# Production of the excited charm mesons $D_{1}$ and $D_{2}^{*}$ at HERA 

## ZEUS Collaboration

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#### Abstract

The production of the excited charm mesons $D_{1}(2420)$ and $D_{2}^{*}(2460)$ in $e p$ collisions has been measured with the ZEUS detector at HERA using an integrated luminosity of $373 \mathrm{pb}^{-1}$. The masses of the neutral and charged states, the widths of the neutral states, and the helicity parameter of $D_{1}(2420)^{0}$ were determined and compared with other measurements and with theoretical expectations. The measured helicity parameter of the $D_{1}^{0}$ allows for some mixing of $S$ - and $D$-waves in its decay to $D^{* \pm} \pi^{\mp}$. The result is also consistent with a pure $D$-wave decay. Ratios of branching fractions of the two decay modes of the $D_{2}^{*}(2460)^{0}$ and $D_{2}^{*}(2460)^{ \pm}$states were measured and compared with previous measurements. The fractions of charm quarks hadronising into $D_{1}$ and $D_{2}^{*}$ were measured and are consistent with those obtained in $e^{+} e^{-}$annihilations.


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## 1. Introduction

The production of the well-established ground-state charm mesons $D$ and $D^{*}$ has been extensively studied in ep collisions at HERA. The large charm production cross section at HERA makes it possible to also investigate the excited charm-meson states. In a previous ZEUS analysis [1], with an integrated luminosity of $126 \mathrm{pb}^{-1}$, the orbitally excited states $D_{1}(2420)^{0}$ with $J^{P}=1^{+}$and $D_{2}^{*}(2460)^{0}$ with $J^{P}=2^{+}$were studied in the decay modes ${ }^{61}$ $D_{1}(2420)^{0} \rightarrow D^{*}(2010)^{+} \pi^{-}$and $D_{2}^{*}(2460)^{0} \rightarrow D^{*}(2010)^{+} \pi^{-}, D^{+} \pi^{-}$. The width of the $D_{1}^{0}$ was found to be significantly above the 2008 world-average value [2]. A study of the helicity angular distribution of the $D_{1}(2420)^{0}$ gave results that were consistent with some $S$-wave admixture in the decay $D_{1}^{0} \rightarrow D^{*+} \pi^{-}$, contrary to Heavy Quark Effective Theory (HQET) predictions [3,4] and to previous experimental results [5] which had yielded a pure $D$-wave decay in this channel.

In this paper the analysis was repeated with an independent data sample of higher integrated luminosity. In addition the production of the charged excited charm mesons $D_{1}(2420)^{+}$ and $D_{2}^{*}(2460)^{+}$was studied for the first time at HERA in the decay modes $D_{1}(2420)^{+} \rightarrow$ $D^{*}(2007)^{0} \pi^{+}$and $D_{2}^{*}(2460)^{+} \rightarrow D^{*}(2007)^{0} \pi^{+}, D^{0} \pi^{+}$. For both the neutral and charged excited charm mesons the study also includes a measurement of fragmentation fractions and ratios of the $D_{2}^{*}$ branching fractions.

The analysis was performed using data taken from 2003 to 2007, when HERA collided electrons or positrons at 27.5 GeV with protons at 920 GeV . The data correspond to an integrated luminosity of $373 \mathrm{pb}^{-1}$. The upgraded ZEUS detector included a microvertex detector, allowing the measurement of the decay vertex of charm mesons. In particular, the signal-to-background ratio was significantly improved for the $D^{+}$meson, which has the highest lifetime among the charm hadrons.

To maximise the statistics, both photoproduction and deep inelastic scattering events were used in this analysis. Events produced in the photoproduction regime contributed 70-80\% of the selected charm-meson samples.

## 2. Experimental set-up

A detailed description of the ZEUS detector can be found elsewhere [6]. A brief outline of the components that are most relevant for this analysis is given below.

