

AperTO - Archivio Istituzionale Open Access dell'Università di Torino

Food Traceability Systems: Performance Evaluation and Optimization

This is the author's manuscript

Original Citation:

Availability:

This version is available <http://hdl.handle.net/2318/78780> since

Published version:

DOI:10.1016/j.compag.2010.10.009

Terms of use:

Open Access

Anyone can freely access the full text of works made available as "Open Access". Works made available under a Creative Commons license can be used according to the terms and conditions of said license. Use of all other works requires consent of the right holder (author or publisher) if not exempted from copyright protection by the applicable law.

(Article begins on next page)



UNIVERSITÀ DEGLI STUDI DI TORINO

This Accepted Author Manuscript (AAM) is copyrighted and published by Elsevier. It is posted here by agreement between Elsevier and the University of Turin. Changes resulting from the publishing process - such as editing, corrections, structural formatting, and other quality control mechanisms - may not be reflected in this version of the text. The definitive version of the text was subsequently published in [*Food traceability systems: Performance evaluation and optimization*, 75, 1, January 2011, doi 10.1016/j.compag.2010.10.009].

You may download, copy and otherwise use the AAM for non-commercial purposes provided that your license is limited by the following restrictions:

- (1) You may use this AAM for non-commercial purposes only under the terms of the CC-BY-NC-ND license.
- (2) The integrity of the work and identification of the author, copyright owner, and publisher must be preserved in any copy.
- (3) You must attribute this AAM in the following format: Creative Commons BY-NC-ND license (<http://creativecommons.org/licenses/by-nc-nd/4.0/deed.en>), [<http://www.sciencedirect.com/science/article/pii/S016816991000219X>]

1 **Food Traceability Systems: Performance Evaluation and Optimization**

2
3 Fabrizio Dabbene^a, Paolo Gay^b

4 ^a IEIIT-CNR - Politecnico di Torino, 24 Corso Duca degli Abruzzi, 10129 Torino – Italy,
5 fabrizio.dabbene@polito.it;

6 ^b D.E.I.A.F.A. – Università degli Studi di Torino, 44 Via Leonardo da Vinci, 10095 Grugliasco (TO) – Italy,
7 paolo.gay@unito.it;

8
9 **Corresponding author:** Paolo Gay

10 Email: paolo.gay@unito.it Tel: +39 011 6708620 Fax: 011 6708591

11 12 **Abstract**

13 The aim of a traceability system is to collect in a rigorous way all the information related to
14 the displacement of the different products along the supply chain. This information proves
15 essential when facing food safety crisis, and allows efficiently managing the consequent
16 product recall action. Although a recall action could be absolutely critical for a company,
17 both in terms of incurred costs and of media impact, at present most companies do not
18 possess reliable methods to precisely estimate the amount of product that would be discarded
19 in the case of recall.

20 The skill of limiting the quantity of recalled products to the minimum can be assumed as a
21 measure of the performance and of the efficiency of the traceability system adopted by the
22 company. Motivated by this consideration, this paper introduces novel criteria and
23 methodologies for measuring and optimizing the performance of a traceability system. As
24 opposed to previous introduced methods, which optimize indirect measures, the proposed
25 approach takes into direct account the worst-case (or the average) quantity of product that
26 should be recalled in the case of a crisis. Numerical examples concerning the mixing of
27 batches in a sausage production process are reported to show the effectiveness of the
28 proposed approach.

29 **Keywords:** traceability, optimization, supply chain management, batch dispersion, MILP

33 **1. Introduction**

34 Traceability in the agricultural/food chain is nowadays a fundamental requirement, which is
35 becoming mandatory in almost all developed countries. As discussed in Ràbade & Alfaro
36 (2006), traceability represents a mechanism for reinforcing the level of coordination between
37 producers and firms, and between firms and retailers

38 Primal goal of a traceability system it to precisely log the history and the location of the
39 different products along the supply chain. Recently, the technological advances in this
40 direction have led to the design of ICT instruments, such as e.g. bar codes and RF-ID
41 devices, aimed at facilitating data acquisition and reducing the traceability management costs
42 (Gandino et al., 2009; Regattieri et al., 2007; and Sahin et al. 2002), and to the development
43 of data bases and web-based systems for data processing (Alfaro & Ràbade, 2009; Ruitz-
44 Garcia et al., 2010). The information collected by the traceability systems becomes strategic
45 in the unfortunate case when a batch of product has to be recalled (Bechini et al., 2008).
46 Indeed, besides the media impact of this action, the firm has to incur costs related to the
47 recall and the destruction of all the products that are, in some way, connected with the
48 incriminated batch (Jacobs, 1996). Since this occurrence could be absolutely critical for a
49 company, some studies have been carried on for modelling and forecasting the effects of
50 recall actions (e.g., see Kumar & Budin, 2006 and Randrup et al., 2008). However, at
51 present most companies do not have reliable methods to precisely estimate the amount of
52 product that has to be discarded in the case of a recall. Indeed, this quantity, to which we
53 associate a *recall cost* (RC), depends on many factors:

- 54 – the size of the batches that have been individually tracked and managed by the
55 traceability system;
- 56 – the way the batches of different components have been mixed to obtain the final product;
- 57 – the skill of the firm to manage and maintain segregated different batches of product,
58 especially in the case of continuous processes (e.g. milk processing in a dairy, grain or
59 soya, see for instance Thakur & Hurburg, 2009, Thakur et al., 2010, Thakur & Donnelly,
60 2010, and Skoglund & Dejmek, 2007).

61 From the analysis of these factors, it is clear that a simple reduction in the size of the
62 batches, and their consequent increase in number, leading to a finer granularity of the
63 traceability system (Bertolini et al, 2006), may be not sufficient to minimize the amount of
64 product to be discarded. For a discussion on the role of different levels of granularity the

65 interested reader is referred to Karlsen (2011) and references therein, where an example
66 related to farmed salmon is also presented.

67

68 The previous considerations suggest selecting the recall cost as a natural measure of the
69 performance for a traceability system. This gives rise to two fundamental problems: i) the
70 evaluation of the performance of a given traceability system, ii) the optimization of the
71 supply-chain design in order to minimize its performance.

