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Restructuring Hospital Industry to Control Public Health Care Expenditure: The Role of Input Substitutability ♣

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Abstract. In this paper we investigate the economic rationality of the bed downsizing process, characterising the hospital industry worldwide in the last decades, as a measure to control public health care expenditure. Considering a sample of Italian hospitals, we provide fresh evidence on the factor substitutability in the production of hospital services. Differently from other studies, based on North-American data and limited to pre-determined cost function models, we estimate a general specification (the *Generalised Composite*), and test it against traditional nested models (e.g. the *Translog*). For all the specifications we derive Allen, Morishima and Shadow elasticities of substitution between input pairs, obtaining a fairly consistent picture across all models and elasticity concepts. In particular, our results highlight a very limited degree of substitutability between factors in the production of hospital services, especially between beds and medical staff. These findings suggest that a restructuring policy of the hospital industry, which is confined to reducing the number of beds without involving workforce management, could not be a viable strategy for controlling public health care expenditure.

Keywords: Public health care expenditure, Hospital industry downsizing, Cost function models, Input substitutability

JEL Codes: D24, H51, I18, L32

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1. Introduction

Hospital industries worldwide have been interested by a huge process of reorganisation in the last decades. At the macro level, in order to curb the presence of excess capacity, public producers' number of beds has been reduced by Central or Regional governments almost anywhere (e.g., McKee, 2004; Kroneman and Siegers, 2004; Hensher *et al.*, 1999). At the micro level, a number of M&As - involving both private and public hospitals - has been observed in several countries, not only as a response to bed reduction, but also to exploit scale and scope economies, and improve effectiveness and quality of care. The process has been originated on two basic premises: on the one hand, the need to contain public health care expenditure imposed governments to find new ways to improve the efficiency (and the effectiveness) in the provision of health services. Empirical analyses on the determinants of health expenditure suggest a positive correlation between the share of inpatients expenditure (i.e., the bulk of hospital costs) and total health spending (e.g., Gerdtham and Jönsson, 2000, and Propper, 2001). As expenditure for hospital services represented (and still represent) a significant share of total health expenditure, it is not surprising that hospitals were clearly at the core of policies aimed at controlling expenditure growth. On the other hand, the perception that an ageing population would have different needs (especially chronic illnesses) with respect to past years caused traditional hospitals – which focus typically on acute care – not to be tailored to answer these structural changes in the epidemiological context.

This massive ongoing reshaping of the hospital industry raises of course a number of questions, that only in recent years the academic literature has started to ask. A first problem to address is to understand whether hospital M&As are justified both from an efficiency and an effectiveness point of view. In this perspective, as discussed in Posnett (1999), results are somewhat mixed. As for efficiency, for instance, studying

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the Canadian Province of Ontario, Preyra and Pink (2006) find large scale unexploited gains from consolidation in the hospital sector, while Bilodeau *et al.* (2002), concentrating on Québec, show the presence of both economies and diseconomies of scale, with some establishments operating at constant returns to scale. As for effectiveness, for example, focusing on U.S. surgical procedures, Birkmeyer *et al.* (2002) find that mortality rates are lower the higher the volume of patients treated, whereas Grilli *et al.* (1998) challenge this view, by surveying literature on cancer patients.

A second question to focus on is the strategic reply of hospitals' managers to bed reductions implemented by Central and Local governments. As for the occupancy rates, Kroneman and Siegers (2004) find for instance that behavioural responses are related to the hospital financing system: in particular, in global budget systems, occupancy rates appear to decline after a reduction in hospital bed supply, while in per diem financing systems, admission rates did not drop following bed downsizing. In both systems, no effects are detected on average length of stay. As for the health expenditure growth, in order to understand the potential role of industry restructuring, an important issue to be discussed concerns workforce management after bed reductions. According to the available literature, there exists a limited substitutability between beds and medical staff. This suggests that, after bed reductions, keeping constant the severity of patients and the quality of treatments, one should observe also a decrease in hospital staffing in order to avoid waste of resources. But while in the U.S. bed downsizing has been accompanied (at least in some cases) with staff reduction, in other countries (especially in Europe) the restructuring of the industry has been limited mostly to beds. This casts some doubts on the effectiveness of this policy in controlling health expenditure growth.

Since the few papers on the estimation of substitution elasticities in the production of hospital services are limited to non-European data, in this paper we provide first evidence on the degree of substitutability for a representative sample of Italian public hospitals, which properly reflects both the prevalence of public producers of health care services in most European countries, and – most importantly – the prevalence of public funding for health care expenditure. In particular, we estimate different cost function models and derive factors elasticity of substitution, considering all hospitals active in an Italian region¹. Like other European countries, the Italian hospital industry experienced a wide restructuring process, and strong pressures to control costs; however, downsizing imposed by the Central government has been limited mostly to beds, while workforce reduction has been tackled at the regional level only blocking turnover, causing a large increase in medical staff per bed. Besides uncovering possible inefficiencies which can limit the potentially positive impact of hospital restructuring on health expenditure rationalization, the estimation of input elasticities of substitution is important *per se*, since the very few studies that have addressed so far this issue did not test the *a priori* imposed specification for the hospital cost function.

The remainder of the paper is structured as follows: Section 2 surveys the economic literature on bed downsizing and its implication for workforce management, including also a discussion of the available estimates of input substitutability in the production of hospital services. Our empirical analysis is presented in Sections 3 and 4, where we first describe our modelling strategy, and then we present the main

¹ The 19 Regions and the 2 Autonomous Provinces in Italy are the administrative entities in charge of managing health care services at the local level. See France *et al.* (2005). Notice that, as each region is held responsible of controlling its own health expenditure, this is the appropriate level of analysis for the problem at hand.

characteristics of the sample and the estimates of a long-run total cost function model. In Section 5 we provide several robustness checks, including the estimation of a shortrun variable cost function. Finally, Section 6 concludes with some implications for health policy.

2. Bed downsizing and workforce management

In this section, we briefly review the scant available literature on the impact of bed downsizing on the staffing of hospitals. The evidence suggests somewhat different effects, according to the prevalence of public or private producers. In the U.S., where the share of private producers is higher than elsewhere, bed downsizing has been sometimes accompanied also with staff reductions, with no clear effects on hospital performance. Chadwick *et al.* (2004) find for example that Human Resource Management practices are important determinants of successful downsizing, of both beds and the workforce. In particular, looking at financial performance of hospitals, they find a positive impact of consideration for employees' morale and welfare during downsizing (like more extensive communication and advance notice, respectful treatment of laid off employees, attention to survivors' concerns on job security). Somewhat contrary to this view, Aiken *et al.* (2002a, 2002b) find that better staffing is positively associated with higher nurse-assessed quality of care, lower risk-adjusted and failure-to-rescue rates, lower level of dissatisfaction and burnout, hence suggesting a deterioration of performance following downsizing.

In other countries, especially in Europe, where the share of public producers is higher, the restructuring of the industry has been mainly driven by the need to control public health expenditure growth. Indeed, as shown by an abundant empirical literature (surveyed by, e.g., Gerdtham and Jönsson, 2000, and Propper, 2001), the ratio of hospital expenditure to total spending is positively related to health care expenditure.

However, differently from the U.S., the restructuring process has been limited in most cases to bed downsizing, while workforce management and planning has been conducted using fixed ratio relationships (e.g., physicians to patients) that have no empirical validity (e.g., Bloor and Maynard, 2003). Of course, this one-factor restructuring process has caused a consistent change in the input-mix, in particular an increase in medical staff per bed. Several factors can help explain observed variations in input-mix. For instance, a higher need of labour can be related to a higher severity of illness in acute care patients (e.g., McKee, 2004). This might be linked to the increase in patients turnover and the reduction in average length of stay (endogenously determined by clinicians), which characterised hospital industries in countries that adopted a Prospective Payment System. Or it might be a signal of the increase in the quality of services, both perceived by nurses or measured in terms of mortality rates (e.g. Aiken *et al.*, 2002a, 2002b).