In the kinematic range of the analysis, charged particles were tracked in the central tracking detector (CTD) [7] and the microvertex detector (MVD) [8]. These components operated in a magnetic field of 1.43 T provided by a thin superconducting solenoid. The CTD consisted of 72 cylindrical drift-chamber layers, organised in nine superlayers covering the polar-angle ${ }^{62}$

[^2]region $15^{\circ}<\theta<164^{\circ}$. The MVD silicon tracker consisted of a barrel (BMVD) and a forward (FMVD) section. The BMVD contained three layers and provided polar-angle coverage for tracks from $30^{\circ}$ to $150^{\circ}$. The four-layer FMVD extended the polar-angle coverage in the forward region to $7^{\circ}$. After alignment, the single-hit resolution of the MVD was $24 \mu \mathrm{~m}$. The transverse distance of closest approach (DCA) of tracks to the nominal vertex in the $X-Y$ plane was measured to have a resolution, averaged over the azimuthal angle, of $\left(46 \oplus 122 / p_{T}\right) \mu \mathrm{m}$, with $p_{T}$ in GeV . For CTD-MVD tracks that pass through all nine CTD superlayers, the momentum resolution was $\sigma\left(p_{T}\right) / p_{T}=0.0029 p_{T} \oplus 0.0081 \oplus 0.0012 / p_{T}$, with $p_{T}$ in GeV .

The high-resolution uranium-scintillator calorimeter (CAL) [9] consisted of three parts: the forward (FCAL), the barrel (BCAL) and the rear (RCAL) calorimeters. Each part was subdivided transversely into towers and longitudinally into one electromagnetic section (EMC) and either one (in RCAL) or two (in BCAL and FCAL) hadronic sections (HAC). The smallest subdivision of the calorimeter was called a cell. The CAL energy resolutions, as measured under test-beam conditions, were $\sigma(E) / E=0.18 / \sqrt{E}$ for electrons and $\sigma(E) / E=0.35 / \sqrt{E}$ for hadrons, with $E$ in GeV .

The luminosity was measured using the Bethe-Heitler reaction $e p \rightarrow e \gamma p$ by detector which consisted of an independent lead-scintillator calorimeter [10] and a magnetic spectrometer [11] system.

## 3. Event simulation

Monte Carlo (MC) samples of charm and beauty events were produced with the Pythia 6.221 [12] and the RAPGAP 3.000 [13] event generators. The generation included direct photon processes, in which the photon couples directly to a parton in the proton, and resolved photon processes, where the photon acts as a source of partons, one of which participates in the hard scattering process. The CTEQ5L [14] and the GRV LO [15] parametrisations were used for the proton and photon parton density functions, respectively. The charm- and beauty-quark masses were set to 1.5 GeV and 4.75 GeV , respectively. The masses and widths for charm mesons were set to the latest PDG [16] values.

Events for all processes were generated in proportion to the respective MC cross sections. The Lund string model was used for hadronisation in Pythia and Rapgap. The Bowler modification [17] of the Lund symmetric fragmentation function [18] was used for the charm- and beauty-quark fragmentation.

The Pythia and Rapgap generators were tuned to describe the photoproduction and the deep inelastic scattering regimes, respectively [1]. Subsequently, the PYTHIA events, generated with $Q^{2}<1.5 \mathrm{GeV}^{2}$, were combined with the RAPGAP events, generated with $Q^{2}>1.5 \mathrm{GeV}^{2}$, where $Q^{2}$ is the exchanged-photon virtuality.

The generated events were passed through a full simulation of the detector using GEANT 3.13 [19] and processed with the same reconstruction program as used for the data.

## 4. Event selection and reconstruction of ground-state charm mesons

The ZEUS trigger chain had three levels [6,20,21]. The first- and second-level trigger used CAL and CTD data to select ep collisions and to reject beam-gas events. At the third-level trigger, the full event information was available. All relevant trigger chains were used for the data. Triggers that required the presence of a reconstructed $D^{*+} \rightarrow D^{0} \pi^{+} \rightarrow\left(K^{-} \pi^{+}\right) \pi^{+}$or $\left(K^{-} \pi^{+} \pi^{-} \pi^{+}\right) \pi^{+}, D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$or $D^{0} \rightarrow K^{-} \pi^{+}$candidate constituted a major fraction
of the selected events. However, events missed by these triggers but selected with other trigger branches were also used in the analysis. Applying, in the MC, either no trigger selection cuts or requiring at least one trigger chain to be passed did not affect the final measurements.