72

73 To better formalize these problems, some nomenclature has to be introduced. Moe (1998)
74 has introduced the concept of *traceable resource unit* (TRU) for batch processes as “unique
75 unit, meaning that no other unit can have exactly the same, or comparable, characteristics
76 from the point of view of traceability”. In modern agricultural supply system, units must be
77 uniquely identifiable within each system in which they are processed. To this extent, Bollen
78 et al. (2007) introduced the *identifiable unit* (IU), whose size reflects the granularity of the
79 traceability system. In many supply chains granularity is the consequence of a combination
80 of tradition, short-term convenience and use of available facilities. In very few cases
81 granularity depends on the results of a formal analysis and optimization in the supply chain.
82 The simple implementation of a finer granularity by itself has no value unless it provides
83 more precise traceability. The precision of a traceability system can be evaluated, as
84 discussed in Bollen et al. (2007), as the ratio between IUs at two points in the supply chain
85 and it is the consequence of the number and the nature of the transformations of IUs and of
86 the extent, nature and accuracy of data recorded. If a IU is split up, the separated parts keep
87 the identification of the parent IU, while if some IUs are put together, the identification of
88 the IU is different from the identification of the parent IUs.

89 One possible solution to maintain the same level of traceability precision consists of
90 breaking the processing into segments of relative homogeneity, both for processing
91 conditions and product origin, and recording all relevant information.

92

93 Finally, one has to take into account if the product is processed in completely separated runs,
94 or if some mixing can occur between products of two succeeding batches. In the latter case,
95 it is necessary to specify if tolerances can be accepted. This problem has been addressed by
96 Skoglund & Dejmek (2007) for the case of continuous processing where it has been referred

97 as *fuzzy traceability*, while Riden & Bollen (2007) considered the case of discrete products,
98 with an application to packhouse processing transformations.

99

100 The problem of the performance evaluation and optimization of traceability systems was first
101 introduced by Dupuy et al. (2005), and successively applied in different endeavours (see for
102 instance Donnelly et al., 2009). Tamayo et al. (2009) employ genetic algorithms to solve the
103 optimization problem proposed by Dupuy et al. (2005). Finally, Wang et al. (2010) propose
104 the joined optimization of traceability and manufacturing performances, acting both on batch
105 sizes and batch dispersion, by introducing risk functions. In all these works, the performance
106 of a traceability system is associated to the number of active paths between raw-materials
107 and finished products, as formally detailed in Section 3. This measure is indeed related to the
108 final quantity to be recalled, since it aims at reducing the mixing of different batches, and
109 was proven effective in the above-mentioned works. However, it should be remarked that, in
110 general, the minimization of this index does not necessarily result in the minimization of the
111 recall cost, when intended as the quantity of products to be recalled in the worst-case.

112

113 In this paper, we introduce a modelling framework and optimization strategy to cope with
114 this problem, directly adopting the recall cost as performance criterion. Similarly to Dupuy
115 et al. (2005), the optimization problem is expressed in the form of mixed-integer linear
116 programming (MILP), for which efficient numerical solvers are available. To show its
117 effectiveness, the proposed approach has been first applied to the numerical example
118 presented in Dupuy et al. (2005) and in Tamayo et al. (2009), and finally to a larger test case.

119

120 **2. Modelling**

121 A complete food production process can be seen as a sequence of storage/carrying actions
122 and of unit operations. Bulk products are stored and carried in containers (as for instance
123 tanks, vats, bins etc.) depending on the nature of the products. Unit operations can be
124 conducted on a batch of product at a time (e.g. concentration in a bull, cooking in a oven) or
125 continuously, as the processes of milk pasteurization/sterilization, or of concentration in a
126 continuous evaporator.

127 From the point of view of traceability, this second instance (continuous unit operations) can
128 also be interpreted as a batch process situation, by either guaranteeing proper cleaning cycles

129 between two subsequent lots, or by allowing (and then neglecting) small percentages of
 130 contamination (Skoglund & Dejmek, 2007). Each container/processing-unit that individually
 131 stores/ processes a batch of product, at a certain time, can be modeled as a node in a graph.

132

133 Formally, at each node k one associates a variable Q_k , which accounts for the quantity of
 134 product contained in the node. This variable can be bounded by the capacity of the container,
 135 or by the amount of product that can be processed at a time. This corresponds to imposing
 136 the constraint $Q_k \leq \bar{Q}_k$. In some cases, it is also possible to introduce the equality constraint
 137 $Q_k = \bar{Q}_k$ to reflect the cases when one wants to fix the quantity of material in node k
 138 precisely to the value \bar{Q}_k . This is the case, for instance, of final products that are sold in
 139 fixed-weight packages, or of middle nodes where a fixed amount of product is processed at a
 140 time.

141

142 The flow of the batches inside the supply chain is modeled via a number of oriented arrows
 143 (links of the graph). These links are formally described introducing a $m \times 2$ matrix $L \in N_+^{m,2}$
 144 of positive numbers, where m is the number of links. The entries of L have the following
 145 structure: $L_{i,1}$ indicates the starting node of the link i , while $L_{i,2}$ represents its destination
 146 node. The amount of material transferred through the i -th link is expressed by the variable
 147 $\alpha_i \in R$, $\alpha_i \geq 0$, $i = 1, 2, \dots, m$. Associated to the variable α_i , one can define the *binary* variable
 148 $\bar{\alpha}_i$, which is true whenever the i -th link is active, that is

$$\bar{\alpha}_i = \begin{cases} 1 & \text{if } \alpha_i > 0 \\ 0 & \text{if } \alpha_i = 0. \end{cases} \quad (1)$$

149

150 Nodes can be schematically grouped into three sets: input, processing and output nodes.
 151 Letting $I = \{1, 2, \dots, n_{nodes}\}$ be the set of the indexes of all nodes, one can define $I_{in} \subset I$ and
 152 $I_{out} \subset I$ as the sets of indexes of the input and output nodes, respectively. The cardinality of
 153 these sets (i.e. the number of elements belonging to the set) is denoted as n_{in} and n_{out} ,
 154 respectively. Then, to each input node $k \in I_{in}$ is associated the initial quantity of available
 155 product (raw material) Q_k^0 that has to be transferred and/or processed by the network.

