## Improved measurement of the semileptonic decay $D_s^+ \to K^0 e^+ \nu_e$

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Analyzing  $e^+e^-$  collision data corresponding to an integrated luminosity of 7.33 fb<sup>-1</sup> collected at center-of-mass energies between 4.128 and 4.226 GeV with the BESIII detector, we measure the branching fraction of the semileptonic decay  $D_s^+ \to K^0 e^+ \nu_e$  to be  $(2.98 \pm 0.23_{\rm stat} \pm 0.12_{\rm syst}) \times 10^{-3}$ . Based on fit to the partial decay rates in various  $q^2$  intervals, the product value of  $D_s^+ \to K^0$  hadronic form factor and Cabibbo-Kobayashi-Maskawa element is measured to be  $f_+^{K^0}(0)|V_{cd}| = 0.143 \pm 0.011_{\rm stat} \pm 0.003_{\rm syst}$ . With  $|V_{cd}| = 0.22486 \pm 0.00067$  as an input, the hadronic form factor is evaluated to be  $f_+^{K^0}(0) = 0.636 \pm 0.049_{\rm stat} \pm 0.013_{\rm syst}$ . The branching fraction and form factor measurements are factors of 1.6 and 1.7 more precise than the previous world averages, respectively.

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#### I. INTRODUCTION

Studies of semileptonic  $D_s^+$  decays provide important input to understand the effects of the strong and weak interactions in charmed meson decays [1]. The partial decay rates of the semileptonic decays  $D_s^+ \to P \ell^+ \nu_\ell$ (P denotes a pseudoscalar meson) are proportional to the product of the hadronic form factor  $f_{+}^{P}(0)$  and the Cabibbo-Kobayashi-Maskawa (CKM) matrix element  $|V_{cs}|$  or  $|V_{cd}|$ . In recent years, there has been much progress in the experimental study of semileptonic  $D_s^+$  decays. However, knowledge of Cabibbo-suppressed semileptonic  $D_s^+$  decays remains limited by statistical uncertainty [2]. Improved measurements of the branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$ and the hadronic form factor of  $D_s^+ \to K^0$  are important to validate theoretical calculations [3–11]. The hadronic form factor measurement helps test and improve theoretical calculations, which in turn improves the measured precision of  $|V_{cd}|$ . This is important for testing the unitary of the CKM matrix and searching for possible indications of new physics.

Theoretical predictions of the branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$  range from  $2.0 \times 10^{-3}$  to  $4.0 \times 10^{-3}$ . In 2009, the CLEO-c experiment reported the first measurement of the branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$  using  $0.31~{\rm fb}^{-1}$  of  $e^+ e^-$  collision data collected at a

Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP<sup>3</sup>. c.m. energy of 4.17 GeV [12]. In 2015, the CLEO collaboration updated the branching fraction measurement using 0.586 fb<sup>-1</sup> of data at the same energy point [13]. In 2019, the BESIII experiment presented a further improved measurement of the branching fraction and the first measurement of the hadronic form factor in  $D_s^+ \to K^0 e^+ \nu_e$  by analyzing 3.19 fb<sup>-1</sup> of data at 4.178 GeV [14,15].

In this paper, we report improved measurements of both the branching fraction and the hadronic transition form factor in  $D_s^+ \to K^0 e^+ \nu_e$ , where the  $K^0$  is reconstructed as  $K_s^0$  assuming that  $K_s^0$  accounts for 50% of the magnitude and neglecting the CP violation effects in neutral kaon decay. The measurement is performed based on 7.33 fb<sup>-1</sup> of  $e^+e^-$  collision data taken with c.m. energies between 4.128 and 4.226 GeV with the BESIII detector. The c.m. energies for each of the datasets are summarized in the Table I. Throughout this paper, charge conjugate modes are implied.

TABLE I. The c.m. energies and  $M_{\rm BC}$  requirements for various datasets.

Dataset	$E_{\rm c.m.}$ (GeV)	$M_{\rm BC}~({\rm GeV}/c^2)$
1	4.128	[2.010, 2.061]
2	4.157	[2.010, 2.070]
3	4.178	[2.010, 2.073]
4	4.189	[2.010, 2.076]
5	4.199	[2.010, 2.079]
6	4.209	[2.010, 2.082]
7	4.219	[2.010, 2.085]
8	4.226	[2.010, 2.088]

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# II. BESIII DETECTOR AND MONTE CARLO SIMULATIONS

The BESIII detector [16] records symmetric  $e^+e^$ collisions provided by the BEPCII storage ring [17], which operates with a peak luminosity of  $1.1 \times 10^{33}$  cm<sup>-2</sup> s<sup>-1</sup> in the c.m. energy range from 1.84 to 4.95 GeV. BESIII has collected large data samples in this energy region [18]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), all enclosed in a superconducting solenoidal magnet that provides a 1.0 T magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identification modules interleaved with steel. The charged-particle momentum resolution at 1 GeV/c is 0.5%, and the dE/dx resolution is 6% for electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the barrel (end cap) region. The time resolution in the TOF barrel (end cap) region is 68 (110) ps, and the end cap TOF system was upgraded in 2015 using multi-gap resistive plate chamber technology, providing a time resolution of 60 ps [19]. Approximately 83% of the data benefits from this upgrade.

Simulated data samples produced with a Geant4-based [20] Monte Carlo (MC) package, which includes the geometric description of the BESIII detector and the detector response, are used to determine detection efficiencies and to estimate backgrounds. The simulation models the beam energy spread and initial state radiation in the  $e^+e^-$  annihilations with the generator KKMC [21]. In the simulation, the production of open-charm processes directly produced via  $e^+e^-$  annihilations are modeled with the generator CONEXC [22], and their subsequent decays are modeled by EvtGen [23] with known branching fractions from the Particle Data Group (PDG) [2]. The initial state radiation production of vector charmonium (like) states and the continuum processes are incorporated in KKMC [21]. The remaining unknown charmonium decays are modeled with LUNDCHARM [24]. Final state radiation from charged final-state particles is incorporated using the PHOTOS package [25].