To ensure high purity in the event sample, the $Z$ position of the primary vertex, reconstructed from CTD and MVD tracks, had to be within $\left|Z_{\mathrm{vtx}}\right|<30 \mathrm{~cm}$. All charm mesons were reconstructed with tracks measured in the CTD and MVD. All tracks were required to have a transverse momentum, $p_{T}$, above 0.1 GeV , to start not further out than the first CTD superlayer and to reach at least the third superlayer. The tracks were assigned either to the reconstructed primary vertex or to a secondary decay vertex associated with the weak decay of a charm meson, $D^{+}$or $D^{0}$. To ensure the use of well reconstructed MVD tracks, all tracks associated with the secondary vertex were required to have at least two BMVD measurements in the $X-Y$ plane and two in the $Z$ direction.

The decay-length significance is a powerful tool for rejection of combinatorial background. It is defined as $S=l / \sigma_{l}$, where the decay length $l$ is the distance in the transverse plane between the production point and the decay vertex of a candidate charm meson projected on its momentum direction and $\sigma_{l}$ is the uncertainty of this quantity [22]. The quantity $S$ is positive when the angle between the particle momenta and the direction from primary to secondary vertex is less than $\pi / 2$; it is negative otherwise. The $S$ distribution is asymmetric around zero, with a stronger positive contribution coming mostly from the charm mesons. The contributions to negative $S$ values are due to background and resolution effects.

The combinatorial background was suppressed by selecting events above a minimum value of the ratio $p_{T}(D) / E_{\perp}^{\theta>10^{\circ}}$, where $D$ denotes $D^{*+}, D^{+}$or $D^{0}$ and $E_{\perp}^{\theta>10^{\circ}}$ is the transverse energy measured using all CAL cells outside a cone of $10^{\circ}$ around the forward direction. In addition, to reduce background, the $d E / d x$ values measured in the CTD of track candidates originating from the $D$ mesons were used. The parametrisation of the $d E / d x$ expectation values and the $\chi^{2}$ probabilities $l_{K}$ and $l_{\pi}$ of the kaon and pion hypotheses, respectively, were obtained as described in previous analyses [23,24]. The cuts $l_{K}>0.03$ and $l_{\pi}>0.01$ were applied.

## 4.1. $D^{*+}$ reconstruction

$D^{*+}$ mesons were identified via the decay modes $D^{*+} \rightarrow D^{0} \pi_{s}^{+} \rightarrow\left(K^{-} \pi^{+}\right) \pi_{s}^{+}$and $D^{*+} \rightarrow$ $D^{0} \pi_{s}^{+} \rightarrow\left(K^{-} \pi^{+} \pi^{-} \pi^{+}\right) \pi_{s}^{+}$, where $\pi_{s}$ is a low-momentum ("soft") pion due to the small mass difference between $D^{*+}$ and $D^{0}$. Tracks were combined to form $D^{0}$ candidates by calculating the invariant-mass combinations $M(K \pi)$ or $M(K \pi \pi \pi)$ with total charge zero. $D^{*+}$ candidates were formed by adding a soft pion, $\pi_{s}$, with opposite charge to that of the kaon. Combinatorial background was reduced by applying cuts as detailed in Table 1.

The mass differences $\Delta M=M\left(K \pi \pi_{s}\right)-M(K \pi)$ and $\Delta M=M\left(K \pi \pi \pi \pi_{s}\right)-M(K \pi \pi \pi)$ were calculated for the $D^{*+}$ candidates that passed the cuts of Table 1. Fig. 1 shows the $\Delta M$ distributions for these $D^{*+}$ candidates. Clean peaks are seen at the nominal value of $M\left(D^{*+}\right)-$ $M\left(D^{0}\right)$ [16].

The $\Delta M$ distributions were fitted to a sum of a background function and a modified Gaussian function [1]. The fit yielded ${ }^{63} D^{*+}$ signals of $64988 \pm 430$ candidates for $D^{0} \rightarrow K \pi$ and $24441 \pm 310$ candidates for $D^{0} \rightarrow K \pi \pi \pi$. The fitted mass differences were $145.400 \pm$ 0.003 MeV and $145.420 \pm 0.003 \mathrm{MeV}$ respectively, in agreement with the PDG average

63 The number of signal candidates was obtained as an integral of the fitted modified Gaussian function over the fit range.