156

157 For any node $k \in I$, one defines the sets of links entering and leaving the node as

$$in_k = \{i \in I : L_{i,2} = k\} \quad \text{and} \quad out_k = \{i \in I : L_{i,1} = k\}. \quad (2)$$

158

159 These indices allow expressing the mass balances for each node k as follows

$$\sum_{i \in in_k} \alpha_i = \sum_{i \in out_k} \alpha_i = Q_k. \quad (3)$$

160

161 The modeling framework proposed in this paper relies on the definition of specific “state
 162 variables” $S_k^l \in \{0,1\}$, $k, l \in I$. The binary variable S_k^l is true whenever the node k contains a
 163 product arising from node l , that is whenever there exists a *path* in the graph connecting
 164 node l to node k . Notice that the state S_k^l can be recursively calculated using the following
 165 relation

$$S_k^l = \bigvee_{i \in in_k} (S_{L_{i,1}}^l \wedge \bar{\alpha}_i), \quad (4)$$

166 where \vee and \wedge represent the logical OR and AND operators respectively. The initial
 167 conditions for recursion (4) are given by

$$S_k^k = 1 \text{ for } k \in I_{in} \quad \text{and} \quad S_k^l = 0 \text{ for } k \in I_{in} \setminus \{l\}. \quad (5)$$

168

169 We recall that both OR and AND operators may be rewritten as linear operations on binary
 170 variables, see for instance Achterberg et al. (2007). More precisely, for binary variables
 171 $a, b, r \in \{0,1\}$, one can write

$$r = a \wedge b \Leftrightarrow \begin{cases} r \leq a \\ r \leq b \\ r \geq a + b - 1 \end{cases} \quad (6)$$

$$r = a \vee b \Leftrightarrow \begin{cases} r \geq a \\ r \geq b \\ r \leq a + b \end{cases} \quad (7)$$

172

173 A simple example of the modeling framework introduced in (1)-(5) is presented in Figure 1.
 174 To illustrate the meaning of the introduced variables, in this figure the explicit construction
 175 of the states introduced in (4) is provided for node 6 and source 1 as an example. The
 176 recursive nature of the states is clearly evidenced: the state S_6^1 depends on S_4^1 and S_5^1 , which
 177 in turn are functions of the state of the sources, which are given by the initial conditions

178 introduced in (5). Notice that, after the recursion is resolved, one obtains a relationship
 179 whose interpretation is clear: node 6 contains material from node 1 whenever both links α_1
 180 and α_6 , or links α_2 and α_8 , are simultaneously active.

181

182 In a generic supply chain, the lots of products are displaced and/or processed according to
 183 some rules that govern each mixing occurrence. In the proposed setup, these rules are
 184 generically referred to as *recipe rules*, and are defined on sets of nodes containing
 185 homogeneous products. In this way, a (possibly large) number of nodes that are devoted to
 186 contain the same type of product can be grouped into a single set. Recipes, which are related
 187 to sets, are valid for each node belonging the involved set. More formally, one can define
 188 n_{type} disjoint sets $T_p \subseteq I$, $p = 1, 2, \dots, n_{type}$, of indices, where the set T_p is formed by the indices
 189 of the nodes that contain a product of type p . Then, recipe constraints can be generally
 190 expressed as linear relationships between product types. In particular, one can define
 191 assembling and disassembling recipes as in Dupuy et al. (2005). This is done by introducing
 192 the matrices of coefficients $D \in R^{n_{type} \times n_{type}}$ and $A \in R^{n_{type} \times n_{type}}$. Then, a disassembling constraint
 193 allows describing the situation when each product belonging to a given type p has to be
 194 destined to nodes belonging to the set T_j according to the percentage expressed by $D_{p,j}$, i.e.

$$\sum_{\substack{i \in out_k \\ L_{i,2} \in T_j}} \alpha_i = D_{p,j} Q_k \quad \text{for } \forall k \in T_p \text{ and } p = 1, \dots, n_{type}. \quad (8)$$

195

196 Analogously, assembly constraints impose that each product of type p has to be composed
 197 by product of type j , according to the percentage $A_{p,j}$.

$$\sum_{\substack{i \in in_k \\ L_{i,1} \in T_j}} \alpha_i = A_{p,j} Q_k \quad \text{for } \forall k \in T_p \text{ and } p = 1, \dots, n_{type} \quad (9)$$

198

199 It should be remarked that the modelling framework proposed in this section improves upon
 200 the one in Dupuy et al. (2005) in the following points: i) the original approach of Dupuy et
 201 al. (2005) considers only three-stages production systems, with a raw-materials stage, a
 202 components stage and a finished products one; ii) only fully-interconnected networks (each
 203 node at one stage is connected to each node in the successive stage) are considered in Dupuy
 204 et al. (2005). On the contrary, the introduction of the link matrix L allows considering

205 arbitrary networks, that is graph configuration consisting of multiple stages and arbitrary link
206 configurations. In particular, this second feature allows excluding a-priori undesired or
207 logistically unfeasible links, thus leading to a significant reduction in the complexity of the
208 ensuing optimization problem. Also, the introduction of the state variables S allows a clear
209 formalization of the desired performance measures related to the recall cost, as shown in the
210 next section.

211

212 **3. Performance evaluation**

213 As discussed in the Introduction, different measures can be defined for assessing the
214 performance of a traceability system. In particular, Dupuy et al. (2005) defined three
215 performance indices: the downward dispersion, the upward dispersion and the batch
216 dispersion. The downward dispersion of a raw material batch is the number of final batches
217 that contain parts of a specific raw material batch. The upward dispersion of a finished
218 product batch is the number of different raw material batches used to produce this batch,
219 while the batch dispersion is defined in Dupuy et al. (2005) as the sum of links between the
220 raw material batches and the finished product batches. The analytical expression of these
221 indices is formally defined at the end of this section.

222

223 As previously discussed, the approach in Dupuy et al. (2005) does not take into account
224 quantities, but only the active paths that are upward/downward involved. However, this
225 setup has the great advantage of allowing a formalization of the optimization problem in
226 terms of mixed-integer linear programming (MILP). Motivated by the fact that the number
227 of variables and constraints in the ensuing MILP problem may increase exponentially,
228 Tamayo et al. (2009) proposed to solve this problem by means of genetic algorithms.

229 Proceeding along the same lines that in Dupuy et al. (2005), in this paper novel performance
230 indices are introduced, which better quantify the cost of product recall as perceived by the
231 industry. To this extent, first introduce the recall cost of product l , $RC(l)$, as the total amount
232 of (final) product that has to be recalled in the case when the batch of raw material contained
233 in node l is recognized as lacking the requirements. This corresponds to the mass of final
234 product that contains – owing to mixing operations – part of the material originally stored in
235 the incriminated node l .

236 On the basis of the formalism presented in the previous section, the recall cost relative to
 237 node l can then be directly defined as

$$RC(l) = \sum_{k \in I_{out}} S_k^l Q_k \quad (10)$$

238
 239 The typical interest of a company is to know – and possibly to reduce – the worst-possible
 240 amount of product that could be necessary to recall. This corresponds to defining the *worst-*
 241 *case recall cost (WCRC)*

$$WCRC = \max_{l \in I_{in}} RC(l) = \max_{l \in I_{in}} \sum_{k \in I_{out}} S_k^l Q_k. \quad (11)$$

242
 243 as the largest amount of product that has to be recalled when a batch of raw material is found
 244 unsafe. Analogously, it is possible to define the *average recall cost (ARC)* index as

$$ARC = \frac{1}{n_{in}} \sum_{l \in I_{in}} RC(l) = \frac{1}{n_{in}} \sum_{l \in I_{in}} \sum_{k \in I_{out}} S_k^l Q_k, \quad (12)$$

245
 246 which represents the average mass of product to be recalled when one of the entering
 247 material is found inappropriate.