#### III. ANALYSIS METHOD

Pairs of  $D_s^{*\pm}D_s^{\mp}$  decaying into  $\gamma D_s^+D_s^-$  are produced copiously in  $e^+e^-$  collisions with c.m. energies between 4.128 and 4.226 GeV. This allows us to study  $D_s^+$  decays using the double-tag (DT) method pioneered by the MARK-III collaboration [26]. The  $D_s^-$  meson, which is fully reconstructed via one of its hadronic decay modes, is referred to as a single-tag (ST)  $D_s^-$  meson. In the presence of a fully reconstructed ST  $D_s^-$  meson at a certain c.m. energy, we can infer the kinematic information of the other

 $D_s^+$  meson. The semileptonic decay  $D_s^+ \to K^0 e^+ \nu$  is thus selected on the side recoiling against the ST  $D_s^-$ , despite the presence of an undetectable neutrino. A DT event is an event in which the transition  $\gamma$  from the  $D_s^{*+}$  and the semileptonic decay  $D_s^+ \to K^0 e^+ \nu_e$  can be successfully selected in the presence of the ST. The branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$  is determined by

$$\mathcal{B}_{D_s^+ \to K^0 e^+ \nu_e} = \frac{N_{\rm DT}}{N_{\rm ST}^{\rm tot} \cdot \bar{\epsilon}_{\gamma \rm SL}},\tag{1}$$

where  $N_{\rm DT} = \sum_{ij} N_{\rm DT}^{ij}$  and  $N_{\rm ST}^{\rm tot} = \sum_{ij} N_{\rm ST}^{ij}$  are the yields of the DT events and ST  $D_s^-$  mesons in data summing over all tag modes i and datasets j, respectively; and  $\bar{e}_{\gamma \rm SL}$  is the efficiency of detecting the  $\gamma$  and the semileptonic decay in the presence of the ST  $D_s^-$  candidate, weighted by the ST yield in data. It is calculated by  $\sum_{ij}[(N_{\rm ST}^{ij}/N_{\rm ST})\cdot(\varepsilon_{\rm DT}^{ij}/\varepsilon_{\rm ST}^{ij})]$ , where  $\varepsilon_{\rm DT}^{ij}$  and  $\varepsilon_{\rm ST}^{ij}$  are the detection efficiencies of the DT and ST candidates, respectively.

#### IV. SINGLE-TAG $D_s^-$ CANDIDATES

The ST  $D_s^-$  candidates are formed using 14 hadronic decay modes:  $D_s^- \to K^+ K^- \pi^-$ ,  $K^+ K^- \pi^- \pi^0$ ,  $\pi^+ \pi^- \pi^-$ ,  $K_S^0 K^-$ ,  $K_S^0 K^- \pi^0$ ,  $K^- \pi^+ \pi^-$ ,  $K_S^0 K_S^0 \pi^-$ ,  $K_S^0 K^+ \pi^- \pi^-$ ,  $K_S^0 K^- \pi^+ \pi^-$ ,  $\eta_{\gamma\gamma} \pi^-$ ,  $\eta_{\gamma\gamma}' \pi^-$ ,  $\eta_{\gamma\gamma}' \pi^+ \pi^- \pi^-$ ,  $\eta_{\gamma\rho}' \pi^-$ , and  $\eta_{\gamma\gamma} \rho^-$ . Throughout this paper, the subscripts on the  $\eta^{(\prime)}$  denote the decay modes that are used to reconstruct the  $\eta^{(\prime)}$  candidates and  $\rho$  denotes  $\rho(770)$ .

In selecting candidates for the  $K^{\pm}$ ,  $\pi^{\pm}$ ,  $K_S^0$ ,  $\gamma$ ,  $\pi^0$ , and  $\eta$ , we use the same selection criteria as those adopted in our previous works [27,28]. All charged tracks, except for those from  $K_S^0$  decays, are required to originate from the interaction point (IP) defined by  $|V_{xy}| < 1$  cm,  $|V_z| < 10$  cm, and  $|\cos\theta| < 0.93$  to ensure reliable main drift chamber measurements, where  $|V_{xy}|$  and  $|V_z|$  are the distances of closest approach to the IP in the transverse plane and along the MDC axis, respectively, and  $\theta$  is the polar angle with respect to the MDC axis. The particle identification (PID) of charged particles is performed with combined dE/dx and TOF information. Those with confidence level for the pion (kaon) hypothesis greater than that for the kaon (pion) hypothesis are assigned to be pion (kaon) candidates.

Candidates for  $K_S^0$  are reconstructed from two oppositely charged tracks satisfying  $|V_z| < 20$  cm because of the long lifetime of the  $K_S^0$  meson. The two charged tracks are assigned as  $\pi^+\pi^-$  without imposing further PID criteria. They are constrained to originate from a common vertex and are required to have an invariant mass within  $|M_{\pi^+\pi^-} - m_{K_S^0}| < 12 \text{ MeV}/c^2$ , where  $m_{K_S^0}$  is the  $K_S^0$  nominal mass [2]. The decay length of the  $K_S^0$  candidate is required to be greater than twice the vertex resolution away

from the IP to suppress the combinatorial backgrounds of  $\pi^+\pi^-$  originated from the non- $K_S^0$  decay.

Photon candidates are selected using information measured by the EMC and are required to satisfy the following criteria. To suppress backgrounds from electronic noise or bremsstrahlung, any candidate shower is required to start within [0, 700] ns from the event start time. The energy of each shower in the barrel (end cap) region of the EMC [16] is required to be greater than 25 (50) MeV. To suppress backgrounds associated with charged tracks, the minimum opening angle between the momentum of the candidate shower and the extrapolated momentum direction of the nearest charged track at the EMC has to be greater than 10°.

Candidates for  $\pi^0$  and  $\eta_{\gamma\gamma}$  are formed from  $\gamma\gamma$  pairs with invariant masses in the mass intervals (0.115, 0.150) and (0.50, 0.57) GeV/ $c^2$ , respectively. To improve momentum resolution, the invariant mass of each selected  $\gamma\gamma$  pair is constrained to either the  $\pi^0$  or  $\eta$  nominal mass [2]. To form candidates for  $\rho^{0(+)}$ ,  $\eta_{\pi^0\pi^+\pi^-}$ ,  $\eta'_{n\pi^+\pi^-}$ , and  $\eta'_{\gamma\rho^0}$ ,

the invariant masses of the  $\pi^+\pi^{-(0)}$ ,  $\pi^0\pi^+\pi^-$ ,  $\eta\pi^+\pi^-$ , and  $\gamma\rho^0$  combinations are required to be within the mass intervals of (0.57, 0.97), (0.53, 0.57), (0.946, 0.970), and (0.940, 0.976) GeV/ $c^2$ , respectively. These mass intervals correspond to approximately  $\pm 3$  times of the standard deviations around the peaks of the reconstructed particles. In addition, to suppress the backgrounds from  $D^*$  decays, the momenta of the photon from  $\eta' \to \gamma\rho$  and all pions are required to be greater than 0.1 GeV/c.