In this paper, we aim at understanding whether the observed change in input-mix is economically rational for controlling health expenditure, by focusing on the production technology of hospital services². While estimation of production and cost functions and efficiency analysis have received considerable attention in the literature on the hospital industry, economic studies working out also input substitutability in the production of hospital services are quite rare, and – most importantly – are all based on North-American data. A pioneering study is that by Bothwell and Cooley (1982), focusing on Health Maintenance Organizations in the U.S. They distinguish four inputs (administrative services, hospital services, medical professional staff services, and

 2^{2} As emphasised by Propper (2001), most governments are concerned with health expenditure growth, but the key issue for the appropriate design of health care system is efficiency. Our investigation of the optimal input-mix in the production of hospital services moves along these lines.

capital expenses for maintaining a health centre), and find that administrative services are complements to all the other inputs, but that there is substitution between all other input pairs. In particular, Allen elasticity of substitution between medical staff and capital expenses (the input pair we are most interested in, to understand the observed change in input-mix), is estimated to be 0.638, which suggests small substitution possibilities. Jensen and Morrisey (1986), studying the U.S. short-term general acute care hospitals, confirm this result, estimating that elasticity of substitution of medical staff with beds ranges between 0.247 (for non-teaching hospitals) to 0.303 (for teaching ones), and elasticity of substitution between nurses and beds ranges between 0.189 and 0.305 (respectively, for the same type of hospitals). These estimates are even lower adjusting output for case-mix. The same difficulties in substituting between inputs is found also for medical staff and nurses, with estimated elasticities close to 0.35 for both types of hospitals. This last result is in contrast with Cowing and Holtmann (1983). Considering New York State hospitals and computing Allen elasticities, they find substantial substitutability between nurses and other types of workers in the short-run.

More recent studies include e.g. Bilodeau *et al.* (2002) and Okunade (2003). Considering hospitals in Québec, the former study estimates an hospital cost function with five inputs (labour, drugs, food, supplies, and energy). While not reporting punctual estimates of Allen elasticities, the authors interpret substitutability of supplies and energy with labour as the hospitals' general ability to substitute capital for labour. A more complete analysis of input substitutability – considering Allen, Morishima, and Shadow elasticity measures - is provided by Okunade (2003) for Health Maintenance Organizations in the U.S.. The general conclusion is that HMOs production technology is characterised by significant but limited factor substitutions. More specifically, estimated Morishima elasticities of substitution between capital and medical staff are respectively 0.51 (given a change in the price of capital) and 0.67 (given a change in the wage of medical professional staff). These estimates imply that a 10% increase in the price of capital will cause the ratio of medical staff to capital to raise to about 5.12%; in a similar vein, a 10% increase in the wages of medical staff will lift the capital/medical staff ratio by about 6.7%.

Taken together, the available evidence emphasizes two main points: first, at least in Europe, bed downsizing has not been accompanied also by a reduction in the workforce; second, estimates on factor substitutability in the production of hospital services generally suggest that substitution between capital and medical staff (both physicians and nurses) is rather limited. However, these estimates are mostly based on U.S. data, where the health care services are predominantly produced by private firms and financed with private funds. Thus, it is important $-$ in order to understand the effectiveness of bed downsizing on health expenditure – to verify whether this holds true also in the European context. To this end, in the next sections, we provide original evidence on input substitutability, by considering different functional forms and different concepts of elasticity.

3. Empirical analysis

3.1. Modelling strategy

As discussed above, the aim of the paper is to study the technological characteristics of hospital services supply, and the exploration of substitution possibilities among the different inputs involved in the productive process, especially between the number of beds and medical staff (both physicians and nurses). This motivates our modelling strategy, that relies on the estimation of a *total* cost function model. To taking into account some of the most common critiques which can be addressed to such an approach, that relies on the assumptions of long-run equilibrium and of cost minimizing

and efficient behaviour of the investigated productive units, we provide different robustness checks of our main results.

As for the first issue, Smet (2002), in his survey on the cost structure of hospitals, suggests that for health organizations it would be more appropriate to estimate a short-run variable cost function. Obviously, estimating a short-run model precludes the chance to investigate substitution possibilities between capital and labour, which is our main focus here. In order to tackle the issue that our results could be distorted if firms are actually far from the long-run equilibrium, in Section 5 we will test the robustness of our findings by discussing also the estimates of a short-run variable cost function.³

Another important potential source of distortion relates to the argument that firms are assumed to be cost minimizers, and this can be questionable for public producers. However, during the Nineties, the Italian Central government promoted a (still unfinished) reform process of the National Health Service (NHS) aimed at controlling health expenditure, and at putting pressures to Regional governments and public producers to minimize costs. These reforms include, for instance, – at a micro level – the introduction of a Prospective Payment System based on DRGs to remunerate hospitals⁴, and – at a macro level – the launch of a seminal form of fiscal federalism.⁵ Notice also that Eakin and Kniesner (1988), using a sample of US hospitals, provided

³ We are indebted to an anonymous referee for having raised this issue.

⁴ About the impact of the new payment system for hospitals on different producers, see Barbetta *et al.* (2007).

 $⁵$ The pressures to control costs were introduced through these reforms by curbing bailout expectations,</sup> thus inducing harder budget constraints for Regional governments and, consequently, for public hospitals. For more details, see Bordignon and Turati (2009).

evidence that there are no substantial differences among technological estimates coming from non-minimum and minimum cost function.⁶

A third caveat of our modelling strategy concerns the possible presence of cost inefficiency in the provision of health care services. Unfortunately, we are unable to estimate jointly a system of cost functions and related cost-share equations in a stochastic frontier framework, considering a *Generalised Composite* specification.7 Without the inclusion of the information on input cost shares, the results obtained using one-equation frontier models, as far as input substitutability is concerned, are generally very poor. However, Canta *et al.* (2006), using the same dataset of the present study, estimated a single-equation stochastic cost frontier and found inefficiency scores that were significantly reducing across the period $2000-2004$.⁸

Considering all these issues, in Section 4 we then present the evidence stemming from the estimation of our preferred model – i.e., a total cost function – and in Section 5 we enrich the analysis with some extensions and refinements.

3.2. The sample

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The data used in the econometric analysis have been obtained by the *Regione Piemonte* (a highly industrialised area in the North-Western part of Italy, which constitutes one of

⁶ The authors conclude that «generalizing the traditional (minimum) cost function to a non-minimum cost function has a minor impact on the estimates of the observed cost concepts» (Eakin and Kniesner, 1988, p. 596).

⁷ Recently, Kumbakhar and Tsionas (2005) showed how to estimate cost (technical and allocative) inefficiency by recurring to simulation-based Bayesian inference procedures in a well-specified *Translog system* including the cost frontier and related cost-share equations.

⁸ While the authors do not investigate input substitutability, the results they obtained, as far as output and other technological characteristics are concerned, are very similar to the ones presented in Section 4.1. below.

the 21 administrative entities in charge of managing Regional Health Care Systems), and are relative to the productive activity and the cost structure of *all* the hospitals operating in the 27 Local Health Units (LHU) active during the period 2000-2004. LHU are vertically integrated organisations funded by the Region, and responsible of a whole array of hospital and community services⁹. The sample includes two types of hospitals: those directly managed by the LHU (ASL from now on), and other major hospitals that have been hived off from the LHU and transformed into independent enterprises called *Aziende Ospedaliere* (AO from now on).

This unique dataset includes all the publicly owned firms involved in the provision of hospital services in Piedmont. The time span covered by the data follows the NHS reform process discussed above, so that our units are affected by the downsizing policy of the industry, which has been pursued during the 90s, and which is still regarded as one of the primary areas of intervention to control the growth in public health expenditure promoted by the Central government. Planning at the regional level of health care provisions (as envisaged in the recent Piedmont Socio-Health Plan for the years 2006-2010) foresees a reorganisation of the regional hospital network, with the aim of increasing the quality and the effectiveness of services, while controlling expenditure growth. This would imply a reduction of the required number of beds, due to the planned reduction of average length of stay, and a parallel increase in outpatient treatments, home care services, consultancy and day hospital treatments.

