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Thermodynamics and fragility of glass-forming alloys

L. Battezzati* and G. Dalla Fontana

Dipartimento di Chimica e Centro NIS, Università di Torino, Via P. Giuria 7, 10125 Torino, Italy
Corresponding Author: livio.battezzati@unito.it, tel 0039 011 6707567, fax 0039 011 6707855.

Abstract
The existing correlation between the extensive properties, \( \Delta H \) and \( \Delta S \), the enthalpy and entropy difference between liquid and crystal phases has been checked to relate metallic glasses to other classes of amorphous materials.

Expressing the specific heat difference, \( \Delta C_p \), of molten and crystalline metallic glass-formers as a function of temperature with different functional trends, parametric expressions of fragility are derived using relevant temperatures for alloys. It is shown that relationships between the \( \Delta S_g / \Delta C_{p,g} \) ratio and such temperatures are useful to estimate unknown quantities when the experimental determination of the specific heat is possible.

Thermodynamic indicators of fragility are compared to the kinetic fragility obtained from viscosity data accounting for the estimated errors on parameters which are derived from extrapolations. The outcome of the analysis indicates that a relationship between thermodynamic and kinetic parameters exists. Moreover a systematic scatter for some alloys indicates a diverse behaviour which can be ascribed to structure modification either in the liquid or in the solid reference state.

Keywords: metallic glasses, amorphous materials, thermodynamic properties, viscosity.
1. Introduction

Since the early times of rapid solidification processing, the formation of metallic glasses from a supercooled melt near deep eutectics showed that it is necessary to meet specific thermodynamic conditions, in addition to a proper quenching technique, to allow survival of the liquid at low temperatures and transform it into a glass.

These requirements are expressed by the trend of extensive properties, $\Delta H$ and $\Delta S$, the enthalpy and entropy difference between liquid and crystal phases which, obviously, will determine the trend of $\Delta G$, the related difference in free energy [1]. The functional form of these quantities versus temperature depends on the specific heat of the liquid and of the solid ($C_p^l$ and $C_p^s$). While the solid specific heat complies to the rule of mixing molar quantities of the elements, the specific heat of the liquid deviates considerably from it having an increasing trend on decreasing temperature. The Potential Energy Landscape (PEL) model suggests this is due to sampling of a varied number of potential energy minima among the vast ensemble of them available in the liquid at every temperature [2]. As a consequence, it might be envisaged the $C_p^l$ curves could be used to study the so-called melt thermodynamic fragility. This concept has been introduced by expressing the rate of entropy loss in the temperature range of the glass transition: a faster rate of entropy loss implies a more rapid change in the number of states sampled by the liquid, therefore termed fragile in contrast to the strong ones having less states available and, consequently, more steady dependence on temperature of entropy [2]. Application of the PEL model has provided insight also into the dynamics of liquids, e. g. structural relaxation times and viscosity, which is equally controlled by the landscape topology showing a correlation between kinetic and thermodynamic properties of glass-formers [3].

Following up an extensive discussion on the specific heat behaviour of metallic glass formers in relation to fragility indicators [4], in this paper we discuss first the correlation between thermodynamic quantities, then we check for simple correlations between thermodynamic and kinetic properties of metallic glass-formers and compare them with those of other melts both
inorganic and organic. The aim is to provide a general frame of “normal” behaviour, possibly usable to estimate quantities for new alloys, and, eventually, find exceptions worth of further investigation in terms of structure of the liquid and of possible transformations of it in the undercooling regime.

2. Correlation between thermodynamic quantities of undercooled melts

The extensive thermodynamic properties of a substance as a function of temperature are correlated, according to the respective dependence on the specific heat \[1\].

\[
\frac{\Delta S_{\ell}}{\Delta S_m} \cdot \frac{\Delta H_{\ell}}{\Delta H_m} = \left(1 - \frac{\gamma_{\ell} \Delta C_{\ell}}{\gamma_m \Delta C_m} \int d\ln T \right) \left(1 - \frac{\gamma_{\ell} \Delta C_{\ell}}{\gamma_m \Delta H_m} \int dT \right)
\]

(1)

For glass-forming alloys the liquid specific heat is higher than that of the corresponding solid. This behaviour is actually general for all classes of glass-formers and leads to enthalpy and entropy loss on undercooling with an envisaged catastrophe when the property equals that of the solid. The long-standing Kauzmann paradox refers to such entropy crisis at the temperature \(T_K\) which is avoided by vitrifying the melt at a glass transition temperature, \(T_g\), kinetically defined \[5\]. At this temperature the extensive thermodynamic quantities are frozen-in with values which can be computed if the specific heat and melting enthalpy of the substance are known from calorimetry measurements. With this in mind it is of interest to exploit the links between properties to estimate the value or range of those which are not amenable to measurement, e. g. the amount of entropy frozen-in at the glass transition.

