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Use of the canonical discriminant analysis to select SNP markers for bovine breed assignment and traceability purposes

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1 **Running head:** Bovine breed assignment and traceability

2

3 **Use of the canonical discriminant analysis to select SNP markers for bovine breed assignment**
4 **and traceability purposes**

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15   **Summary**

16   Several market researches have shown that consumers are primarily concerned with the provenance
17   of the food they eat. Among the available identification methods, only DNA-based techniques
18   appear able to completely prevent from frauds. In this paper, a new method to discriminate among
19   different bovine breeds and assign new individuals to groups was developed. Bulls of three cattle
20   breeds farmed in Italy, Holstein, Brown and Simmental, were genotyped by using the 50K SNP
21   Illumina BeadChip. The multivariate canonical discriminant analysis was used to discriminate
22   among breeds whereas, the discriminant analysis was used to assign new observations. The method
23   was able to completely identify the three groups already at chromosome level. Moreover, a genome
24   wide analysis developed by using 340 linearly independent SNPs yielded a significant separation
25   among groups. Using the reduced set of markers, the discriminant analysis was able to assign 30
26   independent individuals to the proper breed. Finally, a set of 48 high discriminant SNPs was
27   selected and used to develop a new run of the analysis. Again, the procedure was able to
28   significantly identify the three breeds and to correctly assign new observations. These results
29   suggest that an assay with the selected 48 SNP could be used to routinely track mono breed
30   products.

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32   **Keywords:** allocation method, bovine breeds, livestock products.

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36

37   **Introduction**

38

39   The relevant concern of consumers about food quality has resulted in an increased importance of
40   products traceability in agriculture. Among the available identification methods, only DNA-based
41   techniques appear able to completely prevent from frauds. Microsatellite (Casellas *et al.* 2004; Orrù
42   *et al.* 2006; Dalvit *et al.* 2008) and AFLP markers (De Marchi *et al.* 2006; Negrini *et al.* 2007) have
43   been traditionally used for animal identification or parentage determination. More recently, a
44   different category of markers, the single nucleotide polymorphisms (SNP), have been proposed to
45   identify animals, breeds and their products. Compared to microsatellites, SNPs offer the advantage
46   they have lower rates of genotyping errors (Weller *et al.* 2006), are very abundant over the genome
47   (Heaton *et al.* 2005) and their analysis can be largely automatized.

48   At present, however, few studies have investigated the possible exploitation of SNPs for traceability
49   purposes. Orrù *et al.* (2009) tested 18 SNPs for their ability to identify individuals in six European
50   cattle breeds obtaining a probability to find two identical animals equal to 0.0765 out of one million
51   samples. Negrini *et al.* (2008) used a panel of 90 specifically selected SNPs to trace four European
52   protected indication beef products. Authors found a percentage of correct assignment ranging from
53   80% to 100%. Recently, Ramos *et al.* (2011) obtained 99% of correct assignment among five pig
54   breeds by using a SNP assay containing 193 breed specific markers.

55   All the above mentioned methods use a pool of pre-selected SNPs and suitable statistical techniques
56   to correctly assign individuals or animal derived foodstuffs. Essentially, two evaluation approaches
57   are used. The first is the deterministic and consists in finding SNPs with different allelic variants
58   fixed in the compared breeds (Paetkau *et al.* 1995). The second is the probabilistic and relies on
59   markers with typical allelic frequencies in different breeds. Statistical procedures as maximum
60   likelihood functions or Bayesian methods (Rannala & Mountain 1997) are therefore applied to

61 assign new observations to breeds. Several software packages are freely available to develop such
62 analyses (Manel *et al.* 2005).