248 It should be remarked that the *ARC* cost defined in (12) can be readily adapted to the case
 249 when suppliers of the input batches have a different level of reliability and/or one can
 250 associate to different input batches different probabilities of lacking the requirements. This
 251 can be modelled introducing appropriate weights w_i , $i = 1, \dots, n_{in}$, (that can be interpreted
 252 also as probabilities). This leads to the following *weighted recall cost (WRC)* index

$$WRC = \sum_{l \in I_{in}} w_l RC(l) = \sum_{l \in I_{in}} w_l \sum_{k \in I_{out}} S_k^l Q_k, \quad (13)$$

253
 254 Finally, it should be remarked that the introduced setup can easily handle the *batch*
 255 *dispersion cost (BDC)* introduced in Dupuy et al. (2005), by introducing the downward
 256 dispersion from node l as

$$D_DISP(l) = \sum_{k \in I_{out}} y(l, k) \quad (14)$$

257 where

$$y(l,k) = \begin{cases} 1 & \text{if } S_k^l Q_k > 0 \\ 0 & \text{if } S_k^l Q_k = 0 \end{cases} \quad (15)$$

258 Then, the *BDC* index can be written as

$$BDC = \sum_{l \in I_{in}} D_DISP(l) = \sum_{l \in I_{in}} \sum_{k \in I_{out}} y(l,k), \quad (16)$$

259

260 and it represents the sum of links between the raw material batches and the finished product
261 batches. Notice that (16) is exactly the index minimized in Dupuy et al. (2005).

262

263 **4. Optimization**

264 Different approaches can be adopted to optimize the performance of the traceability system.

265 The first possibility is to *compare different scenarios*. Even if this technique cannot properly
266 be referred to as optimization, it permits to compare via simulation some selected
267 configurations of the production process and/or the supply chain (Gay et al., 2009). It is a
268 helpful approach when a decision among few possible alternatives has to be taken. However,
269 clearly this methodology does not bring out optimal solutions that have not been already a-
270 priori selected.

271 A more rigorous approach is *direct optimization*, as in Dupuy et al. (2005) and Tamayo et al.
272 (2009). This methodology is to be preferred whenever one or more parameters of the supply
273 chain have to be designed according to an optimality criterion. In our case, as in Dupuy et al.
274 (2005), the parameters to be designed are the product flows α_i , $i=1, \dots, m$ and the
275 considered optimality criteria are the batch dispersion recalled in (16), and the worst-
276 case/average recall costs defined in (11) – (12).

277 It should be noticed that the framework introduced in Section 2 allows formulating the
278 problem of minimizing both the original batch dispersion measure (Dupuy et al., 2005) and
279 newly introduced more realistic performance measures *WCRC* and *ARC* in terms of mixed-
280 integer linear programs. To this end, first notice that both *WCRC* and *ARC* objective
281 functions contain the product of terms $S_k^l \in \{0,1\}$ and $Q_k \in R$. These quantities depend both
282 on the optimization variables α_i . However, this nonlinearity can be converted in a set of
283 linear inequalities. To see this, remark that an optimization problem of the type $\min S_k^l Q_k$
284 can be reformulated by introducing an additional real variable $r = S_k^l Q_k$, as follows

285

$$\begin{aligned}
\min S_k^l Q_k &\Leftrightarrow \min r && (17) \\
&\text{subject to: } r \geq 0 \\
& r \geq Q_k - M(1 - S_k^l) \\
& r \leq Q_k
\end{aligned}$$

286 where M is a sufficiently large number. Notice also that the minimization of the cost
287 function $WCRC$ in (11), which presents a maximization term, can be reduced to a linear
288 problem by simply writing

$$\begin{aligned}
\min \max_{l \in I_{in}} RC(l) &\Leftrightarrow \min \gamma && (18) \\
&\text{subject to: } RC(l) \leq \gamma, l \in I_{in}
\end{aligned}$$

289 Finally, also the binary version $\bar{\alpha}_i$ of α_i introduced in (1) can be reformulated in the integer
290 programming paradigm by introducing the following two linear constraints

$$\bar{\alpha}_i \leq M\alpha_i, \quad \bar{\alpha}_i \geq \frac{\alpha_i}{M} \quad (19)$$

291 where again M is a sufficiently large number. The same operation can be made for
292 introducing equation (14).

293

294 **5. Numerical examples**

295 In order to demonstrate the effectiveness of the proposed approach, the same example
296 proposed in Dupuy et al. (2005), and subsequently elaborated in Tamayo et al. (2009), is
297 here considered. The problem concerns a sausages fabrication chain modelled as a three-
298 level network, consisting of four batches of input (raw) material divided into two types of
299 product (RM1 and RM2), six processing batch units (“components”, according to the
300 notation introduced in Dupuy et al., 2005) divided into two types (SP1 and SP2), two
301 batches of bought components (additional inputs), one of each type (i.e., SP1 and SP2
302 again), and four batches of finished product, also divided into two types (FP1 and FP2).
303 Since the network is fully interconnected, all α_i , $i = 1, \dots, 56$, coefficients have to be
304 determined.

305 To solve the problem, the batch dispersion minimization and the newly introduced $WCRC$
306 and ARC minimization problems have been written as MILPs using the YALMIP software,
307 that allows parsing of optimization problems under Matlab, see Löfberg (2004) for
308 additional details. The resulting MILP programs were then solved using the commercial
309 solver CPLEX (ILOG-IBM), on a 2.53GHz Macbook Pro.