Table 1
Cuts on $D^{*+} \rightarrow D^{0} \pi_{s}^{+}$candidates for the decay channels $D^{0} \rightarrow K^{-} \pi^{+}$and $D^{0} \rightarrow$ $K^{-} \pi^{+} \pi^{+} \pi^{-}$.

| Variable | $D^{0} \rightarrow K^{-} \pi^{+}$ | $D^{0} \rightarrow K^{-} \pi^{+} \pi^{+} \pi^{-}$ |
| :--- | :--- | :--- |
| $p_{T}(K)(\mathrm{GeV})$ | $>0.45$ | $>0.3$ |
| $p_{T}(\pi)(\mathrm{GeV})$ | $>0.45$ | $>0.3$ |
| $p_{T}\left(\pi_{s}\right)(\mathrm{GeV})$ | $>0.1$ | $>0.1$ |
| $p_{T}\left(D^{*+}\right)(\mathrm{GeV})$ | $>1.5$ | $>3$ |
| $\left\|\eta\left(D^{*+}\right)\right\|$ | $<1.6$ | $<1.6$ |
| $p_{T}\left(D^{*+}\right) / E_{\perp}^{\theta>10^{\circ}}$ | $>0.12$ | $>0.18$ |
| $M\left(D^{0}\right)(\mathrm{GeV})$ for | $1.83-1.90$ | $1.84-1.89$ |
| $p_{T}\left(D^{*+}\right)<3.25 \mathrm{GeV}$ |  |  |
| $M\left(D^{0}\right)(\mathrm{GeV})$ for | $1.82-1.91$ | $1.84-1.89$ |
| $3.25<p_{T}\left(D^{*+}\right)<5 \mathrm{GeV}$ |  | $1.84-1.89$ |
| $M\left(D^{0}\right)(\mathrm{GeV})$ for | $1.81-1.92$ |  |
| $5<p_{T}\left(D^{*+}\right)<8 \mathrm{GeV}$ |  | $1.84-1.89$ |
| $M\left(D^{0}\right)(\mathrm{GeV})$ for | $1.80-1.93$ |  |
| $p_{T}\left(D^{*+}\right)>8 \mathrm{GeV}$ |  |  |

value [16]. Only $D^{*+}$ candidates with $0.144<\Delta M<0.147 \mathrm{GeV}$ were used for the excited charm mesons analysis.

## 4.2. $D^{+}$reconstruction

$D^{+}$mesons were reconstructed from the decay $D^{+} \rightarrow K^{-} \pi^{+} \pi^{+}$with looser kinematic cuts than in the previous analysis [1], made possible by the cleaner identification with the MVD. For each event, track pairs with equal charge and pion mass assignment were combined with a track with opposite charge with a kaon mass assignment to form a $D^{+}$candidate. These tracks were refitted to a common decay vertex, and the invariant mass, $M(K \pi \pi)$, was calculated. The $K$ and $\pi$ tracks were required to have transverse momentum $p_{T}^{K}>0.5 \mathrm{GeV}$ and $p_{T}^{\pi}>0.35 \mathrm{GeV}$ and the distance of closest approach between each pair of the three tracks was required to be less than 0.3 cm . To suppress combinatorial background, the following cuts were applied:

- $\cos \theta^{*}(K)>-0.75$, where $\theta^{*}(K)$ is the angle between the kaon in the $K \pi \pi$ rest frame and the $K \pi \pi$ line of flight in the laboratory frame;
- the decay vertex position was fitted with a global vertex fit [25] and the $\chi^{2}$ of the fit was less than 10;
- the decay-length significance, $S\left(D^{+}\right)$, was greater than 3 .