63 In this paper two multivariate statistical techniques were exploited to assess differences among
64 three bovine breeds and to assign independent individuals to the proper group by using genomic
65 data. The first objective was reached by using the canonical discriminant analysis (CDA) which
66 extracts a set of linear combinations of the original variables able to maximize differences among
67 predefined groups. The second was obtained by using the discriminant analysis (DA) which
68 elaborates a discriminant function able to assign new observations to groups. Both techniques do
69 not start from preselected variables, i.e. breed-specific SNPs. CDA and DA, analyze the correlation
70 structure of SNPs in order to assess the difference among groups and assign new individuals. So,
71 and this is one of the most important output of the CDA, a restricted pool of markers able to
72 discriminate breeds is obtained at the end of the procedure.

73 Aims of the present work were a) to develop an efficient automated method for breed assignment
74 and traceability purposes by using CDA and DA, b) to obtain a restricted pool of discriminant
75 markers that could be used in traceability protocols.

76

77 **Materials and methods**

78 The data

79 Data consisted of 1,042 Holstein, 750 Brown Swiss and 480 Simmental bulls genotyped by using
80 the Illumina 50K BeadChip (Matukumalli *et al.* 2009). Only markers located on the 29 autosomes
81 were considered. SNP monomorphic, not in Hardy-Weinberg equilibrium, and with minor allele
82 frequency lower than 5% were removed. This selective editing procedure obviously leads to discard
83 SNPs fixed or typical for a specific breed, On the other hand, the aim of the present work is to use a

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84 multivariate technique to detect a pool of highly discriminant markers based on their correlation
85 structure and not, for example, on the occurrence of rare alleles. Finally, markers with more than
86 2.5% missing values were excluded. After data editing, the retained SNP were 38,450 for Holstein,
87 37,254 for Brown and 40,179 for Simmental, with 30,055 markers in common. The final matrix of
88 data, however, still contained missing values. In this case, CDA and DA delete the corresponding
89 rows, thus obtaining a very small data set. For this reason, missing data were imputed according to
90 the most frequent genotype at each locus. Genotypes were finally coded as the number of copies of
91 one SNP allele it carries, i.e. 0 (homozygous for allele A), 1 (heterozygous) or 2 (homozygous for
92 allele B). Ten samples of 30 randomly selected bulls (10 for each breed) were generated and used as
93 independent observations in the cross-validation procedure.

94

95 The Canonical discriminant analysis

96 The general objective of CDA is to distinguish among different populations by using a particular set
97 of variables (Mardia *et al.* 2000). Unlike cluster analysis, in CDA the group to which each
98 individual belongs is known. In this study CDA was applied to discriminate animals of three cattle
99 breeds by using around 30K markers. Given the classification criterion (the breed), CDA derives a
100 new set of variables, the canonical functions (CAN), which are linear combination of the original
101 markers. The coefficients of the linear combination are the canonical coefficients (CC) which
102 indicate the partial contribution of each original variable. When k -groups and m -variables are
103 involved in the analysis, the maximum number of possible canonical functions is $p = \min(m; k-1)$.
104 Being, in general, $m > k$, $k-1$ functions are derived. In the present work, being $k-1=2$, two canonical
105 functions (CAN1 and CAN2) were derived.

106 The statistical significance in group separation can be expressed by means of the Mahalanobis'
107 distance and the corresponding Hotelling's T-square test (De Maesschalck *et al.*, 2000). Groups are
108 declared significantly separated if the Hotelling's test shows a p-value less than 0.05. This test can
109 be developed only if the pooled (co)variance matrix of data is not singular. However, the visual
110 inspection of the CAN1 vs. CAN2 scatter-plot and the values of distances among groups can be
111 useful to assess if groups are separated. CDA and the related tests were developed by using the
112 CANDISC procedure implemented in the SAS-STAT software (SAS Institute Inc., Cary, NC,
113 USA). After differences among groups were assessed, the proc DISCRIM of SAS was used to
114 develop the DA. In this case, the canonical functions, applied to each animal, produced the
115 discriminant score: an individual is assigned to a particular group if its discriminant score is lower
116 than the cutoff-value obtained by calculating the weighted mean distance among group-centroids
117 (Mardia *et al.* 2000).