The backgrounds from non- $D_s^{\pm}D_s^{*\mp}$  processes are suppressed with the beam-constrained mass of the ST  $D_s^-$  candidate, which is defined as

$$M_{\rm BC} \equiv \sqrt{E_{\rm beam}^2/c^4 - |\vec{p}_{\rm tag}|^2/c^2},$$
 (2)

where  $E_{\text{beam}}$  is the beam energy and  $\vec{p}_{\text{tag}}$  is the momentum of the ST  $D_s^-$  candidate in the  $e^+e^-$  c.m. frame. The  $M_{\text{BC}}$  is required to be within the intervals shown in Table I. This requirement retains 90% of the  $D_s^-$  and  $D_s^+$  mesons from  $e^+e^- \to D_s^{*\mp}D_s^{\pm}$ .

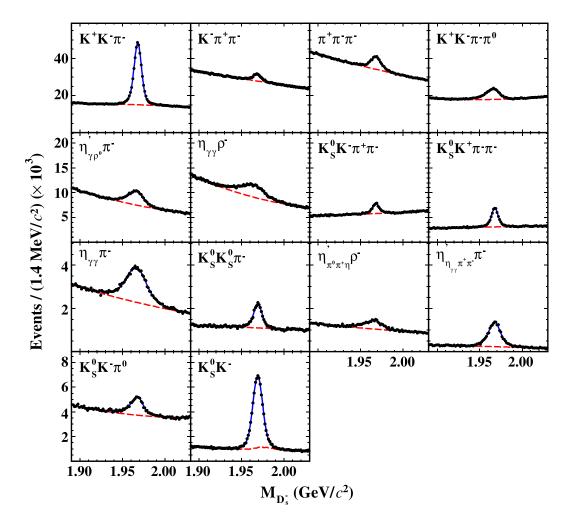


FIG. 1. Fits to the  $M_{D_s^-}$  distributions of the ST candidates for various tag modes. The points with error bars are data; the blue solid curves are the best fit results; and the red dashed curves are the fitted background shapes.

In the case of multiple candidates, only the candidate with the  $D_s^-$  recoil mass

$$M_{\rm rec} \equiv \sqrt{\left(E_{\rm c.m.}/c^2 - \sqrt{|\vec{p}_{\rm tag}|^2/c^2 + m_{D_s^-}^2}\right)^2 - |\vec{p}_{\rm tag}|^2/c^2}$$
(3)

closest to the  $D_s^{*+}$  nominal mass [2] per tag mode is retained for further analysis. The distributions of the invariant mass  $(M_{tag})$  of the accepted ST candidates for various tag modes are shown in Fig. 1. The yields of ST  $D_s^$ mesons reconstructed in various tag modes are derived from fits to individual  $M_{\text{tag}}$  distributions and are listed in Table II. In the fits, the signals are described by the simulated signal shapes convolved with Gaussian functions to incorporate the possible resolution differences between data and simulation, where the widths of the convolved Gaussian functions range from  $(0.6 \pm 0.2) \text{ MeV}/c^2$  to  $(3.5 \pm 1.3) \text{ MeV}/c^2$  for different ST modes. The combinatorial background is described by a second-order Chebychev polynomial function and has been verified with the inclusive MC sample. For the  $D_s^- \to K_S^0 K^-$  tag, the broad peaking background from  $D^- \to K_S^0 \pi^-$  is modeled using the simulated shape and the size of this background relative to other combinatorial ones is fixed. Figure 1 shows the results of the fit to the data sample. For each tag mode, the ST yield is obtained by integrating the signal shape over the selected  $D_s^-$  signal region defined within  $1.94 < M_{D_s^-} < 1.99 \text{ GeV}/c^2$ . The second and third columns of Table II summarize the yields of ST  $D_s^-$  mesons  $(N_{\rm ST})$  for various tag modes obtained from the data sample and the corresponding detection efficiencies ( $\epsilon_{ST}$ ), respectively. The total ST yield summed over all ST modes is  $N_{\rm ST}^{\rm tot} = (783.1 \pm 2.5) \times 10^{-3}$ , where the uncertainty is statistical only.

### V. SELECTION OF $D_s^+ \to K^0 e^+ \nu_e$

In the system recoiling against the  $D_s^-$  tag and the transition  $\gamma$  from the  $D_s^{*-}$ , the semileptonic decay  $D_s^+ \rightarrow K^0 e^+ \nu_e$  is selected using tracks that have not been used for the single tag reconstruction. To identify positrons, the combined confidence levels  $CL'_e$ ,  $CL'_\pi$ , and  $CL'_K$  for the electron, pion, and kaon hypotheses are calculated with the dE/dx, TOF, and EMC information. The positron candidates are required to satisfy  $CL'_e > 0.001$  and  $CL'_e/(CL'_e + CL'_\pi + CL'_K) > 0.8$ .

Due to the misidentifications between charged kaons and positrons, the background from  $D_s^+ \to K^0 K^+$  can be reconstructed as  $D_s^+ \to K^0 e^+ \nu_e$ . This background is vetoed by requiring the invariant mass of  $K^0 e^+$  to be less than 1.78 GeV/ $c^2$ . The background contributions from  $D_s^+$  hadronic decays associated with fake photons misidentified from showers are rejected by requiring the largest energy of

the unused showers  $(E_{\rm extray}^{\rm max})$  to be less than 0.2 GeV. The DT candidate is rejected if additional charged tracks  $(N_{\rm extra}^{\rm charge})$  is detected.

To identify the transition  $\gamma$  produced directly from the  $D_s^{*\pm}$ , we perform kinematic fits under two hypotheses. One assumes that the  $D_s^{*-}$  is formed by the transition  $\gamma$  and the ST  $D_s^-$ , and the other assumes that the  $D_s^{*+}$  is formed by the transition  $\gamma$  and the semileptonic decay. The final particles from the  $D_s^{\pm}D_s^{*\pm}$  system are constrained to obey energy and momentum conservation in the  $e^+e^-$  c.m. frame with the neutrino treated as a missing particle. The particle candidates for  $D_s^{\pm}$  are constrained to their known mass from the PDG [2]. For the former hypothesis, the mass of the transition  $\gamma$  and the tagged  $D_s^-$  is constrained to the known  $D_s^{*-}$  mass. For the latter hypothesis, the mass of the transition  $\gamma$  and the semileptonic decay is constrained to the known  $D_s^{*+}$  mass. The hypothesis with the smallest  $\chi^2$ of the kinematic fit  $(\chi^2_{KMFIT})$ , which also satisfies  $\chi^2_{\rm KMFIT}$  < 100, is kept for further analysis.