310 In the first numerical example, the exact same numerical setup used in Tamayo et al. (2009)
 311 was adopted, with initial values for the first nodes equal to $Q_1^0 = Q_3^0 = 1,000$ and
 312 $Q_2^0 = Q_4^0 = 1,200$, and with final desired quantities in the last four nodes set to the values
 313 $\bar{Q}_{13} = \bar{Q}_{14} = \bar{Q}_{15} = \bar{Q}_{16} = 2,000$. The solution minimizing the average cost criterion ARC was
 314 sought. The CPLEX solver returned, after 2.7 sec of elaboration, the solution reported in
 315 Figure 2, which is guaranteed to be optimal. The average recall cost of this configuration is
 316 $ARC = 3,333$. The graph contains a total of 23 links, and ten direct source-destination paths,
 317 hence providing a batch dispersion measure $BDC = 10$. These figures can be compared with
 318 the numerical solution obtained in Tamayo et al. (2009), which has a recall cost
 319 $ARC = 3,667$. This corresponds to a 10% improvement of our solution. However, it should
 320 be noted that the solution in Tamayo et al. (2009) presents 13 direct source-destination paths
 321 ($BDC=13$), and hence it is not optimal also for the batch dispersion cost introduced by
 322 Dupuy et al. (2005). This fact is not surprising, since the genetic algorithm approach in
 323 Tamayo et al. (2009) does not provide any guarantee of returning an optimal solution.
 324 Hence, we computed the optimal solution using the BDC cost, which provided the same
 325 performance as our ($ARC = 3,333$ and $BDC = 10$), with a computation time of 5.8 sec. A
 326 similar behavior was observed when comparing with the worst-case optimality criterion
 327 $WCRC$.

328
 329 Based on this observation, a second numerical example was run. This second example
 330 considers the same node configuration of the first one, but with the quantities in the first
 331 nodes, and the final desired quantities in the last four nodes, now unbalanced. That is,
 332 $Q_1^0 = 450$, $Q_2^0 = 2,350$, $Q_3^0 = 150$, $Q_4^0 = 1,450$, and $\bar{Q}_{13} = 1,750$, $\bar{Q}_{14} = 3,150$, $\bar{Q}_{15} = 2,250$,
 333 $\bar{Q}_{16} = 850$. The solution of the three different optimality indices BDC , ARC and $WCRC$
 334 were again computed using the CPLEX solver. Optimal solutions were returned respectively
 335 in 92.5, 47.8 and 0.6 seconds. The respective optimal configurations are shown in Figures 3,
 336 4 and 5, and the relative quantities of interest are reported in Table 1.

337
 338 A few comments are at hand for the figures reported in Table 1. First, it can be observed that
 339 the BDC solution, although presenting fewer direct paths between input and final nodes,
 340 provides an average recall cost that is around 23% worse than the optimal ARC one, and a
 341 worst-case recall cost that is more than 55% worse than the optimal $WCRC$ one. Second, this

342 improvement in performance is obtained together with an even more significative
343 improvement in terms of computational cost: the *WCRC* optimization was about 156 times
344 faster than *BDC*, and about 81 times faster than *ARC*.

345

346 Finally, the *BDC* and *WCRC* optimization criteria were compared in a larger example,
347 consisting of on four layers, with 8 batches of input (raw) material, 7 nodes in the second
348 layer, 16 nodes in the third layer and 13 batches of finished product was considered. This
349 network is only partially interconnected, according to the diagram reported in Fig. 6. As it
350 can be seen, the initial configuration contains 78 feasible links and 44 nodes (a fully-
351 interconnected configuration would involve 376 links). The maximum capacity of each
352 node, the amount of raw material of the input batches and the desired quantity in the output
353 nodes are also reported in Fig. 6. Remark that the particular features in this example, i.e. a
354 number of layers and the definition *a-priori* of the set of feasible links, can not be managed
355 by the formulation in Dupuy et al. (2005).

356

357 The solutions of the two minimizations are reported in Figures 7 and 8, respectively for the
358 *BDC* and the *WCRC* criteria. The relative quantities of interest are reported in Table 2. To
359 comments these results, it can be observed that the direct minimization of the worst-recall
360 cost allows a 25% improvement of the *WCRC* performance. This can be interpreted as
361 follows: by adopting the configuration in Figure 8 one is guaranteed that, no matter what is
362 the initial product found inadequate, the quantity of material to be recalled will be less than
363 24,600. Contrary, adopting the *BDC* solution of Dupuy et al. (2005) reported in Figure 7,
364 one can incur a recall cost as high as 30,750. Also, it can be noted that, as a side product, the
365 *WCRC* minimization allows to exclude from the supply chain four nodes (nodes 23, 26, 27,
366 31), while the optimal *BDC* one excludes two nodes only (22, 31). In a typical industrial
367 situation, this would easily correspond to a save in the production costs. Moreover, also in
368 this case, the computation time for the *BDC* criterion was dramatically higher than the one
369 of *WCRC* (7 days compared to half an hour). This behavior, which was observed in all our
370 simulations, can be explained by the fact that the *BDC* cost function formulation (15)
371 requires the introduction of $n_{in} \times n_{out}$ binary variables, which are not present in the *WCRC*
372 one. This seems to explain the large increase in the computational time.

373

374 **4. Conclusions and future research directions**

375 In this paper novel criteria and methodologies for measuring and optimizing the performance
376 of a traceability system have been introduced. As opposed to the methods previously
377 adopted, which optimize indirect measures, the proposed approach takes in direct account
378 the worst-case or the average quantity of product that should be recalled in the case of a
379 crisis. Numerical examples testify to the effectiveness of the proposed methodology, both in
380 terms of performance and of computational cost.

381 **5. Acknowledgements**

382 The authors would like to thank Constantino M. Lagoa for the fruitful and inspiring
383 discussions on the topics of this paper that arose while he was visiting the first author. This
384 work was partially supported by the grants of the project Namatech – Converging
385 Technologies (CIPE2007), Regione Piemonte, Italy.

386

387 **References**

388

389 Achterberg, T., Brinkmann R., Wedler M., 2007. Property checking with constraint integer
390 programming, ZIB-Report 07-37, Konrad-Zuse-Zentrum für Informationstechnik Berlin.

391

392 Alfaro, J. A., Ràbade, L. A., 2009. Traceability as a strategic tool to improve inventory
393 management: A case study in the food industry. *International Journal of Production*
394 *Economics* 118, 104-110.

395

396 Bechini, A., Cimino, A., Marcelloni, F., Tomasi, A., 2008. Patterns and technologies for
397 enabling supply chain traceability through collaborative e-business. *Information and*
398 *software technology* 50, 342-359.

399

400 Bertolini, M., Bevilacqua, M., Massini, R., 2006. FMECA approach to product traceability
401 in the food industry. *Food Control* 17(2), 137-145.

402

403 Bollen, A. F., Riden, C. P., Cox, N. R., 2007. Agricultural supply system traceability, Part I:
404 Role of packing procedures and effects of fruit mixing. *Biosystems Engineering* 98, 391-
405 400.

406

407 Donnelly, K. A. M., Karlsen, K., Olsen, P., 2009. The importance of transformations for
408 traceability – A case study of lamb and lamb products. *Meat Science* 83, 68-73.