With the discovery of bulk glass-formers in various alloy systems, data on transition temperatures, heat of fusion and specific heat are now available in the literature. Their quality and scatter has been thoroughly discussed earlier \[4\] motivating a critical selection of data on metallic glasses based on Zr, La, Pd, Cu, Mg, Au and Pt.
The relevant compositions are reported in Tab. 1. For simplicity, in the following graphs each alloy listed in Tab. 1 will be identified only by means of the base element and/or the corresponding number.

For these alloys Fig. 1 shows the correlation between \( \Delta S_g \), the entropy of the liquid frozen-in at the glass transition temperature and the corresponding enthalpy content, \( \Delta H_g \), with both quantities referred to the respective value at the melting (eutectic) point \( \Delta S_m \) and \( \Delta H_m \). The bisector line in the figure corresponds to the case of the difference in specific heat between liquid and crystal phases, \( \Delta C_p \), being nil as reported for some pure elements, at least at high temperature. The area above the bisector line corresponds to the rather unphysical case \( \Delta C_p < 0 \). The points referring to metallic glass-formers cluster in between two limiting lines which were computed by assuming an hyperbolic dependence of \( \Delta C_p \) on temperature between \( T_m \) and \( T_g \) and a \( T_g/T_m \) ratio of \( \frac{1}{2} \) and \( \frac{2}{3} \) expressing the cases for either marginal or good glass-formers, respectively [26]. Should \( \Delta C_p \) be expressed by other functions (e. g. linear, \( T^{-2} \)) lines could be drawn falling very close to these. It should also be noted that the inevitable error in the experimental determination of \( \Delta C_p \) versus temperature will affect \( \Delta S \) and \( \Delta H \) in the same sense because of the correlation expressed by eq.1, but their ratio to a minor extent. In the event that \( T_g \) is close to the crystallization temperature of the glass, \( T_x \), i. e. the materials is a marginal glass-former, the experimental determination of the enthalpy of crystallization, \( \Delta H_x \), will allow the estimate of the residual entropy at the same temperature by using the relative correlation line.

3. The residual entropy at \( T_g \) and fragility parameters

The quantity \( \Delta S_g \) has been thoroughly discussed in the literature on the glass transition. It was suggested at first it should take a “universal” value if expressed per mole of bead, i. e. an appropriate structural unit to be defined by examining the structure of the material. It appeared, however, that this would not hold for substances of different families where diverse contributions to
the total residual entropy could appear and be relevant. This was inferred from the location of points referring to various substances in a plot of $\Delta S_g$ versus $\ln(T_g/T_K)$ [27] where several correlation lines were drawn each implying a constant, or effective, value of $\Delta C_p$ in the temperature range between $T_g$ and $T_K$\textsuperscript{1}. In this context, metallic glasses, for which a “bead” should correspond to every atom in the alloy, appear to align similarly to inorganic glasses, with slope of $\Delta C_p = 18$ J/mol·K, higher than that of polymeric and organic glasses (12.5 J/mol·K) (Fig. 2).

The concept of “bead” has been recently re-used to define the units for molecular motion in the description of the library of possible states in the potential energy landscape (PEL) of the undercooled melt [26, 28] The distribution in energy of such states for “excitable units” in the PEL has been modelled as gaussian, hyperbolic, and logarithmic\cite{3} establishing links between the configurational entropy content of the melt and its dynamic properties, especially viscosity. This connection implies that the viscosity diverges at a temperature $T_0 = T_K$, being expressed by the Vogel-Fulcher-Tammann equation [29]

$$\eta = \eta_\infty \exp\left(\frac{B}{T - T_0}\right)$$

(3)

where $\eta_\infty$ gives the viscosity in the high temperature limit, $B = DT_0$ contains information on the fragility, $D$.

It has been argued that $T_0$ and $T_K$ do not coincide and the latter temperature exceeds the former in dependence of the fragility parameter, $m$ [26],

$$m = \left[\frac{d \log(\eta)}{T_g} \right]_{T = T_g}$$

(4)

In Fig. 3 the $T_K/T_0$ ratio is plotted versus $m$ [7] for metallic glasses and the substances, mostly organic, listed in the Table available online [26]. Although on average the points actually lie above unity, no clear trend is discernible. At present, it cannot be stated with certainty whether this

\textsuperscript{1} The plot stems from $\Delta S_K = 0 = \Delta S_g - \Delta C_p \ln(T_g/T_K)$.

\[(2)\]
expresses a departure from the common assumption that $T_K = T_0$, considering also the deviation associated to both temperatures (see the estimated scatter of the ordinate) which are obtained by extrapolation of either the entropy or the viscosity to ranges where experiments cannot provide direct measurement of properties.