The presence of the neutrino is inferred from the distribution of the missing-mass squared variable, which is defined as

$$M_{\text{miss}}^2 = E_{\text{miss}}^2/c^4 - |\vec{p}_{\text{miss}}|^2/c^2.$$
 (4)

Here,  $E_{\text{miss}} = E_{\text{c.m.}} - \Sigma_i E_i$  and  $\vec{p}_{\text{miss}} = \Sigma_i \vec{p}_i$ , where  $E_i$  and  $\vec{p}_i$ , with  $i = (\text{tag}, \gamma, e, \text{ and } K^0)$ , are the energy and momentum of particle i.

The  $M_{\rm miss}^2$  distribution of the accepted candidates for  $D_s^+ \to K^0 e^+ \nu_e$  in data summed over all c.m. energies is shown in Fig. 2. The signal yield of  $D_s^+ \to K^0 e^+ \nu_e (N_{\rm DT})$  is

TABLE II. Fitted yields of single-tag  $D_s^-$  mesons from the data sample  $(N_{\rm ST})$ , the efficiencies of detecting single-tag  $D_s^-$  mesons and double-tag events  $(\epsilon_{\rm ST}$  and  $\epsilon_{\rm DT})$  for various tag modes. For all quantities, the uncertainties are statistical only. The listed efficiencies do not include the branching fractions of the daughter particles's decays.

Tag mode	$N_{\rm ST}~(\times 10^3)$	ε <sub>ST</sub> (%)	ε <sub>DT</sub> (%)
$K^+K^-\pi^-$	$281.7 \pm 0.8$	$41.94 \pm 0.03$	$10.92 \pm 0.11$
$K^{+}K^{-}\pi^{-}\pi^{0}$	$85.4 \pm 1.0$	$11.53 \pm 0.03$	$3.39 \pm 0.12$
$\pi^-\pi^+\pi^-$	$76.9 \pm 1.0$	$53.84 \pm 0.06$	$15.28 \pm 0.11$
$K_S^0K^-$	$63.2 \pm 0.3$	$47.18 \pm 0.06$	$12.73\pm0.11$
$K_S^0 K^- \pi^0$	$21.9 \pm 0.5$	$16.56 \pm 0.08$	$4.81 \pm 0.12$
$K^-\pi^+\pi^-$	$36.8 \pm 0.8$	$47.06 \pm 0.08$	$12.78 \pm 0.11$
$K_S^0K_S^0\pi^-$	$10.6\pm0.2$	$22.92 \pm 0.13$	$5.82 \pm 0.12$
$K_S^0K^+\pi^-\pi^-$	$30.5 \pm 0.3$	$21.48 \pm 0.07$	$5.48 \pm 0.12$
$K_S^0 K^- \pi^+ \pi^-$	$16.4 \pm 0.4$	$19.21\pm0.10$	$4.74 \pm 0.12$
$\eta\pi^-$	$33.7 \pm 0.6$	$40.43 \pm 0.08$	$12.54 \pm 0.11$
$\eta'(\pi^+\pi^-\eta) ho^-$	$7.2 \pm 0.3$	$5.62 \pm 0.08$	$1.83 \pm 0.11$
$\eta'(\eta\pi^+\pi^-)\pi^-$	$15.6 \pm 0.2$	$19.20 \pm 0.10$	$5.45 \pm 0.12$
$\eta'(\gamma\rho)\pi^-$	$47.3 \pm 0.7$	$30.94 \pm 0.07$	$8.77 \pm 0.11$
$\eta \rho^-$	$56.0\pm1.2$	$14.35 \pm 0.04$	$5.02 \pm 0.12$

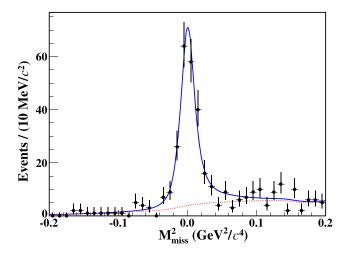


FIG. 2. Fit to the  $M_{\rm miss}^2$  distribution of the candidates for  $D_s^+ \to K^0 e^+ \nu_e$ . The points with error bars are the data summed over all c.m. energies, the blue solid curve is the total fit, and the red dashed curve is the fitted background shape.

derived from an unbinned maximum likelihood fit to this distribution. In this fit, the signal is described by a simulated signal shape convolved with a Gaussian function, where the width of the Gaussian function is  $(0.5\pm0.3)\times10^{-3}~{\rm GeV^2}/c^4$  determined from the fit. The background is described by a simulated shape derived from the inclusive MC sample. From this fit, the signal yield is  $225.3\pm17.3$  where the uncertainty is statistical only. The corresponding DT efficiencies  $\epsilon_{\rm DT}^i$  of various ST are summarized in the fourth column of Table II.

#### VI. BRANCHING FRACTION

The detection efficiency  $\varepsilon_{\rm SL}$ , which does not include the branching fraction of  $K^0 \to K^0_S \to \pi^+\pi^-$ , is estimated to be  $(27.88 \pm 0.21)\%$  for  $D^+_s \to K^0 e^+ \nu_e$ . Figure 3 shows good consistency in the  $\cos\theta$  and momenta distributions for the  $K^0$  and  $D^+_s \to K^0 e^+ \nu_e$  candidates between data and the inclusive MC sample. The branching fraction of  $D^+_s \to K^0 e^+ \nu_e$  is determined by Eq. (1) to be

$$\mathcal{B}(D_s^+ \to K^0 e^+ \nu_e) = (2.98 \pm 0.23 \pm 0.12) \times 10^{-3},$$

where the first uncertainty is statistical and the second is systematic, which is discussed below and summarized in Table III.