409

410 Dupuy, C., Botta-Genoulaz, V., Guinet, A., 2005. Batch dispersion model to optimize
411 traceability in food industry. *Journal of Food Engineering* 70, 333-339.

412

413 Gay, P., Piccarolo, P., Tortia, C., 2009. Food traceability systems: performance evaluation
414 and optimization. Proc. of XXXIII CIOSTA, Reggio Calabria, Italy, 17-19 June, 465-469.

415

416 Gandino, F., Montrucchio, B., Rebaudengo, M., Sanchez, E.R., 2009. On Improving
417 Automation by Integrating RFID in the Traceability Management of the Agri-Food Sector.
418 *IEEE Transactions on Industrial Electronics* 56 (7), 2357-2365.

419

420 Löfberg, J., 2004. YALMIP : A Toolbox for Modeling and Optimization in MATLAB. In
421 Proc. of the CACSD Conference, Taipei, Taiwan.

422

423 Jacobs, R. M., 1996. Product recall – a vendor/vendee nightmare. *Microelectronics*
424 *Reliability* 36 (1), 101-103.

425

426 Karlsen, K.M., Donnelly K.A., Olsen P., 2011. Granularity and its importance for
427 traceability in a farmed salmon supply chain. *Journal of Food Engineering* 102, 1-8

428

429 Kumar, S., Budin, E., 2006. Prevention and management of product recalls in the processed
430 food industry: a case study based on an exporter's perspective. *Technovation* 26, 739-750

431

432 Moe, T., 1998. Perspective on traceability in food manufacture. *Trends in Food Science e*
433 *Technology* 9, 211-214.

434 Ràbade, L. A., Alfaro, J. A., 2006. Buyer–supplier relationship’s influence on traceability
435 implementation in the vegetable industry. *Journal of Purchasing & Supply Management* 12,
436 39-50.
437

438 Randrup, M., Storøy, J., Lievonen, S., Margeirsson, S., Arnason, S. V., Olavstovu, D.,
439 Møller, S. F., Frederiksen, M. T., 2008. Simulated recalls of fish products in five Nordic
440 countries. *Food Control* 19, 1064-1069.
441

442 Riden, C. P., Bollen, A. F., 2007. Agricultural supply system traceability, Part II:
443 Implications of packhouse processing transformations. *Biosystems Engineering* 98, 401-410.
444

445 Regattieri, A., Gamberi, M., Manzini, R., 2007. Traceability of food products: General
446 framework and experimental evidence. *Journal of Food Engineering* 81, 347-356.
447

448 Ruiz-Garcia, L., Steinberger, G., Rothmund, M., 2010. A model and prototype
449 implementaion for tracking and tracing agricultural batch products along the food chain.
450 *Food Control* 21, 112-121.
451

452 Sahin, E., Dallery, Y., Gershwin, S., 2002. Performance evaluation of a traceability system:
453 an application to the Radio Frequency Identification Technology. *Proc. of the IEEE Int.*
454 *Conf. on System, Man and Cybernetics* 3, 210–218.
455

456 Skoglund, T., Dejmek, P., 2007. Fuzzy traceability: a process simulation derived extension
457 of the traceability concept in continuous food processing. *IChem* 85, 354-359.
458

459 Tamayo, S., Monteiro, T., Sauer, N., 2009. Deliveries optimization by exploiting production
460 traceability information. *Engineering Applications of Artificial Intelligence* 22, 557 – 568.
461

462 Thakur, M., Donnelly, K.A.M., 2010. Modeling traceability information in soybean value
463 chains. *Journal of Food Engineering* 99, 98-105
464

465 Thakur, M., Hurburg, C. R., 2009. Framework for implementing traceability system in the
466 bulk grain supply chain. *Journal of Food Engineering* 95, 617-626
467

468 Thakur, M., Wang, L., Hurburgh, C.R., 2010. A multi-objective optimization approach to
469 balancing cost and traceability in bulk grain handling. *Journal of Food Engineering* 101,
470 193-200
471

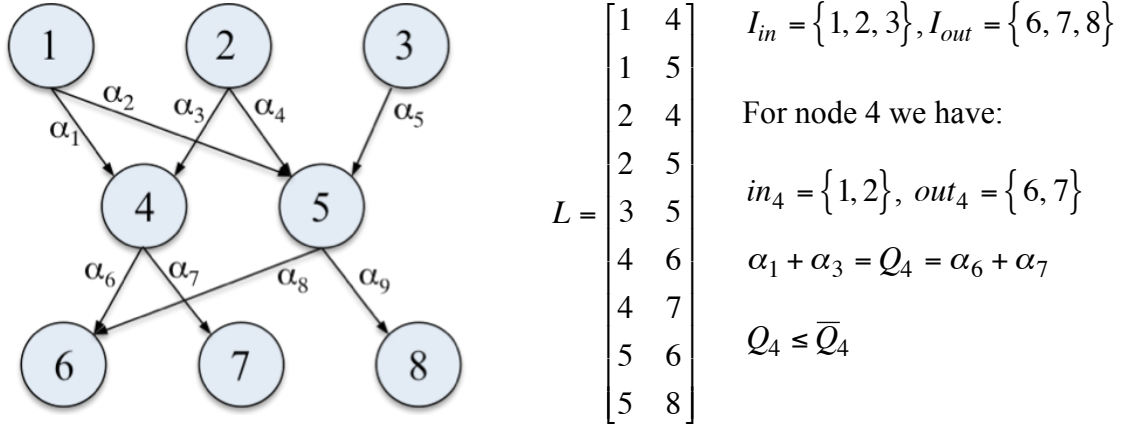
472 Wang, X., Li, D., O’Brien, C., Li Y., 2010. A production planning model to reduce risk and
473 improve operations management. *International Journal of Production Economics* 124, 2,
474 463-474.
475
476
477
478
479
480
481