Information on the number of beds and on the quantity and complexity of the services provided (total number of patients, average DRG weight, number of inpatient

⁹ See e.g. France *et al.* (2005) for a description of the Italian NHS. We stress again that the regional dimension of our dataset represents the correct choice given the regional level of the current organisation of the Italian NHS.

and outpatient days) have been collected for each single hospital within a LHU and for each AO. The total number of beds, both for inpatient and outpatient treatments, are then computed for each ASL by aggregating the values of the different hospitals which belong to the same LHU. Unfortunately, disaggregated information on the costs and on the labour force are available only for AO, but are not available for each hospital within each LHU. This limitation can represent a problem for ASL units, since staff costs can be related also to community services, rather than hospital services. For such units, considering all costs as relative to the core hospital activity would be inappropriate, so that caution must be put in choosing which type of costs can be included in the study. To that purpose, the different types of costs have been selected and reorganised so as to obtain a measure of operating cost with a composition that can be comparable for ASL and AO structures. We then selected the costs items that are more closely related to the core activity of hospitals, that is the provision of health care services. We come out with a final aggregation named operating hospital cost (*OHC*, the dependent variable in our econometric model) which is the sum of the costs of the following inputs, which are essential for the production of hospital services: labour (physicians and nurses as well as technicians, professionals and administrative staff), drugs, capital (the measure of which is proxied by the total number of beds). As shown in Table 1, for what concerns the relative weight of the different cost categories, the two types of hospitals are very similar. Labour costs are on average about 86% of operating hospital costs, while the weights of drugs and depreciation are respectively 9.6% and 4.4%. *OHC* has a mean value of 79 million euro for ASLs (average yearly growth rate of 3.6%) and 122 million euro for AOs (average yearly grow rate of 4.8%).

[TABLE 1 HERE]

3.3. Explanatory variables of the cost model

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Exploiting the informative content of the database, we have obtained the following explanatory variables to be included in the estimation of the cost function: output, complexity of provided services (case-mix), input prices. The full sample is a panel of 29 productive units which are observed over a period of 5 years, for a total of 145 observations. As an index of production volume (*Y*) we opted for the total number of patients per year (both inpatients and outpatients). We included both types of patients to take into account the increase observed in the last decade in the share of outpatients out of total patients; this solves also the omitted variable bias emphasised by Crémieux and Ouellette (2001) for hospital cost functions. In addition, in order to account for the severity of illnesses and the composition of our output measure, a control variable of the average DRG weight (*DRGW*) has been added. This should reflect the differences in the production mix, i.e. the average degree of complexity of the services provided by the hospital structures 10 .

As the labour input is concerned, a distinction has been made between medical staff (*MS*, including physicians and nurses) and other staff (*OS*, including technicians, professionals, and administration); as common in the literature, average prices for the two categories (P_{MS} and P_{OS} , respectively) have been obtained by dividing costs by the

 10 For example, a tonsillectomy is a typical operation with a low degree of complexity (DRG weight 0.27), while thyroid (DRG weight 1.04) and cardiovascular operations (DRG weight 2.40) have an average and a high degree of complexity, respectively. Notice that DRG weights can be influenced by upcoding at the hospital level. However, while we do not have direct evidence of such practices in Italy, Silverman and Skinner (2004) have shown that they are uncommon in public hospitals.

effective number of employees¹¹. As a proxy for the price of drugs (P_D) we used the ratio between the corresponding cost and the total number of inpatients and outpatients days per year. Finally, as common in the literature (see, e.g., Farsi and Filippini, 2008), the average price of the capital input (P_K) has been computed by dividing depreciation charges by the total number of beds (*K*). Admittedly, this is only a crude measure of capital usage in the production of hospital services; however, this is just the policy variable we are interested in assessing substitution possibilities (e.g., Jacobs *et al.*, 2006, for general comments and a survey).

A time trend - that should capture the effect of technical progress - has been added to the model *(T)* and fully interacted with input price, output and DRG variables, in order to explore the possibility that technological change is not neutral and scale augmenting/reducing.¹²

Table 2 reports the descriptive statistics of the variables used in the estimation. There is a high variability in the level of operating costs and in the output levels, which is partially due to the fact that our sample of hospitals is very heterogeneous in size, but can be also explained by the above mentioned differences among ASL and AO units¹³.

[TABLE 2 HERE]

¹¹ Notice that wages are contracted at the national level, with only minor contractual arrangements at the regional level. Hospital managers then define staffing taking as given the labour prices.

¹² In the more parsimonious version of the model in which T has not been interacted, its coefficient can be interpreted as a growth (or decline) rate of costs due to a Hicks-neutral technological change.

¹³ The sample consists of 7 small units (average number of beds \leq 368), 15 units of an average size (368 < average number of beds ≤ 621) and 7 big units (average number of beds > 621).

3.4. Functional form and estimation procedure

The bulk of empirical works on hospital costs adopted the well-known Translog specification. Given the complexity of hospital services production process, we do not impose *a priori* restrictions on the functional form and estimate a more general model, namely the *Generalised Composite* cost function, which has been first introduced by Pulley and Braunstein (1992, PB_G). The PB_G model reads as follows:

$$
OHC^{(\phi)} = \begin{cases} \begin{bmatrix} \alpha_0 + \alpha_Y Y^{(\pi)} + \alpha_{DRGW} DRGW^{(\pi)} + \alpha_T T + \frac{1}{2} \alpha_{YY} Y^{(\pi)} Y^{(\pi)} + \frac{1}{2} \alpha_{DRGWDRGW} DRGW^{(\pi)}) DRGW^{(\pi)} \\ + \frac{1}{2} \alpha_{TT} T^2 + \alpha_{YDRGW} Y^{(\pi)} DRGW^{(\pi)} + \alpha_{YT} Y^{(\pi)} T + \alpha_{DRGW} DRGW^{(\pi)} T + \sum_r \delta_{yr} Y^{(\pi)} \ln P_r \\ + \sum_r \delta_{DRGWr} DRGW^{(\pi)} \ln P_r + \sum_r \delta_{rr} T \ln P_r + \sum_i \gamma_i Z_i \end{bmatrix} & \times \exp \begin{bmatrix} \sum_r \beta_r \ln P_r + \frac{1}{2} \sum_r \sum_i \beta_{ri} \ln P_r \ln P_i \end{bmatrix} \end{cases} (1)
$$

where the superscripts in parentheses π , ϕ and τ represent Box-Cox transformations (for example $Y^{(\pi)} = (Y^{\pi} - 1)/\pi$ for $\pi \neq 0$ and $Y^{(\pi)} \rightarrow \ln Y$ for $\pi \rightarrow 0$). *OHC* is the long-run production cost of hospital services, *Y* is the output, *DRGW* is the average degree of complexity of the service provided, P_r indicates factor prices (with $r = MS$, *OS*, *D* and *K*), *T* is the time trend, and *Z* is a vector of additional control variables.¹⁴ By applying the *Shephard's Lemma*, the associated input cost-share equations are:

$$
S_r = \begin{bmatrix} \alpha_0 + \alpha_Y Y^{(\pi)} + \alpha_{DRGW} DRGW^{(\pi)} + \alpha_T T + \frac{1}{2} \alpha_{YY} Y^{(\pi)} Y^{(\pi)} + \frac{1}{2} \alpha_{DRGWDRGW} DRGW^{(\pi)} DRGW^{(\pi)}) \\ + \frac{1}{2} \alpha_{TT} T^2 + \alpha_{YDRGW} Y^{(\pi)} DRGW^{(\pi)} + \alpha_{YT} Y^{(\pi)} T + \alpha_{DRGW} DRGW^{(\pi)} T + \sum_r \delta_{Y_r} Y^{(\pi)} \ln P_r \\ + \sum_r \delta_{DRGW} DRGW^{(\pi)} \ln P_r + \sum_r \delta_{Tr} T \ln P_r + \sum_i \gamma_i Z_i \\ \times \left(\delta_{Y_r} Y^{(\pi)} + \delta_{DRGW} DRGW^{(\pi)} + \delta_{Tr} T \right) + \beta_r + \sum_i \beta_{ri} \ln P_i \end{bmatrix} \tag{2}
$$

¹⁴ The latter are respectively two dichotomous variables that identify large and medium-sized hospitals $(D_L$ and D_M), one dummy for *AO* units (D_{AO}) , and one variable controlling for the ratio of outpatient beds to the total number of beds (*OUTBED*)

The *Composite* specification (PB_C) is obtained by setting $\pi = 1$ and $\tau = 0$. In a similar vein, the well-known *Generalised Translog* (GT) and *Standard Translog* (ST) models, as well as the *Separable Quadratic* (SQ) functional form, can be estimated by imposing simple restrictions on the system $(1)-(2)^{15}$.

