the diffusion coefficient could produce an effect similar to the one induced by break in the injection spectrum, we compute the electron flux for a smooth SNR distribution by varying $\Delta\delta$ in the interval 0.1–0.6 and compare it to the case where the injection spectrum of SNRs is a broken power law in Equation (18), with the standard $K(E)$ of Equation (8). We place the break E_b^K at 60 GeV, in order to have a shape electron spectrum similar to the case for which we use a break in the injection spectrum. The result is shown in Figure 11. We note that similar shifts in the diffusion coefficient or in the injection spectrum power laws $\Delta\delta \sim \Delta\gamma_{\text{SNR}}$ give electron fluxes described by different broken power laws. This is different from what one would expect for protons for instance, for which the flux is approximately $\Phi_p \propto Q(E)/K(E)$. In particular, the break required to fit the *Fermi*-LAT $e^+ + e^-$ spectrum ($\Delta\gamma_{\text{SNR}} = 0.4$, see Table 8), cannot be due to a break in the diffusion coefficient, even with a very unlikely value for $\Delta\delta$. For example, the $\Delta\delta = 0.6$ case would imply a very unlikely diffusion index $\delta_2 = 0.1$ above the break energy. Nevertheless, the case with $\Delta\delta = 0.6$ does not modify the electron flux sufficiently to obtain the hardening of the spectrum due to $\Delta\gamma_{\text{SNR}} = 0.4$.

We therefore conclude that a break at $E_b^O = 100$ GeV in the injection spectrum of a smooth Galactic SNR population can reproduce the potential break suggested by the *Fermi*-LAT $e^+ + e^-$ spectrum. On the other hand, a break in the diffusion coefficient is unable to reproduce the spectrum, even if the

diffusion coefficient above the break is as hard as $K(E) \propto E^{-\delta_2} \sim E^{-0.1}$. We remark, however, that this result holds within the assumptions of our model, in which the diffusion coefficient is spatially independent. We cannot exclude a priori that a spatially inhomogeneous and/or anisotropic diffusion coefficient could induce a break in the observed spectrum for a single-power-law injection spectrum.

6. Conclusions

The *Fermi*-LAT Collaboration has recently reported a new measurement of the inclusive $e^+ + e^-$ spectrum in the energy range between 7 GeV and 2 TeV, obtained with almost seven years of Pass 8 data (Abdollahi et al. 2017a). In this paper, we have explored several theoretical interpretations of this spectral measurement in terms of known sources: electrons and positrons emitted by primary sources, such as SNRs and PWNe, or produced as a secondary CR component, due to the collision of protons and helium nuclei with the ISM. The propagation of the leptons in the Galaxy has been modeled, including their large energy losses, by adopting the semi-analytical model discussed in detail in Delahaye et al. (2010) and Di Mauro et al. (2014).

We summarize our main results as follows.

1. The *Fermi*-LAT $e^+ + e^-$ spectrum is compatible with the sum of leptonic components arising from electrons produced by a smooth SNR population (distributed as in G15), electrons and positrons coming from the PWNe in the ATNF catalog L04, and a secondary component. However, the PWNe emission turns out to slightly exceed the AMS-02 absolute positron flux.
2. When a prior on the positrons measured by AMS-02 is adopted, the higher-energy portion of the $e^+ + e^-$ spectrum does not reproduce the *Fermi*-LAT spectrum. This is the part of the spectrum where local sources (both for electrons and positrons) have the largest impact.
3. When SNRs are separated into a far component (smoothly distributed as in G15) and a near component (SNR distance less than 0.7 kpc), where the near component is populated by the SNRs present in Green’s catalog, the agreement with the *Fermi*-LAT spectrum is significantly improved, including the high-energy tail. The improvement is especially visible in the case of a large confinement volume for CRs (the MAX model). However, once the electron emission from the brightest local SNRs, the Vela, and the Cygnus Loop SNRs, is constrained from radio observations, the quality of the fit worsens.
4. All these results have been obtained without invoking breaks in the spectral features of sources. A smooth distribution of SNRs with a break in the injection spectrum at $E_b^O = 100 \pm 15$ GeV is the case that best reproduces the *Fermi*-LAT spectrum.
5. A spectral break in the diffusion coefficient is unable to reproduce the measured $e^+ + e^-$ spectrum.

In conclusion, the *Fermi*-LAT $e^+ + e^-$ spectrum can be reproduced either by local SNRs, as those present in Green’s catalog and closer than about 1 kpc, or by a smooth distribution of sources endowed with a spectral break in the injection spectrum at about 100 GeV (at injection). In general, we find that the MAX propagation model performs better in