118

119 The CDA method for breed assignment

120 The matrix of data consisted of more than $m = 30K$ SNP-variables and $n = 2K$ animals. In this
121 condition, multivariate techniques became meaningless, being the rank of the extracted (co)variance
122 matrix $\leq n-1$ (Dimauro *et al.* 2011). To overcome at least partially this problem, in genomic data
123 mining statistical analyses are often developed by chromosome (Macciotta *et al.* 2010). In the
124 present research, CDA was at first performed separately by each autosome. As a consequence, 29
125 CAN1 vs. CAN2 scatter-plots and 29 distance matrices were obtained. However, being the 29
126 pooled (co)variance matrices singular ($m > n$ in all chromosomes), the Mahalanobis' distance and the
127 related statistical test cannot be evaluated. Therefore, to obtain a pool of linearly independent
128 markers, canonical functions extracted for each chromosome were first ranked according to the CC
129 values. Then SNPs whose CC exceed an arbitrary fixed threshold were retained. So the final pool of

130 selected SNPs, besides linearly independent, were also the most discriminant. This markers were
131 used to develop a genome wide CDA (GW-CDA) where both the Mahalanobis' distance and the
132 Hotelling's test could be evaluated. Furthermore, the minimum subset of SNPs able to discriminate
133 the three groups was also detected by using the same procedure applied to select the linearly
134 independent SNPs.

135 To test the ability of the selected SNPs in assigning new animals to the proper breed, the DA was
136 applied to the 10 cross-validation datasets previously generated. Moreover, the assignment test was
137 also performed by using three independent algorithms included in the GeneClass2 software (Piry *et*
138 *al.* 2004): the frequency-based method of Paetkau *et al.* (1995), the Bayesian-based methods of
139 Rannala & Mountain (1997) and Baudouin & Lebrun (2000).

140

141 **Results and discussion**

142 CDA by chromosome

143 All CAN1 vs. CAN2 scatter plots displayed a clear separation among groups already at
144 chromosome level, as shown in Figure1, where plots for BTAs 1 and 28 are reported. These
145 chromosomes were chosen because they had the greater (BTA1) and the lower (BTA28) number of
146 SNPs, respectively. Distances among breeds were different in the two chromosomes (figure 1). For
147 example, the Euclidean distance between Holstein and the other two breeds on BAT28 was equal to
148 0.15 the corresponding distance on BTA1. The mean correlation value between distances among
149 breeds and number of markers in each chromosome was around 0.75. This result clearly indicates
150 that the multivariate description of a breed obtained by using genomic data produces, as expected, a
151 greater separation among groups as the number available information (the markers) increases.

152 Distances between Brown and Simmental were lower than those for Holstein vs. Brown and
153 Holstein vs. Simmental for all chromosomes. Similar results were obtained by Del Bo *et al.* (2001)
154 who studied the genetic distances among 13 cattle breeds. Authors found a double distance among
155 Holstein and the other two groups involved in the present study. A clear separation was also
156 reported between Brown and Simmental.

157

158 Genome-wide CDA

159 In each chromosome, the threshold for the absolute value of CCs in CAN1 and CAN2 was
160 arbitrarily fixed at 0.85 and 0.45 respectively. Different values were adopted for the two canonical
161 functions because CC values in CAN1 were higher than in CAN2. A total of 1,836 SNPs were
162 obtained and used to develop a GW-CDA. The resulting CAN1 vs. CAN2 scatter plot showed a
163 clear separation of the three breeds (Figure 2) and, as in the by chromosome CDA, Holstein breed
164 was markedly separated from the other two groups. The increase of distances between breeds for
165 larger numbers of markers suggests that CDA is able to discriminate groups even if they are not
166 markedly differentiated. It is worth remembering that the editing performed in this study has
167 discarded rare alleles. Moreover, the selected SNPs used to develop the GW-DA gave 100% correct
168 assignment of the new 30 observations in the 10 cross-validation datasets. This results clearly
169 confirmed the goodness of the method in discriminating the three bovine breeds.