The PB cost functions originate from the combination of the log-quadratic input price structure of the ST and GT specifications with a quadratic structure for outputs.¹⁶ The relatively few studies which employed the PB specifications referred to the banking, telecommunications, multi-utilities and electricity sectors (e.g., Fraquelli *et al.*, 2005, Piacenza and Vannoni, 2009). Overall, the composite model has consistently proved to be successful in obtaining more stable and reliable estimates than the alternative functional forms (see Piacenza and Vannoni, 2004, for more details). The PB_G model proposes to transform both sides of the cost function – from $OHC = C(Y, P)$ to *OHC*^{(ϕ}) = $[C(Y, P)]^{(\phi)}$ – in order to enlarge the set of plausible empirical specifications. The optimal value of ϕ can be estimated resorting to non-linear least squares routines. The comparison between the general PB_G specification and the nested models (i.e. PB_C , SQ, GT, and ST) can be made by LR tests using the estimated loglikelihood values for the system (1)-(2).

¹⁵ More precisely, the GT model is obtained by setting $\phi = 0$ and $\tau = 1$, while the ST model requires the further restriction $\pi = 0$. The SO model is obtained from the PB_C specification by adding the restrictions $\delta_{Yr} = 0$, $\delta_{DRGWr} = 0$ and $\delta_{Tr} = 0$ for all *r*.

 16 The log-quadratic input price structure can be easily constrained to be linearly homogeneous. To be consistent with cost minimization, equation (1) must satisfy symmetry ($\beta_{rl} = \beta_{lr}$ for all couples *r*,*l*) as well as the following properties: *a*) non-negative fitted costs; *b*) non-negative fitted marginal costs with respect to outputs; *c*) homogeneity of degree one of the cost function in input prices ($\Sigma_r \beta_r = I$ and $\Sigma_l \beta_{rl} = 0$ for all *r*, as well as $\Sigma_r \delta_{Yr} = 0$, $\Sigma_r \delta_{DRGWr} = 0$ and $\Sigma_r \delta_{Tr} = 0$; *d*) non-decreasing fitted costs in input prices; *e*) concavity of the cost function in input prices.

All the specifications of the cost function are estimated jointly with their associated input cost-share equations. In our four-inputs case, to avoid the singularity of the covariance matrix of residuals, the equation for other staff (S_{OS}) was not included in each of the estimated systems. Prior to estimation, all variables were standardized on their respective sample means. Parameter estimates were obtained via a non-linear GLS estimation (NLSUR), which ensures estimated coefficients to be invariant with respect to the omitted share equation.

4. Results

 \overline{a}

4.1. The total cost function

The results of the NLSUR estimation for the ST, GT, SQ, and PB models are presented in table $3¹⁷$ By looking at the summary statistics (last five rows), one can observe that computed R^2 for the cost function is rather high and identical across specifications, while R^2 associated to the factor-share equations are not dissimilar except from the SQ model, for which these are much lower (in particular for capital input). The poor ability of the SQ specification to fit the observed factor-shares is not surprising, given that it assumes a strong separability between inputs and outputs. McElroy's (1977) R^2 can be used as a measure of the general goodness of fit for the NLSUR system. The results suggest that the fit is almost identical for the different functional forms, and between 83% and 86%. However, LR tests comparing PB_G and the restricted specifications (see table 4) always lead to favour the *Generalised Composite* model (at the 5% significance level) with respect to PB_C , SO, GT, and ST alternative functional forms.

¹⁷ Tables 3 through 6 show the results of a parsimonious version of model (1), where T is not interacted with other variables and the additional regressors Z_i are omitted. The estimates for the full model are presented in section 5.

[TABLE 3 AND 4 HERE]

The first six rows of table 3 present the estimates of first-order coefficients for output, average DRG weight and factor prices, which are all highly significant and show the expected sign. Since the results are similar across specifications, we comment only on the estimated parameters for the PB_G model, which is to be preferred over the alternatives according to LR tests. In particular, we briefly discuss cost elasticities with respect to *Y*, *DRGW*, P_{MS} , P_D and P_K for the *average* hospital within the industry¹⁸.

The output elasticity is defined as:

 \overline{a}

$$
\partial \ln C / \partial \ln Y = \begin{pmatrix} \alpha_0 + \alpha_Y Y^{(\pi)} + \alpha_{DRGW} DRGW^{(\pi)} + \alpha_T T + \frac{1}{2} \alpha_{YY} Y^{(\pi)} Y^{(\pi)} + \frac{1}{2} \alpha_{DRGWDRGW} DRGW^{(\pi)} DRGW^{(\pi)}) \\ + \frac{1}{2} \alpha_{TT} T^2 + \alpha_{YDRGW} Y^{(\pi)} DRGW^{(\pi)} + \alpha_{YT} Y^{(\pi)} T + \alpha_{DRGW} DRGW^{(\pi)} T + \sum_r \delta_{Y_r} Y^{(\pi)} \ln P_r \\ + \sum_r \delta_{DRGW} DRGW^{(\pi)} \ln P_r + \sum_r \delta_{Tr} T \ln P_r + \sum_i \gamma_i Z_i \\ \times (\alpha_Y + \alpha_{YDRGW} DRGW^{(\pi)} + \alpha_{YT} T + \alpha_{YY} Y^{(\pi)} + \sum_r \delta_{Y_r} \ln P_r) \cdot Y^{\pi-1} \cdot Y \end{pmatrix}^{r-1}
$$
(3)

At the normalization point, and for the first year of our sample (i.e., with $T = 1$), it can be computed as 19 :

$$
\partial \ln C / \partial \ln Y = \left(\alpha_0 + \alpha_T + \frac{1}{2} \alpha_{TT} \right)^{r-1} (\alpha_Y + \alpha_{YT})
$$
\n(4)

In a similar vein, at the normalization point, the cost elasticity with respect to DRGW is:

$$
\partial \ln C / \partial \ln DRGW = \left(\alpha_0 + \alpha_T + \frac{1}{2} \alpha_{TT}\right)^{r-1} \left(\alpha_{DRGW} + \alpha_{DRGWT}\right)
$$
\n(5)

¹⁸ The *average* LHU (the point of normalization) corresponds to a hypothetical LHU operating at an average level of production and degree of complexity, and facing average input prices.

¹⁹ Notice that in the Translog functional form $\tau = 1$, so that $\partial \ln C / \partial \ln Y = \alpha_Y + \alpha_{YT}$.

The estimate of the output elasticity is significantly lower than 1 (around 0.71, Standard Error 0.05), revealing the presence of remarkable scale economies (the index of returns to scale – $1/(\partial \ln C/\partial \ln Y)$ – is about 1.41, SE 0.11) that could be better exploited, for instance, by enlarging the average size of hospitals managed by LHUs. On the *DRGW* side, it emerges a strong impact of the severity of illnesses on *OHC* (∂ ln*C*/ ∂ ln*DRGW* is about 0.39, SE 0.13), which is consistent with previous empirical literature on the cost structure of hospital services. Finally, as for the estimates of input cost-shares for the average hospital – corresponding to cost elasticities ($\partial \ln C / \partial \ln P_r$) with respect to the price of medical staff (0.66) , drugs (0.10) , and capital, proxied by beds (0.05) – they are very similar to their respective sample mean values (see S_{MS} , S_D and S_K in table 2), thus confirming the general goodness of fit of the PB_G cost function model.