Background from $D^{*+}$ decays was removed by requiring $M(K \pi \pi)-M(K \pi)>0.15 \mathrm{GeV}$. Background from $D_{s}^{+} \rightarrow \phi \pi, \phi \rightarrow K^{+} K^{-}$was suppressed by requiring that the invariant mass of any two $D^{+}$decay candidate tracks with opposite charge should be outside $\pm 8 \mathrm{MeV}$ around the nominal $\phi$ mass when the kaon mass was assigned to both tracks. $D^{+}$candidates in the kinematic range $p_{T}\left(D^{+}\right)>2.8 \mathrm{GeV}$ and $\left|\eta\left(D^{+}\right)\right|<1.6$ were kept for further analysis.

Fig. 2(a) shows the $M\left(K^{-} \pi^{+} \pi^{+}\right)$distribution for $D^{+}$candidates after the cuts. A clear signal is seen at the nominal value of the $D^{+}$mass [16]. The mass distribution was fitted to a sum of a modified Gaussian function and a polynomial background. The fit yielded ${ }^{63}$ a $D^{+}$signal of $39283 \pm 452$ events and a $D^{+}$mass of $1869.1 \pm 0.1 \mathrm{MeV}$, in agreement with the PDG average

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Fig. 1. The distribution of the mass difference (dots), (a) $\Delta M=M\left(K \pi \pi_{s}\right)-M(K \pi)$ and (b) $\Delta M=M\left(K \pi \pi \pi \pi_{s}\right)-$ $M(K \pi \pi \pi)$. The solid curves are fits to the sum of a modified Gaussian function and a background function (dashed lines). Candidates from the shaded area, $0.144-0.147 \mathrm{GeV}$, are used for the analysis of excited charm mesons.
value [16]. Only $D^{+}$candidates with $1.85<M(K \pi \pi)<1.89 \mathrm{GeV}$ were used for the excited charm mesons analysis.

## 4.3. $D^{0}$ reconstruction

$D^{0}$ mesons were reconstructed from the decay $D^{0} \rightarrow K^{-} \pi^{+}$. For each event, two tracks with opposite charge and $K$ and $\pi$ mass assignments, respectively, were combined to form a $D^{0}$ candidate. These tracks were refitted to a common decay vertex, and the invariant mass, $M(K \pi)$, was calculated. Both tracks were required to have transverse momentum $p_{T}^{K}>0.5 \mathrm{GeV}$ and $p_{T}^{\pi}>0.7 \mathrm{GeV}$ and the distance of closest approach between these tracks was required to be less than 0.1 cm . To suppress combinatorial background, the following cuts were applied:

- $\left|\cos \theta^{*}(K)\right|<0.85$, where $\theta^{*}(K)$ is the angle between the kaon in the $K \pi$ rest frame and the $K \pi$ line of flight in the laboratory frame;
- the decay vertex position was fitted with a global vertex fit [25] and the $\chi^{2}$ of the fit was less than 20;
- the decay-length significance, $S\left(D^{0}\right)$, was bigger than 0 .
$D^{0}$ candidates in the kinematic range $p_{T}\left(D^{0}\right)>2.6 \mathrm{GeV}$ and $\left|\eta\left(D^{0}\right)\right|<1.6$ were kept for further analysis.

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Fig. 2. The mass distributions (dots), (a) $M\left(K^{-} \pi^{+} \pi^{+}\right)$for events with significance $S>3$ and (b) $M\left(K^{-} \pi^{+}\right)$for events with significance $S>0$. The solid curves are fits to the sum of a modified Gaussian and a background function (dashed lines) and for (b) including also a contribution from a second broad modified Gaussian representing a reflection (see text). Candidates from the shaded areas, (a) $1.85-1.89 \mathrm{GeV}$ and (b) $1.845-1.885 \mathrm{GeV}$, are used for the analysis of excited charm mesons.