The early assumption of a constant value of $\Delta C_p$ in the temperature range between $T_g$ and $T_K$ appears limiting to date also in view of the models of the number of states in the PEL which are constructed by taking $\Delta C_p$ dependent on temperature as $T^{-n}$ with $n$ of order 1 and 2 [26]. With $n = 1$, the modified relationship (with respect to that expressed by Fig. 2) is expressed by

$$\frac{\Delta S_g}{\Delta C_{p,g}} = \frac{T_g - T_s}{T_K} \quad (5)$$

as shown in Fig. 4. The correlation appears enhanced in comparison to Fig. 2. Here again the caveat holds, as stated above, on the error in determining $\Delta C_p$ versus temperature which affects both $\Delta S_g$ and $T_K$. In spite of this, should $\Delta S_g$, $\Delta C_{p,g}$ and $T_g$ be known from independent experiments or calculations, $T_K$ could be estimated from the plot.

The left hand side of eq. 5 is the inverse of the exact expression of the thermodynamic fragility parameter, $m_T$ [26, 3], defined as:

$$m_T = \left[ \frac{d \Delta S}{d \frac{T_s}{T}} \right]_{T = T_g} \quad (6).$$

Assuming an hyperbolic distribution of the states in the PEL of the melt, it was derived that

$$m_T + 1 = \frac{m}{17} = \frac{T_g}{T_g - T_K}$$

therefore the right hand side (rhs) of eq. 5 equals $1/(m_T - 1)$. Fig. 4 results then a representation of the melt fragility within such assumption.

A parallel conclusion is obtained by assuming $n = 2$ and obtaining
In this case the rhs of eq. 7 becomes \( 1/(m_T-1) \) when it is posed \( m_T + 1 = \frac{T_g^2 + T_k^2}{T_k^2 - T_g^2} \) \[3\], as a consequence of assuming a gaussian distribution of the states in the PEL of the melt. The corresponding plot does not add information with respect to the previous one and is not reported here.

4. Link with kinetic fragility parameters

Analyzing in detail the values of the quantities reported in Fig. 4 it appears that some \( \Delta S_g/\Delta C_{p,g} \) ratios are unrealistically too low, or that some \( \Delta C_{p,g} \)'s are too high for an undercooled liquid phase. This is likely due to extrapolation of high temperature data to the inaccessible range. For the sake of comparison, although with the warning of the deviation shown in Fig. 3, an analogous plot as been constructed by substituting the \( T_0 \) obtained by fitting viscosity data for \( T_K \) (Fig. 5). As expected, the scatter of point is large, although a correlation is still recognized. It is seen that most of the points just mentioned are displaced with respect to the correlation line. Others fall clearly off any conceivable correlation suggesting that the data should be reconsidered, possibly with new and more extended experiments. A further hint in this sense will be given at the end of this paragraph.

The \( T_0 \) temperature is also derived from data extrapolation and therefore carries a substantial uncertainty. It, however, has been shown to correlate rather nicely with the \( B \) parameter \[13\] in eq. 3. Since the pre-exponential factor of viscosity is of the order of \( 10^5 \) Pa·s in most cases and the viscosity at \( T_g \) is conventionally taken as \( 10^{12} \) Pa·s, the \( B \) and \( T_0 \) parameters are related by \( \ln 17 = B/(T_g - T_0) \). This is confirmed for the ensemble of alloys examined in this work by the plot of Fig. 6. In the event that the viscosity can be expressed by eq. 3, the dynamic fragility parameter \( m \) defined in eq. 4 is given by
\[ m = BT_g \left[ 2.3(T_g - T_0) \right] \]  

(8)

and, therefore, the knowledge derived from either experiments or calculation, of any of the \( m, B, \)
and \( T_0 \) parameters will allow deriving the others.

An empirical formula [26] to compute \( m \) using thermodynamic quantities accessible to experiments
has proved rather accurate for various inorganic and organic substances

\[ m = 56 \frac{T_i \Delta C_{p,g}}{\Delta H_m} \]  

(9).

Application of eq. 9 to metallic glasses shows that the general trend is followed, although with large
scatter especially for some compositions (Fig. 7). The deviation from the mainstream behaviour
appear useful, however, to pinpoint materials for which the above formula is not applicable either
because of scatter in the experimental data or, more interestingly, because of inherent structural
modifications: e. g. a ring-chain equilibrium in the liquid state of sulphur and selenium gives an
extra contribution to the specific heat of the melt which is not accounted for in eq. 9. In the case of
metallic glasses the largest deviation is for the \( \text{Au}_{77}\text{Ge}_{13.6}\text{Si}_{19.4} \) glass-forming melt. Here, \( \Delta C_{p,g} \)
refers to the transition from the metallic glass to the metallic undercooled liquid, whereas \( \Delta H_m \)
refers to that from a crystalline mixture containing a large amount of semiconducting Si to a
metallic liquid. The deviation suggests that the heat of fusion of the alloy should be corrected for
the heat of transformation of Si from semiconducting to metallic crystal in order to use eq. 9
properly. Other transitions may also occur in the melt giving liquid polyamorphism [30]. For
metallic glass formers this has not yet been fully proven even if a volume transition has been
recently revealed by containerless undercooling in three Zr-based melts [31].