4.2. The elasticities of substitution

Definitions. Given the main aim of this study, we computed Allen, Morishima, and Shadow elasticities of substitution for all the estimated models (Chambers, 1988). Ideally, one wants to measure for each couple of inputs the percentage change in the input ratio x_r/x_l due to a percentage change in the input price ratio P_l/P_r . Allen elasticities can be considered as *one price-one factor* elasticities, since they measure how the use of an input varies due to changes in the price of another input. They can be computed as:

$$
\sigma_{rl}^4 = \varepsilon_{rl}/S_l \tag{6}
$$

where S_l is the l^{th} cost share and ε_{rl} is the derived input-demand elasticity of input x_r with respect to price P_l (dln*x_r*/dln*P_l*). While they have been criticized to a great extent in the literature, Allen elasticities are still widely used in applied production analysis as they serve as the basis for deriving other elasticities. *Morishima* elasticities represent *two factor-one price elasticities* and are closer proxies to the desirable measure. They are

computed as $\sigma_{rl}^M = \varepsilon_{rl} - \varepsilon_{ll}$ and measure how the *r*,*l* input ratio responds to a change in *P*_{*l*}. As expressed by (7), there is a useful link between Morishima and Allen elasticities:

$$
\sigma_{rl}^M = (\sigma_{rl}^A - \sigma_{ll}^A) S_l \tag{7}
$$

It is straightforward to notice than when inputs are Allen substitutes, they must be also Morishima substitutes (since σ_{ll}^4 is always negative) but the converse does not hold, so that inputs can well be Allen complements and Morishima substitutes. Finally, *Shadow* elastiticities of substitution are a weighted average of Morishima elasticities and, as such, they are *two factor-two price* elasticities:

$$
\sigma_{n}^{S_{rl}} = \frac{S_r}{S_r + S_l} \sigma_{n}^{M} + \frac{S_l}{S_r + S_l} \sigma_{n}^{M} \tag{8}
$$

After some computation, Allen elasticities can be written as:

 \overline{a}

$$
\sigma_{\scriptscriptstyle A}^{\scriptscriptstyle A} = \frac{\frac{\partial S_r}{\partial P_l} P_l + S_r S_l}{S_r S_l} \tag{9}
$$

Thus, in order to compute elasticities (6)-(8) for our different cost function models, it is important to compute the partial derivative $\partial S_r/\partial \ln P_l$ ²⁰ From (2):

$$
\partial S_{r}/\partial \ln P_{i} = \begin{bmatrix}\n\alpha_{0} + \alpha_{Y}Y^{(\pi)} + \alpha_{DRGW}DRGW^{(\pi)} + \alpha_{T}T + \frac{1}{2}\alpha_{YY}Y^{(\pi)}Y^{(\pi)} + \frac{1}{2}\alpha_{DRGWDRGW}DRGW^{(\pi)}DRGW^{(\pi)})\n\end{bmatrix}^{r-2}\n\begin{bmatrix}\n10 \\
+\frac{1}{2}\alpha_{TT}T^{2} + \alpha_{DDRGW}Y^{(\pi)}DRGW^{(\pi)} + \alpha_{TT}Y^{(\pi)}T + \alpha_{DRGW}DRGW^{(\pi)}T + \sum_{r} \delta_{r}Y^{(\pi)}\ln P_{r}\n\end{bmatrix}^{r-2}\n\begin{bmatrix}\n10 \\
+\sum_{r} \delta_{DRGW}DRGW^{(\pi)}\ln P_{r} + \sum_{r} \delta_{r}T\ln P_{r} + \sum_{i} \gamma_{i}Z_{i}\n\end{bmatrix}
$$

[TABLE 5 HERE]

²⁰ At the point of normalization: $\partial S_r / \partial \ln P_l = \left[\alpha_0 + \alpha_T + \frac{1}{2} \alpha_{TT} \right]^{r-2} (\tau - 1) (\delta_T) (\delta_T) + \beta_{rl}$ $\partial S_r / \partial \ln P_i = \left[\alpha_0 + \alpha_r + \frac{1}{2} \alpha_{rr} \right]^{r-1}$ ln $P_l = \left[\alpha_0 + \alpha_T + \frac{1}{2} \alpha_{TT} \right]^{r-2} (\tau - 1) (\delta_{Tr}) (\delta_{T} + \beta_{rl})$. It can be easily

shown that in the ST, GT and SQ specifications, such derivative trivially corresponds to the coefficient *βrl*.

Empirical evidence. As can be seen in table 5, except from Allen elasticities for the input pair drugs-capital, all inputs are substitutes, but the low estimated values suggest that substitution possibilities are in general very limited. As an example, in the PB_G specification, $\sigma_{MS,K}^M = 0.13$, suggesting that a 10% increase in the price of capital implies only a 1.3% change in the *MS/K* ratio. The highest figures are recorded for the input pairs involving *OS,* suggesting that the other three inputs (medical staff, drugs and capital) are particularly responsive to increases in the price of 'non medical' staff $(\sigma_{r,OS}^M)$ are higher than σ^{M} _{*OS,r*} for all *r*). The results are remarkably stable across specifications for almost all input pairs, and are broadly consistent with the ones previously appeared in the empirical literature. As discussed in Section 2, e.g. Jensen and Morrisey (1986) found substitution elasticities equal to 0.25 for the pair medical staff/beds and equal to 0.19 for the pair nurses/beds. Bilodeau *et al.* (2002) found that labour and drugs were substitutes with substitution elasticities lower than 1. As far as capital is concerned, the substitution possibilities with other inputs are lower, i.e. the values of $\sigma_{r,K}^M$ are lower than all the other $\sigma_{r,l}^M$ couples and the values of $\sigma_{K,r}^M$ are lower than all the other $\sigma_{l,r}^M$ couples.

[TABLE 6 HERE]

Discussion. Table 6 presents the estimates of Shadow elasticities of input substitutability when the productive scale (*Y*) and the DRG weight (*DRGW*) of the average hospital of our sample are increased (and reduced) proportionally, focusing on the cost function model best fitting the data, i.e. the PB_G specification. Parameters $λ_Y$ and $λ_{DRGW}$ refer to the coefficients used to scale down (λ_Y = 0.25, 0.5; λ_{DRGW} = 0.5) and up (λ_Y = 2, 3; λ_{DRGW}

 $=$ 2) the average values of the output (*Y* = 22,072 patients) and DRG weight (*DRGW* = 1.12), respectively²¹. First, notice that for almost all input pairs (with the notable exception of *MS-OS*), it emerges a certain degree of complementarity only by scaling down the average producer. Even if estimated elasticities are always insignificant at the usual confidence levels, this result suggests a higher rigidity in managing inputs for small-scale low-complexity generalist community hospitals, for instance because they need to respect exogenously given standards for staff and beds, which are binding given their volumes of output. Clearly enough, this rigidity helps explain the findings of unexploited scale economies for very small hospitals. Second, note that by scaling up the average hospital, both with respect to output volume and with respect to output complexity, substitution possibilities (and statistical significance) increase, but substitutability remain fairly small and significantly less than unity. These results hold even scaling up contemporaneously the average hospital in the two mentioned directions. For instance, concentrating on the most interesting of these input pairs for us (*MS-K*), by doubling the DRG weight and tripling output volume, elasticity of substitution rises from 0.14 to 0.30 only. Notice also that – for the *MS-K* pair – holding constant output volume at $\lambda_Y = 3$, it emerges a slight decrease of substitution possibilities when increasing complexity of output. This last result shows up also for almost all other couples of inputs, and suggests that – at high volumes – substitution between factors becomes increasingly difficult when also complexity of treated patients increase. This finding is consistent with a high rigidity of the production process starting from high levels of output. Results are more ambiguous when holding DRG weights fixed at $\lambda_{DRGW} = 2$: increasing the levels of output eases substitutability for the *MS-K*, *D-K*, and *K-OS* pairs, while substitutability worsens for the remaining couples of inputs. Finally, note that for

²¹ Notice that scale parameters are based on values of *Y* and *DRGW observed* in our sample.

the *MS-OS* input pair, estimated elasticities are invariant both to scaling with respect to output volume and to scaling with respect to output complexity, being consistently close to unity (and statistically significant). Overall, our findings confirms then previous estimates in the literature, validating the difficulties for hospitals in substituting between input pairs, in particular between medical staff and beds.