Fig. 2(b) shows the $M\left(K^{-} \pi^{+}\right)$distribution for $D^{0}$ candidates after the cuts. A clear signal is seen at the nominal value of the $D^{0}$ mass [16]. The mass distribution was fitted to a sum of a modified Gaussian function, a broad modified Gaussian representing the reflection produced by $D^{0}$ mesons with the wrong (opposite) kaon and pion mass assignment and a polynomial background. For the reflection, the shape parameters of the broad modified Gaussian were obtained from a study of the MC signal sample and the normalisation (integral) was set equal to that of the other modified Gaussian. The fit yielded ${ }^{63}$ a $D^{0}$ signal of $145740 \pm 2944$ events and a $D^{0}$ mass of $1864.1 \pm 0.1 \mathrm{MeV}$ which is 0.8 MeV lower than the PDG average value [16]. This deviation does not affect any of the results of the excited charm mesons. Only $D^{0}$ candidates with $1.845<M(K \pi \pi)<1.885 \mathrm{GeV}$ were used for the excited charm mesons analysis.

## 5. $D_{1}$ and $D_{2}^{*}$ reconstruction

### 5.1. Reconstruction of the $D_{1}(2420)^{0}$ and $D_{2}^{*}(2460)^{0}$ mesons

The $D_{1}(2420)^{0}$ and $D_{2}^{*}(2460)^{0}$ mesons were reconstructed in the decay mode $D^{*+} \pi^{-}$by combining each $D^{*+}$ candidate with an additional track, assumed to be a pion $\left(\pi_{a}\right)$, with a charge opposite to that of the $D^{*}$. Combinatorial background was reduced by applying the following cuts:

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Fig. 3. The mass distributions (dots), (a) $M\left(D^{*+} \pi_{a}\right)$ and (b) $M\left(D^{+} \pi_{a}\right)$. The solid curves are the result of a simultaneous fit to (a) $D_{1}^{0}$ and $D_{2}^{* 0}$ and to (b) $D_{2}^{* 0}$ and feed-downs plus background function (dashed curves). The contributions of the wide states $D_{1}(2430)^{0}$ and $D_{0}^{*}(2400)^{0}$ are given between the dashed and dotted curves. The lowest curves are the contributions of the $D_{1}^{0}, D_{2}^{* 0}$ and feed-downs to the fit.

- $p_{T}\left(\pi_{a}\right)>0.15 \mathrm{GeV}$;
- $\eta\left(\pi_{a}\right)<1.1$;
- $p_{T}\left(D^{*+} \pi_{a}\right) / E_{\perp}^{\theta>10^{\circ}}>0.25(0.30)$ for the $D^{0} \rightarrow K \pi\left(D^{0} \rightarrow K \pi \pi \pi\right)$ channel;
- $\cos \theta^{*}\left(D^{*+}\right)<0.9$, where $\theta^{*}\left(D^{*+}\right)$ is the angle between the $D^{*+}$ in the $D^{*+} \pi_{a}$ rest frame and the $D^{*+} \pi_{a}$ line of flight in the laboratory frame;
- the cut $l_{\pi}>0.01$ was applied for $\pi_{a}$.

For each excited charm-meson candidate, the "extended" mass difference, $\Delta M^{\text {ext }}=$ $M\left(K \pi \pi_{s} \pi_{a}\right)-M\left(K \pi \pi_{s}\right)$ or $\Delta M^{\mathrm{ext}}=M\left(K \pi \pi \pi \pi_{s} \pi_{a}\right)-M\left(K \pi \pi \pi \pi_{s}\right)$, was calculated. Fig. 3(a) shows the invariant mass $M\left(D^{*+} \pi_{a}\right)=\Delta M^{\mathrm{ext}}+M\left(D_{\mathrm{PDG}}^{*+}\right)$, where $M\left(D_{\mathrm{PDG}}^{*+}\right)$ is the nominal $D^{*+}$ mass [16]. A clear signal in the $D_{1}^{0} / D_{2}^{* 0}$ mass region is seen.

The $D_{2}^{*}(2460)^{0}$ was also reconstructed in the decay mode $D_{2}^{*}(2460)^{0} \rightarrow D^{+} \pi^{-}$by combining each $D^{+}$candidate with an additional track, assumed to be a pion $\pi_{a}$, with a charge opposite to that of the $D^{+}$. Combinatorial background was reduced by applying the following cuts:

- $p_{T}\left(\pi_{a}\right)>0.3 \mathrm{GeV}$;
- $\eta\left(\pi_{a}\right)<1.5$;
- $p_{T}\left(D^{+} \pi_{a}\right) / E_{\perp}^{\theta>10^{\circ}}>0.35$;
- $\cos \theta^{*}\left(D^{+}\right)<0.8$, where $\theta^{*}\left(D^{+}\right)$is the angle between the $D^{+}$in the $D^{+} \pi_{a}$ rest frame and the $D^{+} \pi_{a}$ line of flight in the laboratory frame;
- the cut $l_{\pi}>0.01$ was applied for $\pi_{a}$.