Our measurement is performed using the DT technique [26], and most systematic uncertainties related to the ST selection criteria therefore cancel. The systematic uncertainty of the ST  $D_s^-$  yields is evaluated to be 1.0% by using alternative signal and background shapes in the fits to the  $M_{\rm tag}$  spectra. The systematic uncertainty for the  $e^\pm$  tracking and PID efficiency is 1.0% each and is studied using a control sample of  $e^+e^- \rightarrow \gamma e^+e^-$  [29]. The systematic uncertainty in the  $K_s^0$  reconstruction efficiency is estimated

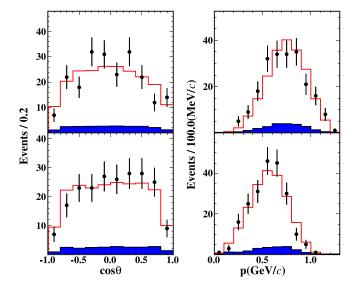


FIG. 3. Comparison of  $\cos\theta$  and momenta for the  $K^0$  (top) and candidates for  $D_s^+ \to K^0 e^+ \nu_e$  (bottom) using all c.m. energies between 4.128 and 4.226 GeV. The points with error bars are data, the blue filled histograms are the simulated background, and the red line histograms are the inclusive MC samples. These events have been required to satisfy  $|M_{\rm miss}^2| < 0.03~{\rm GeV^2}/c^4$ .

with the control samples  $J/\psi \to K^*(892)^{\mp}K^{\pm}$  and  $J/\psi \rightarrow \phi K_S^0 K^{\pm} \pi^{\mp}$  [30] and is determined to be 1.5% per  $K_s^0$ . The systematic uncertainty of the transition  $\gamma$ reconstruction [31], which is weighted by the branching fraction of  $D_s^{*+} \rightarrow \gamma D_s^+$ , is assigned to be 1.0%. For requirements on  $E_{\mathrm{extray}}^{\mathrm{max}}$  and  $N_{\mathrm{extra}}^{\mathrm{charge}}$  and  $\chi_{\mathrm{KMFIT}}^{2}$ , their systematic uncertainties are studied using control samples  $D_s^+ \to K_S^0 K^+$  and  $D_s^+ \to K_S^0 K^+ \pi^0$ , where the accepted efficiencies of the  $E_{\rm extray}^{\rm max}$ ,  $N_{\rm extra}^{\rm charge}$ , and  $\chi_{\rm KMFIT}^2$  requirements are evaluated for both data and MC samples. Then the differences of the accepted efficiencies between data and MC samples, 0.8% for  $E_{\rm extray}^{\rm max}$  and  $N_{\rm extra}^{\rm charge}$  and 2.3% for  $\chi^2_{\mathrm{KMFIT}}$ , are assigned as their systematic uncertainties. The systematic uncertainty due to the different tag dependence between data and MC simulation, called the tag bias [29], is estimated to be 0.2%. The systematic uncertainty due to the quoted branching fraction of  $K^0 \to K_S^0 \to \pi^+\pi^-$  is evaluated as 0.2% [2], which incorporates a 0.2% uncertainty because of the negligence of the possible CP violations in neutron kaon decays. The systematic uncertainty arising from the fit to the  $M_{\rm miss}^2$  distribution is estimated to be 0.9% by varying the signal and background shapes. The uncertainty due to MC statistics is 0.2%. Systematic uncertainty due to the uncertainty on the form factor used in the MC simulation to determine the efficiency is estimated to be 1.4%. This is evaluated by comparing the difference of the signal efficiencies when varying the input hadronic form factor parameter by  $\pm 1\sigma$ , as determined in this work listed in Table VIII. Adding these effects in quadrature, we obtain

TABLE III. Sources of systematic uncertainties in the branching fraction measurement.

Source	Uncertainty (%)
Single-tag yield	1.0
$e^+$ tracking	1.0
$e^+$ PID	1.0
$K_S^0$ reconstruction	1.5
Transition $\gamma$ reconstruction	1.0
$E_{\text{extra}\gamma}^{\text{max}}$ and $N_{\text{extra}}^{\text{charge}}$ requirements	0.8
$\chi^2_{\rm KMFIT}$ requirement	2.3
Tag bias	0.2
Quoted branching fraction	0.2
$M_{\rm miss}^2$ fit	0.9
MC statistics	0.2
Hadronic form factor	1.4
Total	3.9

the total systematic uncertainty on the measurement of the branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$  to be 3.9%. A summary of the systematic uncertainties for the branching fraction is shown in Table III.

#### VII. HADRONIC FORM FACTOR

To study the decay dynamics of the semileptonic decay  $D_s^+ \to K^0 e^+ \nu_e$ , candidates are divided according to the invariant mass squared of the  $e^+ \nu_e$  system  $(q^2 = (E_e/c + E_\nu/c)^2 + |\vec{p}_e + \vec{p}_\nu|^2)$  into five intervals (0.00, 0.35], (0.35, 0.70], (0.70, 1.05], (1.05, 1.40], and

(1.40, 2.16) GeV<sup>2</sup>/ $c^4$ . The partial decay rate in the *i*th  $q^2$  interval,  $\Delta\Gamma^i_{\rm measured}$ , is determined by

$$\Delta\Gamma_{\text{measured}}^{i} = N_{\text{produced}}^{i} / (\tau_{D_{s}^{+}} \mathcal{B}_{K^{0} \to \pi^{+} \pi^{-}} N_{\text{ST}}^{\text{tot}}), \qquad (5)$$

where  $N_{\rm produced}^i$  is the  $D_s^+ \to K^0 e^+ \nu_e$  signal yield produced in the ith  $q^2$  interval in data,  $\tau_{D_s^+}$  is the lifetime of the  $D_s^+$  [2], and  $N_{\rm ST}^{\rm tot}$  is the total yield of ST  $D_s^-$  mesons. The number of events produced in data is calculated as

$$N_{\text{produced}}^{i} = \sum_{j}^{N_{\text{intervals}}} (\varepsilon^{-1})_{ij} N_{\text{observed}}^{j}, \tag{6}$$

where  $N_{\text{observed}}^{j}$  is the  $D_s^+ \to K^0 e^+ \nu_e$  signal yield observed in the *j*th  $q^2$  interval and  $\varepsilon$  is the efficiency matrix, which also includes the effects of bin migration, given by

$$\varepsilon_{ij} = \sum_{k} \left[ (N_{\text{reconstructed}}^{ij} \cdot N_{\text{ST}}) / (N_{\text{generated}}^{j} \cdot \varepsilon_{\text{ST}}) \right]_{k} / N_{\text{ST}}^{\text{tot}}. \tag{7}$$

Here,  $N_{\rm reconstructed}^{ij}$  is the  $D_s^+ \to K^0 e^+ \nu_e$  signal yield generated in the jth  $q^2$  interval and reconstructed in the ith  $q^2$  interval,  $N_{\rm generated}^j$  is the total signal yield generated in the jth  $q^2$  interval, and the index k sums over all tag modes and energies.