5. Conclusions

This work is devoted to the analysis of thermodynamic and dynamic properties of metallic melts in
comparison with other glass formers. Using the specific heat data now available for bulk metallic
glasses, the correlation between extensive properties has been checked for the limiting cases of marginal and good glass-formers.

Simple relationships between the $\Delta S_g/\Delta C_{p,g}$ ratio and relevant temperatures for the glass have been derived and shown to correspond to those obtained with either hyperbolic or gaussian distribution of the states in the PEL of the melt. These correlations appear useful to estimate unknown quantities when the experimental determination of the specific heat is possible.

The link between thermodynamic and dynamic properties was established by posing $T_K = T_0$. Although this is debated in the literature, it has been shown that the assumption appear reasonable in the present context of available data and scatter. The usefulness of this position stems also from the strong correlation existing between $T_0$ and the B parameter in the VFT expression of viscosity.

The use of the Wang-Richet-Angell formula (eq. 9) has further shown that metallic glasses comply to the general behaviour of glass formers and has allowed to pinpoint exceptions due to peculiar transformations occurring either in the liquid or in the solid reference state.

The set of observations made in this work indicate that not only more accurate thermodynamic data are needed for metallic glass-formers, but also that careful search for structure modification in some specific systems will provide advances in the knowledge of such undercooled melts.

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References

Figure captions

Fig. 1. The correlation between $\Delta S_g$, the entropy of the liquid frozen-in at the glass transition temperature and the corresponding enthalpy, $\Delta H_g$. Both quantities are referred to the respective value at the melting (eutectic) point $\Delta S_m$ and $\Delta H_m$. Meaning of lines is given in the text. Black and white circles refer to organic and inorganic glass formers (see supplementary information online).

Fig. 2. Plot of $\Delta S_g$ versus $\ln(T_g/T_K)$. The lines express the correlation between the quantities on the axes when a constant $\Delta C_p$ is assumed [27] with values of 17.4 J/mol·K and 12.5 J/mol·K. Numbers correspond to the alloys listed in Tab. 1.

Fig. 3. The ratio of $T_K$ to $T_0$ for various glass formers as a function of the kinetic fragility parameter, $m$, as obtained with different techniques. Symbols as in Fig. 1, numbers as in Fig. 2.

Fig. 4. The $\Delta S_g/\Delta C_{p,g}$ ratio versus $(T_g-T_K)/T_K$. Symbols as in Fig. 1, numbers as in Fig. 2

Fig. 5. The $\Delta S_g/\Delta C_{p,g}$ ratio versus $(T_g-T_0)/T_0$. Symbols as in Fig. 1, numbers as in Fig. 2

Fig. 6. The correlation between the $B$ parameter in the VFT equation and $(T_g - T_0)$ for the alloys listed in Table 1. Symbols as in Fig. 1, numbers as in Fig. 2

Fig. 7. Plot of $m_{calc}$ calculated according to eq. 9 versus the measured $m$ fragility parameter for metallic glasses. The insert reports the same plot for the organic and inorganic glass formers (see supplementary information online). Symbols as in Fig. 1, numbers as in Fig. 2
Table captions:

Tab.1. List of glassy metallic alloys and their thermal properties.

Supplementary information online.
Tab. 1. List of organic and inorganic glasses and references to their thermal properties.

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Fig. 1
Fig. 2

A scatter plot showing the relationship between $\Delta S_g$ and $\ln \left( \frac{T_g}{T_k} \right)$. Different symbols represent different elements: Zr, La, Cu, Mg, Pd, Pt, and Au. Each point is labeled with a number from 1 to 18, indicating specific data points for each element.
Fig. 3
Fig. 4

The graph shows the relationship between $\Delta S_g / \Delta C_{p_g}$ and $(T_g - T_k)/T_k$. Different symbols represent different materials, such as Ref.[26], Zr, La, Cu, Mg, Pd, Pt, and Au.
Fig. 5

![Graph showing the relationship between $\Delta S_g/\Delta C_p_g$ and $(T_g-T_0)/T_0$. The graph includes data points for various elements labeled with Ref.[26], Zr, La, Cu, Mg, Pd, Pt, and Au, and numbers 1 to 18.]
Fig. 6

- Glassy alloys
- Ref. [26]