The $D_{2}^{*}(2460)^{0} \rightarrow D^{+} \pi^{-}$decay mode was reconstructed by calculating the "extended" mass difference $\Delta M^{\text {ext }}=M\left(K \pi \pi \pi_{a}\right)-M(K \pi \pi)$. Fig. 3(b) shows the invariant mass $M\left(D^{+} \pi_{a}\right)=$ $\Delta M^{\text {ext }}+M\left(D_{\mathrm{PDG}}^{+}\right)$, where $M\left(D_{\mathrm{PDG}}^{+}\right)$is the nominal $D^{+}$mass [16]. A clear $D_{2}^{* 0}$ signal is seen. No indication of the $D_{1}^{0} \rightarrow D^{+} \pi^{-}$decay is seen, as expected from angular momentum and parity conservation for a $J^{P}=1^{+}$state. The various contributions to the mass spectrum will be discussed below.

### 5.2. Reconstruction of the $D_{1}(2420)^{+}$and $D_{2}^{*}(2460)^{+}$mesons

The charged excited meson $D_{1}(2420)^{+}$has been seen [16] in the decay modes $D^{* 0} \pi^{+}$and $D^{+} \pi^{+} \pi^{-}$and the charged excited meson $D_{2}^{*}(2460)^{+}$has been seen [16] in the decay modes $D^{* 0} \pi^{+}$and $D^{0} \pi^{+}$. A search for $D_{1}^{+}$and $D_{2}^{*+}$ signals was performed in the mass distribution $M\left(D^{0} \pi^{+}\right)$. For the $D_{1}^{+}$a possible $D^{0} \pi^{+}$signal can arise only via a feed-down contribution (see Section 6). Each $D^{0}$ candidate was combined with an additional track, assumed to be a pion $\left(\pi_{a}\right)$, with either positive or negative charge. Combinatorial background was reduced by applying the following cuts:

- $p_{T}\left(\pi_{a}\right)>0.35 \mathrm{GeV}$;
- $\eta\left(\pi_{a}\right)<1.6$;
- $p_{T}\left(D^{0} \pi_{a}\right) / E_{\perp}^{\theta>10^{\circ}}>0.3$;
- $\cos \theta^{*}\left(D^{0}\right)<0.85$, where $\theta^{*}\left(D^{0}\right)$ is the angle between the $D^{0}$ in the $D^{0} \pi_{a}$ rest frame and the $D^{0} \pi_{a}$ line of flight in the laboratory frame;
- the cut $l_{\pi}>0.01$ was applied for $\pi_{a}$.

For each excited charm-meson candidate, the "extended" mass difference $\Delta M^{\mathrm{ext}}=M\left(K \pi \pi_{a}\right)-$ $M(K \pi)$ was calculated. Fig. 4 shows the invariant mass $M\left(D^{0} \pi_{a}\right)=\Delta M^{\mathrm{ext}}+M\left(D_{\mathrm{PDG}}^{0}\right)$, where $M\left(D_{\text {PDG }}^{0}\right)$ is the nominal $D^{0}$ mass [16]. A clear signal of $D_{2}^{*+} \rightarrow D^{0} \pi^{+}$is seen. An enhancement above background is also seen at the mass region around 2.3 GeV . The various contributions to the mass spectrum will be discussed below.

## 6. Mass, width and helicity parameters of $D_{1}$ and $D_{2}^{*}$

A significant enhancement above background is seen in the $D^{0} \pi^{+}$mass distribution (Fig. 4) around 2.3 GeV . A small excess of events is also seen in the same mass region in the $D^{+} \pi^{-}$ mass distribution (Fig. 3(b)).