482 **Notation table**
 483

k, i, l	Indexes
Q_k	Quantity of product contained in the node k
\bar{Q}_k	Maximum capacity of the node k
Q_k^0	Initial amount of product in the node k
N_+	Set of natural positive numbers
R	Set of real numbers
m	Number of links
L	Link matrix
$L_{i,1}$	Starting node of the link i
$L_{i,2}$	Destination node of the link i
α_i	Amount of material transferred through the link i
$\bar{\alpha}_i$	Binary variable equal to one when $\alpha_i > 0$
I	Set of indexes of all nodes
I_{in}	Set of indexes of input nodes
I_{out}	Set of indexes of output nodes
n_{nodes}	Number of nodes
n_{in}	Number of input nodes
n_{out}	Number of output nodes
in_k	Set of links entering the node k
out_k	Set of links leaving the node k
S_k^l	Binary variable equal to one when a product from batch node l is present at node k
\vee	OR - operator
\wedge	AND - operator
a, b, r	Binary variables
M	Sufficiently large number
n_{type}	Number of product types
p	Product type
T_p	Set of nodes containing the type of product p
D	Matrix of recipe disassembling coefficients
A	Matrix of recipe assembling coefficients
$RC(l)$	Recall cost of the product l
w_i	Weights of the weighted recall cost
$WCRC$	Worst-case recall cost
ARC	Average recall cost
WRC	Weighted recall cost
BCD	Batch dispersion cost
$D_DISP(l)$	Downward dispersion from node l

484

Figures



State of node 6 with respect to source node 1:

$$S_6^1 = \bigvee_{i=6,8} (S_{L_{i,1}}^1 \wedge \bar{\alpha}_i) = (S_4^1 \wedge \bar{\alpha}_6) \vee (S_5^1 \wedge \bar{\alpha}_8)$$

$$S_4^1 = \bigvee_{i=1,3} (S_{L_{i,1}}^1 \wedge \bar{\alpha}_i) = (S_1^1 \wedge \bar{\alpha}_1) \vee (S_2^1 \wedge \bar{\alpha}_3) = (1 \wedge \bar{\alpha}_1) \vee (0 \wedge \bar{\alpha}_3) = \bar{\alpha}_1$$

$$S_5^1 = \bigvee_{i=4,5} (S_{L_{i,1}}^1 \wedge \bar{\alpha}_i) = (S_1^1 \wedge \bar{\alpha}_2) \vee (S_2^1 \wedge \bar{\alpha}_4) \vee (S_3^1 \wedge \bar{\alpha}_5) = (1 \wedge \bar{\alpha}_2) \vee (0 \wedge \bar{\alpha}_4) \vee (0 \wedge \bar{\alpha}_5) = \bar{\alpha}_2$$

$$\Rightarrow S_6^1 = (\bar{\alpha}_1 \wedge \bar{\alpha}_6) \vee (\bar{\alpha}_2 \wedge \bar{\alpha}_8)$$

Figure 1: An illustrating example showing the formalism introduced in the paper. An example of equations (2), (3) is reported for node 4. Also, explicit construction of the states introduced in (4) is given for node 6 and source 1.

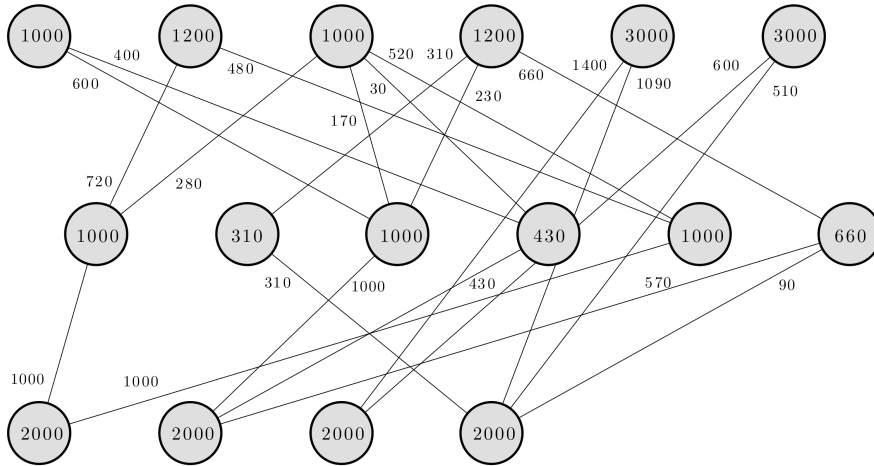


Figure 2: Optimal solution of the example in Tamayo et al. (2009) using the ARC index. The average recall cost of this solution is $ARC=3,333$.

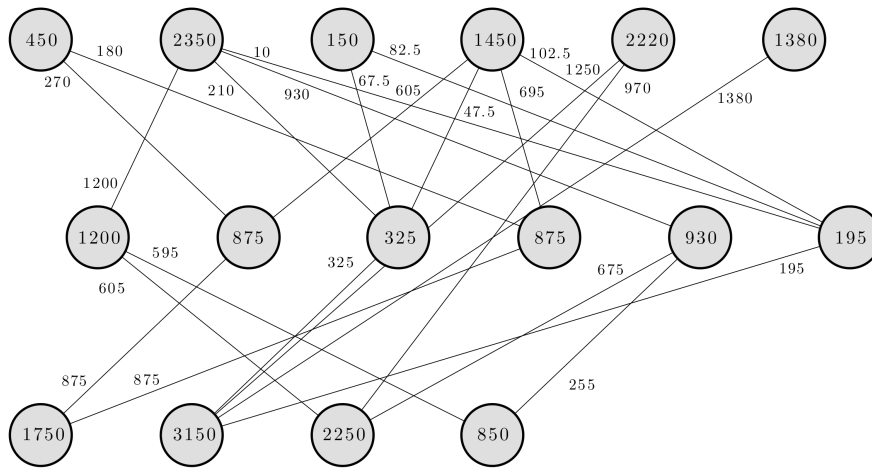


Figure 3: Second numerical example. Optimal solution obtained minimizing the BDC cost.

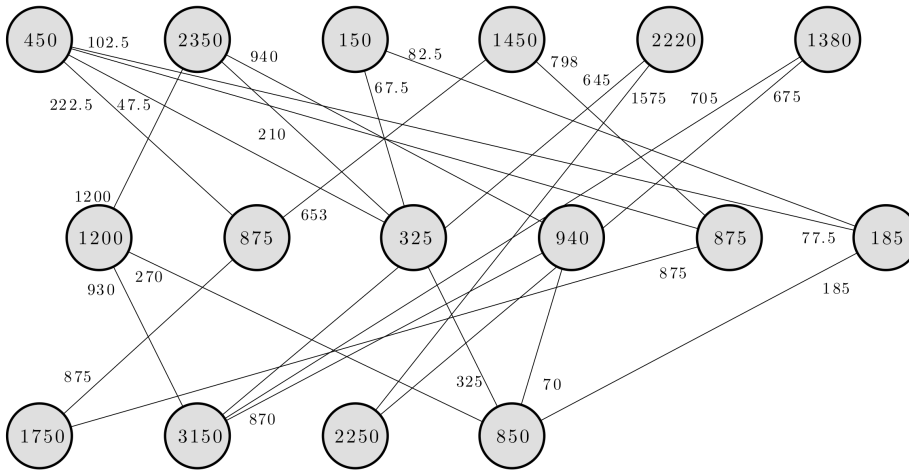


Figure 4: Second numerical example. Optimal solution obtained minimizing the ARC cost.