These difficulties cast some doubts on bed downsizing policies as an effective tool for controlling health expenditure in countries, like the European ones, where the share of public producers (and public funding) is significantly higher than in the U.S. Restructuring of the hospital industry limited to reductions in the number of beds, without tackling the likely presence of excessive staffing, can both bound the production possibilities and – more importantly – preclude potential savings in health expenditure. However, before commenting further on this crucial policy issue, we further discuss our results by providing several robustness checks.

5. Extensions and robustness checks

As anticipated in Section 3.1, we discuss here some critical issues of our empirical strategy, by testing the robustness of our results to alternative assumptions about model specification.

First, in order to tackle the argument that our results could be distorted if firms are actually far from the long-run equilibrium, we estimate a short-run cost function, by including *K* among the explanatory variables, and by using the variable cost (*VC*) as the left hand side variable, which was computed by subtracting the capital cost from *OHC*. The results are quite similar to the ones presented in Section 4, with a cost elasticity with respect to Y ($\partial \ln V C / \partial \ln Y$) equal to 0.602 and a cost elasticity with respect to K (∂ ln*VC*/ ∂ ln*K*) positive and equal to 0.082. This latter result is quite common in the literature (see, for example, Smet, 2002 and Aletras, 1999), and suggests that hospitals

are over-investing in capital. The estimates of short-run scale economies – 1/(∂ ln*VC*/ ∂ ln*Y*) – are equal to 1.66, while long-run scale economies, computed using the formula introduced by Caves *et al.* (1981) – [1 - ($\partial \ln \sqrt{C}/\partial \ln \sqrt{C}/\partial \ln \sqrt{C}/\partial \ln \sqrt{C}$) – are equal to 1.52. More interestingly for our analysis, the estimates of elasticities of substitution among the variable input pairs are very similar to the ones stemming from the total cost function estimation. For example, the last column in table 8 reports that $\sigma_{MS,D}^S = 0.27$, $\sigma_{MS,OS}^S = 0.93$ and $\sigma_{D,OS}^S = 0.44$.

Remaining confined within a total cost function approach, we have performed additional robustness checks, that consider perturbations of the parsimonious version of equation (1), where the time trend is not interacted with the other right hand side variables and the additional explanatory variables Z_i are not included in the regression. Table 7 shows the results of the EXTENDED MODELS. Columns 1 (EXTENDED MODEL 1) and 3 (FULL EXTENDED MODEL) show that 5 out of the 7 coefficients involving the time trend are not significantly different from zero. Columns 2 (EXTENDED MODEL 2) and 3 show an increasing impact on costs of the two size dummies $(D_L$ and D_M) and a decreasing impact on costs of the AO-type dummy (*DAO*) and of the *OUTBED* variable.

[TABLE 7 HERE]

Consistent with a priori expectations, after having controlled for the other right hand side variables, bigger hospitals are found to exhibit higher costs, while more autonomous units (*Aziende Ospedaliere*) are associated with lower costs. Finally, a higher ratio of outpatient beds to the total number of beds is effective in bringing a cost reduction. The computed elasticities of substitution across all input pairs are remarkably stable (see table 8, second column).

The inclusion of a time trend (which is invariant across firms) together with size and AO-type dummies (which are invariant across time) partially allows us to exploit the longitudinal dimension of our dataset. However, we have been also able to estimate a FIXED EFFECTS MODEL, which takes into account potential unobserved heterogeneity across production units and includes a separate dummy for each hospital.²² Once again, elasticities of substitution, reported in the third column of table 8, are very similar.

[TABLE 8 HERE]

We finally performed three additional checks. First, in order to test if results are affected by the choice of pooling together ASL and AO, we have also estimated the different models only on the ASL sub-sample. Second, in order to check for the impact of potential outliers, we adopt a jackknifing procedure, and exclude from the sample 7 extreme observations, for which the staff (both MS and OS) per bed ratio was rather different from the average. Third and last, in order to reduce as much as possible the differences between AO (focusing on hospital services) and ASL (also active in other health activities) types, we have corrected the costs by attributing to the latter only 80% of labour cost and 75% of the cost of capital.²³ In all the three cases, we obtained results (which are available upon request) that were virtually unchanged with respect to our original long-run cost model.

 22 Estimates of hospital-specific fixed effects cost model have not been included here for brevity but are available upon request from the authors.

²³ These percentages, which should make the cost structure more homogenous across the two types, have been suggested in a report carried out by the Italian Ministry of the Economics and Finance (*Relazione Generale sulla Situazione Economica del Paese*, 1995, vol. II, tab. SA.2).

A final issue which can be raised is that our sample of firms is affected by a regulatory intervention aimed at hospital downsizing by means of the reduction in the number of beds. In particular, the constraints are imposed by the Central government at the regional level (i.e., the target of reducing the number of beds must be reached for the whole Piedmont region), so that one cannot include the constraint in the specification of the cost function (which refer to the hospital level). However, we are confident that the presence of this constraint is not seriously biasing the estimates for input elasticities. For example, Granderson and Lovell (1998) were able to introduce a firm-specific variable accounting for rate of return regulation in the gas industry and found that such regulation pushed firms to overinvest in capital and increased the estimates of elasticity of substitution of $\sigma^{M}_{K,r}$ pairs and reduced those of $\sigma^{M}_{r,K}$ pairs. Since, in our case, the constraint pushes toward the opposite direction (i.e., the reduction of beds), it is reasonable to assume that in an unregulated framework one should observe higher values for $\sigma_{r,K}^M$ couples and lower values for $\sigma_{K,r}^M$ pairs. Looking at the figures in table 5, this means that the values of such pairs should get closer the ones to the others, thus making Morishima elasticities more symmetrical and leaving almost unchanged the values of Shadow elasticities.

6. Concluding remarks

The hospital industry in many countries has undergone an unprecedented process of restructuring, aimed at reducing excess capacity and increasing the appropriateness of care. In Italy (like in other European countries) this process has been limited to bed downsizing; the management and planning of the workforce potentially in excess has been conducted using fixed-ratio relationships with no empirical validity, often resulting in a change of the input-mix used in the production of hospital services.

In this paper, starting from the premise that industry restructuring is $-$ at least partly – aimed at controlling expenditure growth, we investigate the economic rationality of input-mix change, providing fresh evidence on the factor substitutions characterising hospitals' technology. We consider all producers located in Piedmont, a region in the North-Western part of Italy, where the hospital industry has been (and still is) marked by a wide reduction in the number of beds, while no significant decrease has been observed for medical staff (including both physicians and nurses). Differently from other studies, we do not impose *a priori* restrictions on the specification of the hospital cost function, and estimate a more general model, namely the *Generalised Composite*, embracing all the standard specifications usually adopted in the literature. For all the models, we derive Allen, Morishima and Shadow elasticities of substitution between input pairs, obtaining a fairly consistent picture across all specifications and elasticity concepts. In particular, confirming previous findings in the literature, our results suggest a very limited degree of substitutability between factors in the production of hospital services. This is particularly true for beds and medical staff.

Given this evidence, one can notice that putting restrictions on bed capacity – without taking into account their limited possibility of substitution – might imply an inefficient use of resources, and severely limit the possibility to control public health expenditure by restructuring the hospital industry. More effective policies are probably needed to obtain the expected savings. An example in this direction is likely to be the reallocation of the workforce from the hospital towards the production of other health services, such as for instance home and community care.