The signal yield  $N_{\text{observed}}^i$  in each  $q^2$  interval is obtained from the fit to the corresponding  $M_{\text{miss}}^2$  distribution, and is shown in Fig. 4. The efficiency matrix for  $D_s^+ \to K^0 e^+ \nu_e$  is

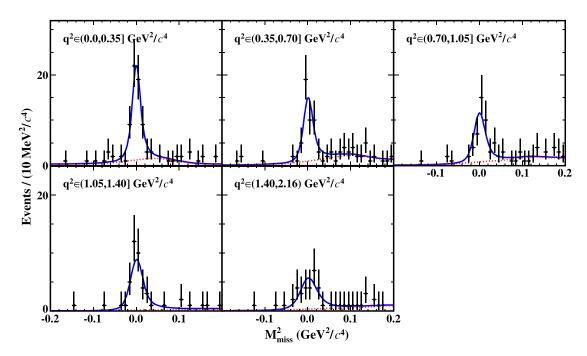


FIG. 4. Fits to the  $M_{\text{miss}}^2$  distributions of  $D_s^+ \to K^0 e^+ \nu_e$  in various reconstructed  $q^2$  intervals. The points with error bars are the data summed over all c.m. energies, the blue solid curves are the best fits, and the red dashed curves are the fitted background shapes.

TABLE IV. Efficiency matrix (in %) for  $D_s^+ \to K^0 e^+ \nu_e$ . The efficiencies do not include the branching fractions of the decays of the daughter particles.

$\overline{(i,j)q^2}$ interval	1	2	3	4	5
1	26.80	0.83	0.00	0.00	0.00
2	0.93	27.62	0.74	0.02	0.00
3	0.00	0.91	27.09	0.64	0.00
4	0.00	0.00	0.83	26.12	0.41
5	0.00	0.00	0.00	0.70	25.56

shown in Table IV. The values for  $N^j_{\text{observed}}, N^j_{\text{produced}}, \Delta \Gamma_j$ , and  $\frac{\Delta \Gamma_j}{\Delta q_i^2}$  are summarized in Table V.

Using the values of  $\Delta\Gamma^i_{\rm measured}$  obtained above and the theoretical parametrization of the partial decay rate  $\Delta\Gamma^i_{\rm expected}$  described below, form factor parameters are extracted by a  $\chi^2$  fit where the  $\chi^2$  is constructed as

$$\chi^{2} = \sum_{i,j=1}^{5} (\Delta \Gamma_{\text{measured}}^{i} - \Delta \Gamma_{\text{expected}}^{i}) C_{ij}^{-1} \times (\Delta \Gamma_{\text{measured}}^{j} - \Delta \Gamma_{\text{expected}}^{j}), \tag{8}$$

where  $C_{ij} = C_{ij}^{\rm stat} + C_{ij}^{\rm syst}$  is the covariance matrix of the measured partial decay rates among  $q^2$  intervals. The differential decay rate is given by

$$\frac{d\Gamma(D_s^+ \to K^0 e^+ \nu_e)}{dq^2} = \frac{G_F^2 |V_{cd}|^2}{24\pi^3} p_{K^0}^3 |f_+^{K^0}(q^2)|^2, \quad (9)$$

where  $p_{K^0}$  is the  $K^0$  momentum in the rest frame of the  $D_s^+$ ,  $G_F$  is the Fermi coupling constant [2],  $|V_{cd}|$  is the  $c \to d$  CKM matrix element, and  $f_+^{K^0}(q^2)$  is the hadronic form factor. The scalar hadronic form factor  $f_0^{K^0}(q^2)$  has been ignored because it is proportional to the positron mass squared

The hadronic form factor,  $f_{+}^{K^0}(q^2)$ , is usually parametrized by the simple pole model, modified pole model, or series expansion. In the modified pole model [32],

TABLE VI. The statistical correlation coefficients of the measured partial decay rate in each  $q^2$  bin for  $D_s^+ \to K^0 e^+ \nu_e$ .

$\epsilon_{ij}$	1	2	3	4	5
1	1.000	-0.065	0.003	-0.000	0.000
2	-0.065	1.000	-0.060	0.003	-0.000
3	0.003	-0.060	1.000	-0.057	0.002
4	-0.000	0.003	-0.057	1.000	-0.044
5	0.000	-0.000	0.020	-0.044	1.000

TABLE VII. The systematic correlation coefficients of the measured partial decay rate in each  $q^2$  bin for  $D_s^+ \to K^0 e^+ \nu_e$ .

$\epsilon_{ij}$	1	2	3	4	5
1	1.000	0.920	0.814	0.952	0.590
2	0.920	1.000	0.816	0.844	0.706
3	0.814	0.816	1.000	0.782	0.893
4	0.952	0.844	0.782	1.000	0.519
5	0.590	0.706	0.893	0.519	1.000

$$f_{+}^{K^{0}}(q^{2}) = \frac{f_{+}^{K^{0}}(0)}{\left(1 - \frac{q^{2}}{M_{\text{pole}}^{2}}\right)\left(1 - \alpha \frac{q^{2}}{M_{\text{pole}}^{2}}\right)},\tag{10}$$

where  $M_{\rm pole}$  is fixed to the known  $D^{*+}$  mass and  $\alpha$  is a free parameter. Setting  $\alpha=0$  and leaving  $M_{\rm pole}$  free, the simple pole model is recovered [33]. Due to limited statistics, we adopt the two parameter series expansion form, which is written as

$$f_{+}^{K^{0}}(q^{2}) = \frac{f_{+}^{K^{0}}(0)P(0)\Phi(0,t_{0})}{P(q^{2})\Phi(q^{2},t_{0})} \cdot \frac{1 + r_{1}(t_{0})z(q^{2},t_{0})}{1 + r_{1}(t_{0})z(0,t_{0})}, \quad (11)$$

where  $t_0 = t_+(1 - \sqrt{1 - t_-/t_+})$ ,  $t_\pm = (m_{D_s^+} \pm m_{K^0})^2$ , and the functions  $P(q^2)$ ,  $\Phi(q^2, t_0)$ , and  $z(q^2, t_0)$  are defined following Ref. [33].