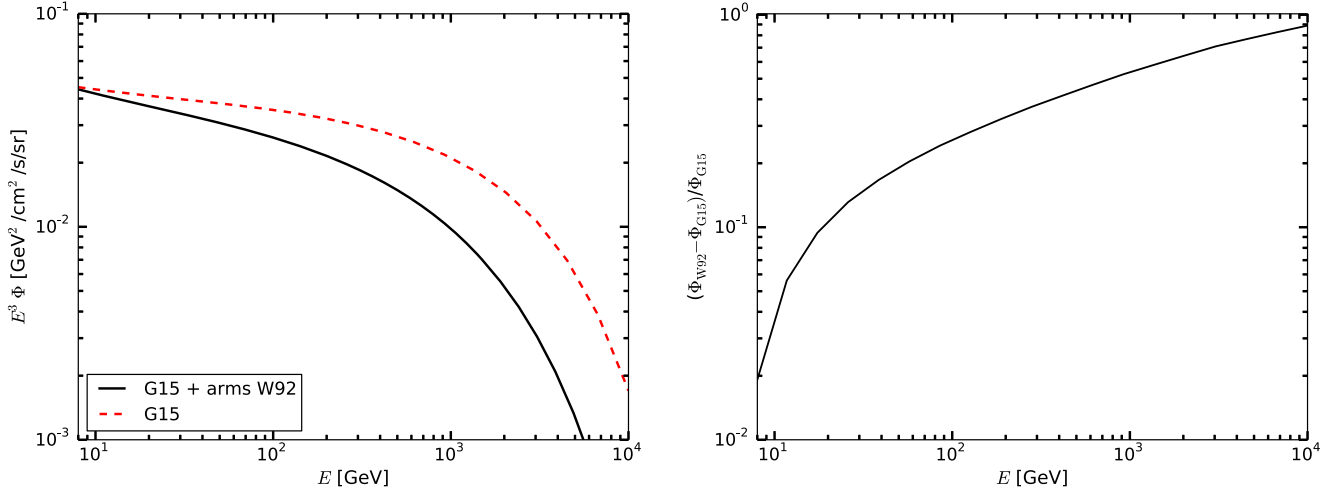


Figure 12. Effect of including a spiral pattern in the SNR source distribution on the propagated electron flux. The fluxes are computed for the MAX propagation setup and using $\gamma_{\text{SNR}} = 2.4$. Left panel: electron fluxes for the **G15** SNR distribution (red dashed line) and for the same distribution with the spiral pattern implemented according to the Wainscoat et al. (1992) model, as described in the text (black solid line). Right panel: relative difference $(\Phi_{\text{W92}} - \Phi_{\text{G15}})/\Phi_{\text{G15}}$ as a function of energy.

reproducing the *Fermi*-LAT spectral measurement under all circumstances.

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Appendix Impact of Adopting an SNR Distribution with a Spiral Structure

The distributions of SNRs that are adopted everywhere in this paper (L04 and G15, see Section 3.1) are azimuthally symmetric and therefore do not contain the spiral structure of the Milky Way. The impact of the presence of spiral arms on the CRs fluxes at the Earth has recently been discussed by many authors (see, e.g., Effenberger et al. 2012; Gaggero et al.

2013; Benyamin et al. 2014; Werner et al. 2015; Johannesson et al. 2016; Kissmann 2017) by means of a fully three-dimensional description of the SNRs distribution function. In order to include the spiral arms’ presence in our semi-analytical technique, we model the distribution function as follows:

$$\rho(r, \phi, z) = \rho_0 f(r) e^{-\frac{|z|}{z_0}} \cdot S(r, \phi) \quad (20)$$

where ρ_0 , $f(r)$, and $e^{-\frac{|z|}{z_0}}$ are discussed in Section 3.1, while the function $S(r, \phi)$ describes the spiral pattern. Specifically, we adopt the four-arm structure described in Wainscoat et al. (1992), with the parameters provided by Faucher-Giguere & Kaspi (2006). We compute the electron flux at Earth by solving a more general version of Equation (13), where any assumption on cylindrical symmetry is relaxed:

$$\begin{aligned} \Phi(\mathbf{x}_\odot, E) &= \frac{v}{4\pi} \frac{\rho_0 \Gamma_*}{b(E)} \int dE_s Q(E_s) \\ &\times \int d\delta_s d\phi_s \mathcal{G}(r_\odot, \phi_\odot, E \leftarrow r_s, \phi_s, E_s) f(r_s) S(r_s, \phi_s) \\ &\times \int dz_s \mathcal{G}_z(z_\odot, E \leftarrow z_s, E_s) e^{-\frac{|z_s|}{z_0}}, \end{aligned} \quad (21)$$

where the expressions for the Green functions $\mathcal{G}(r_\odot, \phi_\odot, E \leftarrow r_s, \phi_s, E_s)$ and $\mathcal{G}_z(z_\odot, E \leftarrow z_s, E_s)$ are the same as for the case without spirals, i.e., the ones derived in Delahaye et al. (2010).

Our results are presented in Figure 12 for the MAX propagation models (we have checked that no significant difference in the spectral features appears if other propagation models are considered). In the left panel, the flux for the **G15** distribution with and without the spiral pattern suggested by the model Wainscoat et al. (1992) are shown for the same spectral index $\gamma_{\text{SNR}} = 2.4$. The two curves are scaled to have the same normalisation at 10 GeV. We find that including the Galaxy spiral arms in our model produces a softening in the electron spectrum, in agreement with Gaggero et al. (2013) and Di Bernardo et al. (2013). The softening is more pronounced at higher energies, as illustrated by the relative difference between the case with and without the spiral pattern in Figure 12 (right panel). This is due to the fact that the Earth sits in an inter-arm

region and high-energy electrons lose more energy before they can reach it from the nearest arm, where the SNR source distribution is peaked.

From these results, we conclude that, given the importance of the softening at higher energies, the presence of the break in the $e^+ + e^-$ flux would be even more significant including the spiral pattern of the SNR source distribution.

As a final remark, we emphasize that here we have implemented the spiral pattern only for the source distribution and not for the energy losses or for the spatial diffusion coefficient. Modeling effects of this kind, albeit necessary to fully ascertain the impact of the presence of the spiral arms on our results, would require a fully numerical treatment of electron propagation and is therefore beyond the scope of the simple analytical model discussed in this work.

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