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Table 1. Breakdown of operating hospital cost by year and type of hospital

Table 2. Summary statistics for the variables used in the cost function models

REGRESSORS ^a	PB _G MODEL	PBC MODEL	SQ MODEL	GT MODEL	ST MODEL
Constant	$1.004***$	$0.995***$	$1.003***$	-0.021	0.982***
Y	$0.717***$	$0.638***$	0.683***	$0.622***$	0.638***
DRGW	$0.391***$	$0.479***$	$0.553***$	$0.367***$	$0.441***$
InP _{MS}	$0.658***$	$0.658***$	$0.661***$	$0.660***$	$0.658***$
$ln P_D$	$0.100***$	$0.101***$	$0.095***$	$0.098***$	$0.100***$
$ln P_K$	$0.046***$	$0.046***$	$0.043***$	$0.044***$	$0.046***$
Τ	0.003	0.002	0.004	0.011	0.008
Y^2	-0.321	-0.113	$-0.136**$	-0.241	$0.187*$
DRGW ²	0.322	0.031	0.002	-0.141	-0.560
YDRGW	0.526	$0.613***$	$0.587***$	0.272	0.214
Y In P_{MS}	-0.013	-0.011	0	$-0.016*$	-0.010
$Y \ln P_D$	$0.019***$	$0.018***$	0	$0.021***$	$0.017***$
$Y \ln P_K$	$0.012**$	$0.011**$	0	$0.012**$	$0.010*$
$DRGW$ In P_{MS}	$-0.025**$	$-0.024*$	0	$-0.035**$	$-0.034**$
$DRGW$ In P_D	$0.037***$	$0.037***$	0	$0.048***$	$0.048***$
$DRGW$ In P_K	0.012	0.012	0	0.015	0.015
InP _{Ms} P _{OS}	0.010	0.007	-0.004	0.005	0.006
InP _{Ms} P _D	$-0.046***$	$-0.046***$	$-0.043***$	$-0.044***$	$-0.044***$
InP _{Ms} P _K	$-0.029***$	$-0.028***$	$-0.023***$	$-0.027***$	$-0.027***$
Ln P _{OS} P _D	-0.010	-0.009	0.001	-0.004	-0.006
Ln P _{OS} P _K	0.004	0.002	0.007	0.006	0.003
In P _D P _K	$-0.012**$	$-0.012***$	$-0.017***$	$-0.014***$	$-0.013***$
Box-Cox ϕ	$-0.446*$	-0.260	-0.260	0	$\boldsymbol{0}$
Box-Cox π	$1.219***$	1	1	$0.563***$	0
Box-Cox τ	0.015	0	0	1	1
System log-likelihood	1406.581	1402.422	1315.912	1385.590	1377.424
System R^{2b}	0.863	0.859	0.832	0.849	0.858
- Cost function R^2	0.921	0.918	0.916	0.918	0.916
- S_{MS} equation R^2	0.514	0.507	0.446	0.528	0.512
- S _D equation R^2	0.769	0.771	0.581	0.766	0.782
- S _K equation R^2	0.571	0.592	0.073	0.518	0.570

Table 3. NLSUR parameter estimates for the *Generalised Composite* (PB_G), *Composite* (PB_C), *Separable Quadratic* **(SQ),** *Generalised Translog* **(GT) and** *Standard Translog* **(ST) models**

^a The dependent variable is Operating Hospital Cost (*OHC*).
^b The goodness-of-fit measure used for NLSUR systems is McElroy's (1977) *R* ².

*** significant at 1 % level, ** significant at 5 % level, * significant at 10 % level (two-tailed test).

Restricted model ^a	χ^2 -statistic	P-value
PBC MODEL $(\pi = 1, \tau = 0)$	8.318	0.016
SQ MODEL $(\pi = 1, \tau = 0, \delta_{\gamma} = \delta_{DRGWr} = 0$ for all r)	181.338	0.000
GT MODEL $(\phi = 0, \tau = 1)$	41.983	0.000
ST MODEL $(\phi = 0, \pi = 0, \tau = 1)$	58.314	0.000

Table 4. Comparing *Generalised Composite* **(PBG) against restricted models by LR tests**

 a ^a The restrictions with respect to PB_G model are reported in parentheses.

Allen elasticities (1 factor, 1 price)		PB _G MODEL PB _C MODEL	SQ MODEL	GT MODEL	ST MODEL
MS, K	0.02(0.27)	0.09(0.25)	0.17(0.25)	0.06(0.26)	0.10(0.26)
MS, D	0.31(0.13)	0.31(0.12)	0.32(0.12)	0.31(0.12)	0.33(0.13)
MS, OS	1.08(0.30)	1.05(0.30)	0.87(1.23)	1.04(0.28)	1.05(0.30)
D, K	$-1.62(1.16)$	$-1.56(1.01)$	$-3.30(0.59)$	$-2.26(0.85)$	$-1.94(1.00)$
D, OS	0.50(0.57)	0.52(0.54)	1.06(0.38)	0.78(0.47)	0.67(0.53)
K, OS	1.39(1.33)	1.22(1.18)	1.85(0.95)	1.66(1.06)	1.38(1.22)
<i>Morishima elasticities</i> (2 factors, 1 price)	PB _G MODEL	PB _c MODEL	SQ MODEL	GT MODEL	ST MODEL
MS, K	0.13(0.13)	0.14(0.11)	0.18(0.10)	0.15(0.11)	0.15(0.12)
K, MS	0.26(0.18)	0.30(0.17)	0.34(0.17)	0.28(0.18)	0.31(0.18)
MS, D	0.26(0.05)	0.20(0.05)	0.31(0.06)	0.29(0.06)	0.29(0.06)
D, MS	0.45(0.09)	0.44(0.09)	0.44(0.09)	0.45(0.09)	0.46(0.09)
MS, OS	1.04(0.28)	1.01(0.28)	1.00(0.43)	1.03(0.26)	1.02(0.28)
OS, MS	0.95(0.25)	0.93(0.25)	0.81(0.86)	0.92(0.24)	0.93(0.25)
D, K	0.05(0.10)	0.07(0.11)	0.03(0.11)	0.05(0.12)	0.05(0.12)
K, D	0.06(0.13)	0.08(0.08)	$-0.03(0.07)$	0.04(0.08)	0.06(0.08)
D, OS	0.92(0.29)	0.90(0.28)	1.04(0.22)	0.99(0.25)	0.95(0.29)
OS, D	0.28(0.09)	0.29(0.09)	0.38(0.08)	0.34(0.09)	0.33(0.09)
K, OS	1.10(0.40)	1.04(0.38)	1.20(0.29)	1.16(0.32)	1.09(0.38)
OS, K	0.19(0.18)	0.16(0.15)	0.25(0.13)	0.22(0.14)	0.20(0.17)
Shadow elasticities (2 factors, 2 prices)	PBG Model	PBc Model	SQ MODEL	GT MODEL	ST MODEL
MS, K	0.14(0.12)	0.15(0.10)	0.19(0.10)	0.16(0.10)	0.16(0.12)
MS, D	0.28(0.05)	0.29(0.05)	0.33(0.06)	0.31(0.06)	0.31(0.06)
MS, OS	1.02(0.27)	0.99(0.27)	0.95(0.53)	1.01(0.25)	1.00(0.28)
D, K	0.06(0.10)	0.07(0.09)	0.01(0.09)	0.05(0.10)	0.06(0.10)
D, OS	0.50(0.14)	0.50(0.14)	0.59(0.11)	0.55(0.13)	0.54(0.15)
K, OS	0.36(0.21)	0.36(0.18)	0.41(0.15)	0.39(0.16)	0.37(0.20)

Table 5. Estimates of input substitutability elasticities (at mean values of output, average DRG weight and input prices) for different cost function models^a

^a Estimated asymptotic standard errors in parentheses. *MS* = Medical Staff, *OS* = Other Staff, *D* = Drugs, *K* = Capital (number of beds).