The statistical covariance matrix is constructed as

$$C_{ij}^{\text{stat}} = \left(\frac{1}{\tau_{D_{\text{obs}}^{+}} \cdot N_{\text{ST}}^{\text{tot}}}\right)^{2} \sum_{n} \varepsilon_{\text{in}}^{-1} \varepsilon_{jn}^{-1} (\sigma(N_{\text{obs}}^{n}))^{2}, \quad (12)$$

where n labels the  $q^2$  interval and the sum extends from 1 to 5. The systematic covariance matrix is obtained by

TABLE V. Partial decay rates of  $D_s^+ \to K^0 e^+ \nu_e$  in various  $q^2$  intervals of data, where the uncertainties are statistical only.

$q^2$ interval	(0.0, 0.35]	(0.35, 0.70]	(0.70, 1.05]	(1.05, 1.40]	(1.40, 2.16]
$N_{ m observed}^{j}$	$60.7 \pm 8.7$	$50.8 \pm 8.1$	$46.1 \pm 7.8$	$40.0 \pm 6.7$	$30.2 \pm 6.5$
$N_{ m produced}^i$	$221.1\pm32.5$	$172.2\pm29.4$	$169.9 \pm 28.9$	$146.2\pm26.5$	$114.1\pm25.4$
$\Delta\Gamma_i$ (ns <sup>-1</sup> )	$1.62 \pm 0.24$	$1.26 \pm 0.22$	$1.18 \pm 0.21$	$1.07\pm0.19$	$0.84 \pm 0.19$
$\frac{\Delta \Gamma_i}{\Delta q_i^2}$ (ns <sup>-1</sup> GeV <sup>-2</sup> $c^4$ )	$4.63 \pm 0.68$	$3.60 \pm 0.62$	$3.37 \pm 0.60$	$3.06 \pm 0.55$	$1.10 \pm 0.24$

TABLE VIII. Hadronic form factors of  $D_s^+ \to K^0 e^+ \nu_e$ , where the first uncertainties are statistical and the second systematic. The parameter for the two-parameter z series expansion is  $r_1$  and the coefficient between the two fitted parameters is given in the fourth column. The  $\chi^2$ /n.d.o.f. is the goodness of fit and n.d.o.f. is the number of degrees of freedom.

Parametrization	$f_+^{K^0}(0) V_{cd} $	Parameter $(M_{\text{pole}}^2/\alpha/r_1)$	Coefficient	$\chi^2$ /n.d.o.f.	$f_{+}^{K^0}(0)$
Simple pole [32]	$0.147 \pm 0.009 \pm 0.001$	$1.75 \pm 0.09 \pm 0.03$	0.72	0.96/3	$0.654 \pm 0.040 \pm 0.004$
Modified pole [32]	$0.144 \pm 0.010 \pm 0.002$	$0.57 \pm 0.25 \pm 0.08$	-0.81	0.93/3	$0.640 \pm 0.044 \pm 0.009$
z series (two par.) [33]	$0.143 \pm 0.011 \pm 0.003$	$-3.7 \pm 1.5 \pm 0.5$	0.85	0.97/3	$0.636 \pm 0.049 \pm 0.013$

summing over the covariance matrix of each systematic uncertainty source. This is taken as

$$C_{ij}^{\text{syst}} = \delta(\Delta \Gamma_{\text{measured}}^{i}) \delta(\Delta \Gamma_{\text{measured}}^{j}), \tag{13}$$

where  $\delta(\Delta\Gamma_{\rm measured}^i)$  is the systematic uncertainty of the partial decay rate in the ith  $q^2$  interval. The systematic uncertainties due to  $\tau_{D_s^+}$ ,  $N_{\rm ST}^{\rm tot}$ ,  $e^+$  tracking efficiency,  $e^+$  PID efficiency,  $K_s^0$  reconstruction efficiency, transition  $\gamma$  reconstruction,  $E_{\rm extray}^{\rm max}$  and  $N_{\rm extra}^{\rm charge}$  requirements,  $\chi^2_{\rm KMFIT}$  requirement, tag bias and quoted branching fraction are taken to be common across all the  $q^2$  intervals. The systematic uncertainties due to  $M_{\rm miss}^2$  fit, MC statistics, and hadronic form factor are determined separately in various  $q^2$  intervals. The total systematic uncertainties of the measured partial decay rates in  $q^2$  intervals from 1 to 5 are evaluated to be 3.93%, 4.00%, 4.51%, 3.84%, and 6.03%, respectively. The resulting statistical and systematic correlation coefficients are summarized in Tables VI and VII, respectively.

Minimizing the  $\chi^2$  constructed in Eq. (8), we obtain the product,  $f_+^{K^0}(0)|V_{cd}|$ , and the parameters of various hadronic form factor parametrizations. The obtained results are summarized in Table VIII and the fit results are shown in Fig. 5. The nominal fit parameters are taken from the fit with the combined statistical and systematic covariance

matrix, and their statistical uncertainties are taken from the fit with the statistical covariance matrix. For each parameter, the systematic uncertainty is obtained by calculating the quadratic difference of uncertainties between these two fits. Taking the CKM matrix element  $|V_{cd}|=0.22486\pm0.00067$  [2] as input, we obtain  $f_+^{K^0}(0)$  as summarized in the last column of Table VIII, where the first uncertainties are statistical and the second are systematic.

#### **VIII. SUMMARY**

In summary, using 7.33 fb<sup>-1</sup> of  $e^+e^-$  collision data taken between 4.128 and 4.226 GeV with the BESIII detector, the branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$  is measured to be  $(2.98 \pm 0.23 \pm 0.12) \times 10^{-3}$ , where the first uncertainty is statistical and the second is the systematic. To measure the hadronic form factor at maximum recoil in  $D_s^+ \to K^0 e^+ \nu_e$ , we use the two parameter z series expansion. Based on fit to partial decay rates in various  $q^2$  intervals, we measure  $f_+^{K^0}(0)|V_{cd}|=0.143\pm0.011\pm0.003$ , and  $f_+^{K^0}(0)=0.636\pm0.049\pm0.013$  with  $|V_{cd}|=0.22486\pm0.00067$  [2] as an input. Figure 6 compares the measured branching fraction and the hadronic form factor in  $D_s^+ \to K^0 e^+ \nu_e$  with theoretical calculations and other experiments. The precision of the measurements are improved by factors of 1.6 and 1.7, respectively, compared to the previous BESIII result [14]. The results can test various theoretical calculations.