170 As at chromosome level, however, the $\mathbf{S}$ matrix of the 1,836 SNPs was singular. So, the number of
171 markers was further reduced till to 340 linearly independent SNP-variables. The 340 SNP were then
172 used to develop a new run of the GW-CDA. As in the previous cases, distances among breeds
173 (table 1) showed a pattern like in CDA applied by chromosome. The Hotelling's test gave a highly

174 significant separation among breeds and GW-DA correctly assigned the animals in the cross-
175 validation datasets.

176 Finally, the selected 340 SNP-variables were reduced by deleting markers with lower CCs till to
177 reach the minimum number of markers able to highlight the existence of the groups. At the end, 48
178 of the most discriminant SNPs were retained and used in a new GW-CDA. A significant separation
179 among breeds was still obtained and the GW-DA was able to 100% assign animals in the 10 cross-
180 validation datasets. The same results were obtained with the GeneClass2 software, by using the
181 selected 48 SNPs. All animals were correctly assigned to the proper breed thus confirming the
182 ability of CDA in selecting markers able to discriminate the involved breeds.

183 As before, the CAN1 vs. CAN2 scatter plot (Figure 3) showed three well defined clusters with
184 Holstein clearly differentiated from the other two breeds. Markers and related CCs for each
185 canonical function are reported in table 2. Interesting considerations can be drawn by observing
186 Figure 3 and table 2. CAN1, which accounted for 92% of the total variability, shows very high CC
187 absolute values, ranging from 0,921 to 0,944. This result indicates that the associated markers
188 heavily affect the separation of Holstein from the other breeds. In figure 4a are displayed the
189 genotypic frequencies for SNP having the negative CC. It can be clearly noticed that the
190 predominant homozygous genotype in Holstein is the opposite of the other breeds. For example, BB
191 is the most frequent genotype in Holstein whereas in Simmental and Brown is the most rare. A
192 reversed pattern is shown for SNPs having positive CCs (figure 4b). For CAN2, which accounted
193 only for the 8% of the total variability, the differences among the genotypic frequencies are less
194 marked and, therefore were not reported.

195

196 **Conclusions**

197 The study demonstrated that the canonical discriminant analysis was able to efficiently distinguish
198 the three breeds involved in the research by using genomic data, also at chromosome level. The
199 high correlation (0.75) between the number of SNPs in a chromosome and the distance among
200 breeds suggested that the more markers are involved the more efficiently groups are discriminated.
201 The subsequent GW-CDA developed by using a reduced number of markers (1,836), chosen among
202 most discriminants, confirmed the ability of the method in separating groups. These results
203 suggested that if really different breeds are under study, even if not highly differentiated, a clear
204 separation could be reached by enlarging the number of SNPs involved in the analysis. however,
205 further analyses involving other breeds should be carried out to confirm this hypothesis. The
206 Hotelling's statistical test evaluated in the GW-CDA developed by using 340 linearly independent
207 SNPs indicated an highly significant difference among breeds, thus confirming the hypothesis that
208 the three cattle populations can be differentiated by using genomic variables. The technique does
209 not require a pool of preselected markers being the detection of the most discriminant markers one
210 of the expected outputs. However, to assess the difference among breeds by using the Hotelling's
211 test, around 2,000 genotyped animals are required. Finally, 48 SNPs were able to separate groups
212 and, by using the DA, new observations were 100% correctly assigned. Moreover, the assignment
213 tests developed by using an independent software as GeneClass2, confirmed the ability of CDA in
214 selecting pool of discriminant markers. The selected 48 markers could be used to create an assay
215 that could be routinely applied to trace milk, meat or other animal products derived from the three
216 breeds involved in the study.