		Scaling procedure for DRG weight (DRGW)						
	Scaling procedure for the output (Y)	$\lambda_{DRGW} = 0.50$			$\lambda_{DRGW} = 1$ (average value)		$\lambda_{DRGW} = 2$	
MS, K	$\lambda_Y = 0.25$	-1.20	(1.52)	-0.34	(0.51)	0.26	(0.32)	
	$\lambda_Y = 0.50$	-0.42	(0.54)	-0.05	(0.22)	0.26	(0.23)	
	λ_Y = 1 (average value)	0.00	(0.24)	0.14	(0.12)	0.26	(0.16)	
	$\lambda_Y = 2$	0.23	(0.16)	0.26	(0.11)	0.28	(0.16)	
	$\lambda_Y = 3$	0.39	(0.19)	0.34	(0.15)	0.30	(0.19)	
MS, D	$\lambda_Y = 0.25$	-0.75	(0.53)	0.04	(0.14)	0.48	(0.16)	
	$\lambda_Y = 0.50$	-0.19	(0.18)	0.18	(0.08)	0.45	(0.11)	
	λ_Y = 1 (average value)	0.12	(0.08)	0.28	(0.05)	0.42	(0.08)	
	$\lambda_Y = 2$	0.30	(0.07)	0.36	(0.05)	0.40	(0.09)	
	$\lambda_Y = 3$	0.41	(0.12)	0.41	(0.09)	0.41	(0.12)	
MS, OS	$\lambda_Y = 0.25$	1.01	(0.22)	1.01	(0.24)	1.02	(0.29)	
	$\lambda_Y = 0.50$	1.01	(0.24)	1.02	(0.26)	1.02	(0.29)	
	λ_Y = 1 (average value)	1.02	(0.25)	1.02	(0.27)	1.02	(0.29)	
	$\lambda_Y = 2$	1.02	(0.28)	1.02	(0.28)	1.02	(0.29)	
	$\lambda_Y = 3$	1.03	(0.31)	1.02	(0.30)	1.02	(0.29)	
D, K	$\lambda_Y = 0.25$	-1.61	(1.33)	-0.45	(0.43)	0.22	(0.29)	
	$\lambda_Y = 0.50$	-0.64	(0.43)	-0.14	(0.17)	0.22	(0.21)	
	λ_Y = 1 (average value)	-0.14	(0.19)	0.06	(0.10)	0.21	(0.15)	
	$\lambda_Y = 2$	0.14	(0.14)	0.19	(0.11)	0.22	(0.16)	
	$\lambda_Y = 3$	0.31	(0.19)	0.27	(0.16)	0.24	(0.20)	
D, OS	$\lambda_Y = 0.25$	-0.57	(0.58)	0.25	(0.20)	0.68	(0.18)	
	$\lambda_Y = 0.50$	0.00	(0.25)	0.39	(0.15)	0.65	(0.15)	
	λ_Y = 1 (average value)	0.33	(0.17)	0.50	(0.14)	0.63	(0.15)	
	$\lambda_Y = 2$	0.52	(0.16)	0.57	(0.15)	0.62	(0.17)	
	$\lambda_Y = 3$	0.63	(0.19)	0.63	(0.18)	0.62	(0.19)	
K, OS	$\lambda_Y = 0.25$	-1.00	(1.58)	-0.13	(0.57)	0.50	(0.36)	
	$\lambda_Y = 0.50$	-0.21	(0.60)	0.17	(0.29)	0.50	(0.27)	
	λ_Y = 1 (average value)	0.21	(0.31)	0.36	(0.21)	0.50	(0.23)	
	$\lambda_Y = 2$	0.46	(0.24)	0.49	(0.20)	0.51	(0.24)	
	$\lambda_Y = 3$	0.62	(0.26)	0.58	(0.23)	0.53	(0.27)	

Table 6. Estimates of Shadow elasticities of input substitutability by scaled values of the <code>average</code> output and DRG weight (PB $_{\rm G}$ model, average input prices) $^{\rm a}$

^a Estimated asymptotic standard errors in parentheses. Bold typeface values indicate 10% (or lower) significance level. *MS* = Medical Staff, *OS* = Other Staff, *D* = Drugs, *K* = Capital (number of beds).

REGRESSORS ^a	EXTENDED MODEL 1		EXTENDED MODEL 2 FULL EXTENDED MODEL	
Constant	0.997***	$0.957***$	$0.972***$	
Υ	$0.701***$	$0.608***$	$0.577***$	
DRGW	$0.505**$	$0.358***$	$0.590**$	
$ln P_{MS}$	$0.642***$	$0.660***$	$0.636***$	
$ln P_D$	$0.115***$	$0.100***$	$0.118***$	
$ln P_K$	$0.049***$	$0.045***$	$0.049***$	
T	-0.004	$0.020***$	0.021	
Y^2	-0.267	0.056	0.174	
DRGW ²	0.226	$1.151***$	0.947	
T^2	0.006		0.002	
YDRGW	0.576	$0.324***$	$0.340**$	
YT	0.004		0.013	
DRGWT	-0.029		-0.046	
$Y \ln P_{MS}$	-0.003	$-0.023***$	-0.009	
$Y \ln P_D$	0.011	$0.028***$	$0.018**$	
$Y \ln P_K$	0.011	$0.015***$	$0.012**$	
$DRGW$ In P_{MS}	-0.021	$-0.039*$	$-0.035*$	
$DRGW$ In P_D	$0.035***$	$0.036**$	$0.050***$	
$DRGW$ In P_K	0.013	0.022	0.015	
T In P_{MS}	$0.005*$		$0.007**$	
T In P_D	$-0.004*$		$-0.005**$	
T In P_K	-0.001		-0.001	
InP _{Ms} P _{OS}	-0.009	0.010	-0.022	
InP _{Ms} P _D	$-0.059***$	$-0.043***$	$-0.062***$	
InP _{Ms} P _K	$-0.026**$	$-0.030***$	$-0.022**$	
Ln P _{OS} P _D	-0.006	-0.017	-0.003	
Ln P _{OS} P _K	-0.002	0.003	-0.005	
$ln P_D P_K$	-0.011	$-0.012***$	$-0.011*$	
D_M		$0.199***$	$0.182***$	
D_L		$0.218**$	$0.189**$	
D_{AO}		$-0.264***$	$-0.256***$	
OUTBED		$-0.146***$	$-0.140***$	
Box-Cox ϕ	-0.432	0.906***	$0.832***$	
Box-Cox π	$1.247***$	0.479	0.299	
Box-Cox t	-0.144	0.950***	0.890***	
System R^{2b}	0.867	0.896	0.908	

Table 7. NLSUR parameter estimates for extended *Generalised Composite* (PB_G) models

^a The dependent variable is Operating Hospital Cost (*OHC*).
^b The goodness-of-fit measure used for NLSUR systems is McElroy's (1977) *R* ².

*** significant at 1 % level, ** significant at 5 % level, * significant at 10 % level (two-tailed test).

Table 8. Estimates of Shadow elasticities of input substitutability (at mean values of output, average DRG weight and input prices) for different specifications of the PB_G model $^\text{a}$

Shadow elasticities (2 factors, 2 prices)	BASIC MODEL	FULL EXTENDED MODEL	FIXED EFFECTS MODEL	VARIABLE COST MODEL
MS, K	0.14(0.12)	0.15(0.14)	0.21(0.05)	$\overline{}$
MS, D	0.28(0.05)	0.24(0.05)	0.32(0.05)	0.27(0.06)
MS, OS	1.02(0.27)	0.79(0.29)	0.92(0.34)	0.93(0.28)
D, K	0.06(0.10)	0.05(0.11)	0.10(0.05)	\blacksquare
D, OS	0.50(0.14)	0.43(0.15)	0.54(0.14)	0.44(0.13)
K, OS	0.36(0.21)	0.28(0.21)	0.33(0.10)	

a Estimated asymptotic standard errors in parentheses. *MS* = Medical Staff, *OS* = Other Staff, *D* = Drugs, *K* = Capital (number of beds).