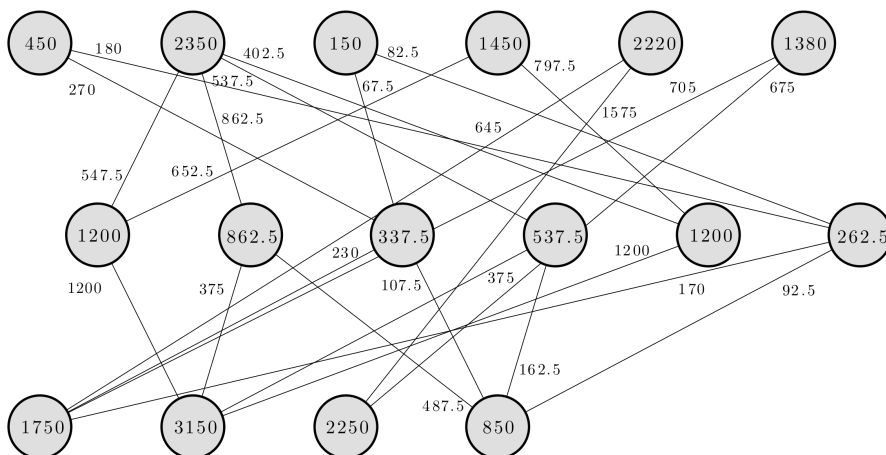


Figure 5: Second numerical example. Optimal solution obtained minimizing the WCRC cost.

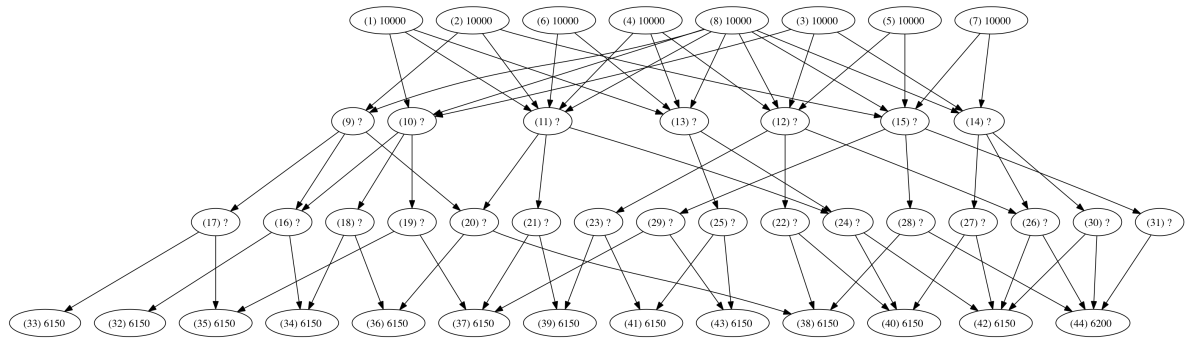


Figure 6: Initial configuration for the four-stage example.

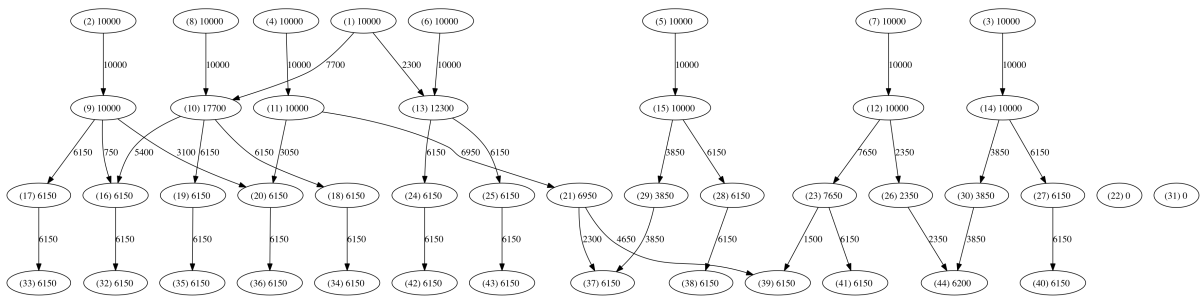


Figure 7: Optimal configuration for the four-stage example obtained minimizing the BDC index.

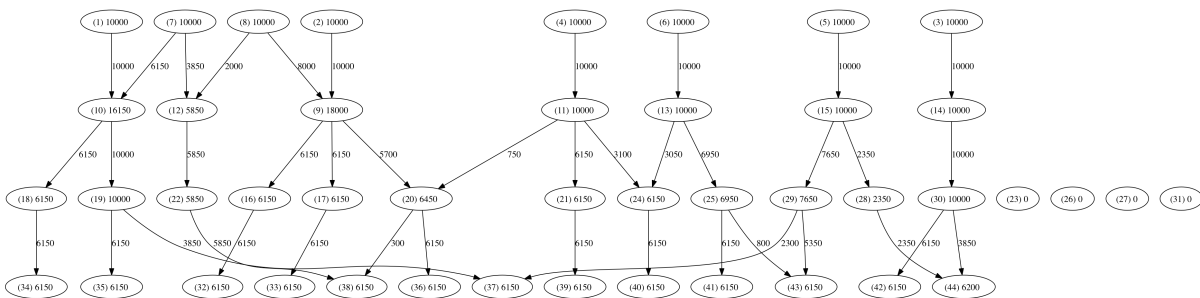


Figure 8: Optimal configuration for the four-stage example obtained minimizing the WCRC index.

Tables

<i>Optimization index</i>	<i>Solution time</i>	<i># of links</i>	<i>BDC</i>	<i>ARC</i>	<i>WCRC</i>
<i>BDC mimimization</i>	92.54	24	10	4,100	6,250
<i>ARC mimimization</i>	47.81	23	10	3,333	5,400
<i>WCRC mimimization</i>	0.59	24	13	3,392	4,000

Table 1. Numerical results of the second example.

<i>Optimization index</i>	<i>Solution time</i>	<i># of links</i>	<i>BDC</i>	<i>ARC</i>	<i>WCRC</i>
<i>BDC mimimization</i>	640,780	41	23	17,694	30,750
<i>WCRC mimimization</i>	2,031	43	31	20,769	24,600

Table 2. Results of the optimization of the four levels problem considering BDC and WCRC optimization criteria