217

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219 Innovagen)

220

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278 **Table 1** Mahalanobis’ distances among group centroids of breeds and, in bracket, the Hotelling’s
279 test of significance evaluated by using 340 linearly independent SNPs

	Brown	Simmental
Simmental	301 (<0.0001)	
Holstein	4300 (<0.0001)	3574 (<0.0001)

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285 **Table 2** Canonical coefficients (CC), in the two canonical functions (CAN1 and CAN2), for the
286 most 48 discriminant markers selected among SNPs belonging to the Illumina BovineSNP50 v2
287 BeadChip

SNP name	BTA	CC (CAN1)	SNP name	BTA	CC (CAN2)
BTB-01524285	5	0.944	Hapmap56688-rs29025335	6	-0.671
ARS-BFGL-NGS-116089	15	0.941	ARS-BFGL-NGS-100916	6	-0.666
Hapmap51971-BTA-18711	11	0.936	ARS-BFGL-NGS-103634	18	-0.664
BTB-01648149	3	0.936	Hapmap30962-BTC-032558	6	-0.651
BTA-23857-no-rs	12	0.933	ARS-BFGL-NGS-41271	20	-0.648
BTB-01267305	5	0.932	ARS-BFGL-NGS-108820	6	-0.645
BTA-73563-no-rs	5	0.931	BTB-00049653	1	-0.640
BTA-79188-no-rs	1	0.930	Hapmap27224-BTA-161106	6	-0.640
ARS-BFGL-NGS-3048	29	0.929	ARS-BFGL-NGS-67658	6	-0.640
BTB-00498059	12	0.928	BTB-00259302	6	-0.639
Hapmap33485-BTA-144281	6	0.928	Hapmap54879-rs29017018	6	-0.635
Hapmap55512-rs29011234	26	0.928	Hapmap52160-rs29020798	6	-0.627
ARS-BFGL-NGS-22403	16	-0.921	ARS-BFGL-NGS-20141	7	0.633
BTA-58999-no-rs	24	-0.922	BTA-37834-no-rs	5	0.636
UA-IFASA-3757	13	-0.922	BTA-110240-no-rs	6	0.636
BTB-00506196	12	-0.922	Hapmap42715-BTA-87995	6	0.643
BTB-00951350	27	-0.925	Hapmap57799-rs29012894	11	0.643
BTB-00506214	12	-0.926	ARS-BFGL-BAC-33135	18	0.650
ARS-BFGL-NGS-36907	26	-0.928	Hapmap50117-BTA-81807	6	0.650
BTB-00146014	3	-0.928	Hapmap44452-BTA-22099	6	0.681
Hapmap44270-BTA-67318	9	-0.928	Hapmap33128-BTC-041916	6	0.766
BTB-00178642	4	-0.928	Hapmap26269-BTC-041695	6	0.782
BTA-18115-no-rs	2	-0.937	ARS-BFGL-NGS-38827	6	0.785
Hapmap51008-BTA-62521	27	-0.943	Hapmap27692-BTC-042876	6	0.787

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294 **Figure 1** Graph of the two canonical functions (CAN1 and CAN2) obtained in a canonical
295 discriminant analysis applied to BTA1 and BTA28, the two chromosomes with the greater and the
296 lower number of SNP-variables, respectively.

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301 **Figure 2** Graph of the two canonical functions (CAN1 and CAN2) obtained in a genome wide
302 canonical discriminant analysis by using a restricted number (1836) of SNP-variables

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308 **Figure 3** Graph of the two canonical functions (CAN1 and CAN2) obtained in a genome wide
309 canonical discriminant analysis by using a restricted number (48) of linearly independent SNP-
310 variables.

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317 **Figure 4** Genotypic frequencies for 48 highly discriminant SNPs for negative (a) and positive (b)
 318 canonical coefficients (CC) in the first canonical function (CAN1)

319