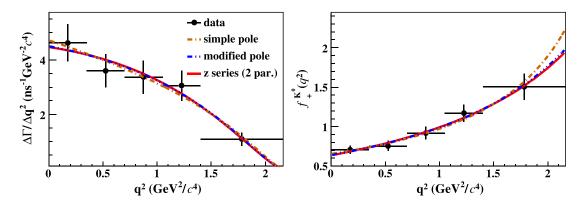
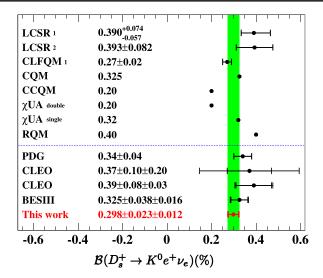


FIG. 5. Left: fit to the partial decay rates of  $D_s^+ \to K^0 e^+ \nu_e$ . Right: projection to the hadronic form factor as a function of  $q^2$ . The points with error bars are the measured partial decay rates, where the horizonal and vertical errors represent the  $q^2$  bin interval and the error of the corresponding partial decay width, respectively. The solid red curves are the best fits.



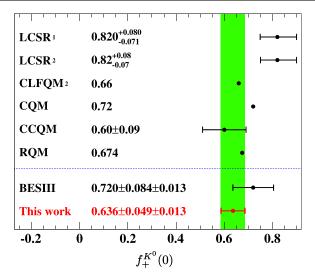


FIG. 6. Comparison of the measured branching fraction of  $D_s^+ \to K^0 e^+ \nu_e$  (left) and the hadronic form factor (right) of  $D_s^+ \to K^0$  with theoretical calculations and other experiments, where the bands show uncertainties of this measurements. The data in the comparison come from LCSR<sub>1</sub> [3], LCSR<sub>2</sub> [4], CLFQM<sub>1</sub> [5], CLFQM<sub>2</sub> [6], CQM [7], CCQM [8,9],  $\chi^{\text{UA}_{\text{double pole}}}$  [10],  $\chi^{\text{UA}_{\text{single pole}}}$  [10], RQM [11], PDG [2], CLEO [13], and BESIII [14].

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<sup>[1]</sup> H. B. Li and X. R. Lyu, Natl. Sci. Rev. 8, nwab181 (2021).

<sup>[2]</sup> R. L. Workman *et al.* (Particle Data Group), Prog. Theor. Exp. Phys. **2022**, 083C01 (2022).

<sup>[3]</sup> Y. L. Wu, M. Zhong, and Y. B. Zuo, Int. J. Mod. Phys. A **21**, 6125 (2006).

<sup>[4]</sup> X. Leng, X. L. Mu, Z. T. Zou, and Ying Li, Chin. Phys. C 45, 063107 (2021).

<sup>[5]</sup> H. Y. Cheng and X. W. Kang, Eur. Phys. J. C 77, 587 (2017); 77, 863(E) (2017).

<sup>[6]</sup> R. C. Verma, J. Phys. G 39, 025005 (2012).

<sup>[7]</sup> D. Melikhov and B. Stech, Phys. Rev. D 62, 014006 (2000).

<sup>[8]</sup> N. R. Soni, M. A. Ivanov, J. G. Körner, J. N. Pandya, P. Santorelli, and C. T. Tran, Phys. Rev. D 98, 114031 (2018).

- [9] M. A. Ivanov, J. G. Körner, J. N. Pandya, P. Santorelli, N. R. Soni, and C. T. Tran, Front. Phys. (Beijing) 14, 64401 (2019).
- [10] S. Fajfer and J. Kamenik, Phys. Rev. D 71, 014020 (2005).
- [11] R. N. Faustov, V. O. Galkin, and X. W. Kang, Phys. Rev. D **101**, 013004 (2020).
- [12] J. Yelton et al. (CLEO Collaboration), Phys. Rev. D 80, 052007 (2009).
- [13] J. Hietala, D. Cronin-Hennessy, T. Pedlar, and I. Shipsey, Phys. Rev. D 92, 012009 (2015).
- [14] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. 122, 061801 (2019).
- [15] B. C. Ke, J. Koponen, H. B. Li, and Y. Zheng, Annu. Rev. Nucl. Part. Sci. 73, 285 (2023).
- [16] M. Ablikim et al. (BESIII Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 614, 345 (2010).
- [17] C. H. Yu et al., Proceedings of IPAC2016, Busan, Korea (JACoW, Geneva, Switzerland, 2016), 10.18429/JACoW-IPAC2016-TUYA01.
- [18] M. Ablikim et al. (BESIII Collaboration), Chin. Phys. C 44, 040001 (2020).
- [19] X. Li *et al.*, Radiat. Detect. Technol. Methods 1, 13 (2017);
   Y. X. Guo *et al.*, Radiat. Detect. Technol. Methods 1, 15 (2017);
   P. Cao *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A 953, 163053 (2020).

- [20] S. Agostinelli et al. (GEANT4 Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
- [21] S. Jadach, B. F. L. Ward, and Z. Was, Phys. Rev. D **63**, 113009 (2001); Comput. Phys. Commun. **130**, 260 (2000).
- [22] R. G. Ping, Chin. Phys. C 38, 083001 (2014).
- [23] D. J. Lange, Nucl. Instrum. Methods Phys. Res., Sect. A 462, 152 (2001); R. G. Ping, Chin. Phys. C 32, 599 (2008).
- [24] J. C. Chen, G. S. Huang, X. R. Qi, D. H. Zhang, and Y. S. Zhu, Phys. Rev. D 62, 034003 (2000); R. L. Yang, R. G. Ping, and H. Chen, Chin. Phys. Lett. 31, 061301 (2014).
- [25] E. Richter-Was, Phys. Lett. B 303, 163 (1993).
- [26] R. M. Baltrusaitis *et al.* (MARK III Collaboration), Phys. Rev. Lett. **56**, 2140 (1986); **60**, 89 (1988).
- [27] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. 122, 121801 (2019).
- [28] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D 99, 072002 (2019).
- [29] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D **108**, 092003 (2023).
- [30] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D 92, 112008 (2015).
- [31] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D **83**, 112005 (2011).
- [32] D. Becirevcic and A. B. Kaidalov, Phys. Lett. B 478, 417 (2000).
- [33] T. Becher and R. J. Hill, Phys. Lett. B 633, 61 (2006).

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