The origin of these structures in both spectra is similar. They originate from the decay chains $D_{1}^{0}, D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}, D^{*+} \rightarrow D^{+} \pi^{0}$ and $D_{1}^{+}, D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}, D^{* 0} \rightarrow D^{0} \pi^{0}$ or $D^{* 0} \rightarrow D^{0} \gamma$. The $\pi^{0} / \gamma$ are not seen in the tracking detectors; thus, the reconstruction is incomplete. However, since the available phase space in the $D^{*} \rightarrow D \pi^{0}$ decay is small and $D$ is much heavier than $\pi^{0}$,

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Fig. 4. The mass distribution (dots), $M\left(D^{0} \pi_{a}\right)$. The solid curve is the result of a simultaneous fit to the feed-down (FD) $D_{1}^{+}$and $D_{2}^{*+}$ contributions and to the $D_{2}^{*+}$ signal plus background function (dashed curves). The lowest curves are the contributions of the $D_{1}^{+}$and $D_{2}^{*+}$ to the fit.
the energy and momentum of $D$ are close to those of $D^{*}$. Consequently, the enhancements in the $M\left(D^{+} \pi_{a}\right)$ (Fig. 3(b)) and $M\left(D^{0} \pi_{a}\right)$ (Fig. 4) distributions are feed-downs of the excited charm mesons $D_{1}, D_{2}^{*}$, shifted down approximately by the value of the $\pi^{0}$ mass, as verified by MC simulations.

### 6.1. Fitting procedure for $D_{1}^{0}$ and $D_{2}^{* 0}$

To distinguish between $D_{1}^{0}, D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}$, their helicity angular distributions were used. These can be parametrised as $d N / d \cos \alpha \propto 1+h \cos ^{2} \alpha$, where $\alpha$ is the angle between the $\pi_{a}$ and $\pi_{s}$ momenta in the $D^{*+}$ rest frame and $h$ is the helicity parameter, predicted [3,4] to be $h=3$ for $D_{1}^{0}$ and $h=-1$ for $D_{2}^{* 0}$. Fig. 5 shows the $M\left(D^{*+} \pi_{a}\right)$ distribution in four helicity bins. As expected from the above $h$ values, the $D_{1}^{0}$ contribution increases with $|\cos \alpha|$ and dominates for $|\cos \alpha|>0.75$, where the $D_{2}^{* 0}$ contribution is negligible.

A $\chi^{2}$ fit was performed using simultaneously the $M\left(D^{+} \pi_{a}\right)$ distribution (Fig. 3(b)) and the $M\left(D^{*+} \pi_{a}\right)$ distributions in four helicity bins (Fig. 5). The background was described by four parameters $a, b, c, d$, separately for $M\left(D^{*+} \pi_{a}\right)$ and $M\left(D^{+} \pi_{a}\right)$, as $B(x)=a x^{b} \exp \left(-c x-d x^{2}\right)$, where $x=\Delta M^{\text {ext }}-M_{\pi^{+}}$. Each resonance was fitted to a relativistic $D$-wave Breit-Wigner (BW) function [1] convoluted with a Gaussian resolution function with a width fixed to the corresponding MC prediction. Yields of the three signals, the $D_{1}^{0}$ and $D_{2}^{* 0}$ masses and widths

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Fig. 5. The mass distributions (dots), $M\left(D^{*+} \pi_{a}\right)$ in four helicity intervals: (a) $|\cos \alpha|<0.25$; (b) $0.25<|\cos \alpha|<0.50$; (c) $0.50<|\cos \alpha|<0.75$; (d) $|\cos \alpha|>0.75$. The solid curves are the result of the simultaneous fit to $D_{1}^{0}$ and $D_{2}^{* 0}$ plus background function (dashed curves).
and the $D_{1}^{0}$ helicity parameter, $h\left(D_{1}^{0}\right)$, were free parameters of the fit while $h\left(D_{2}^{* 0}\right)$ was fixed to the theoretical prediction $[3,4], h\left(D_{2}^{* 0}\right)=-1$. Another free fit parameter was the contribution of the $D_{1}^{0}, D_{2}^{* 0}$ feed-downs to the $M\left(D^{+} \pi_{a}\right)$ distribution (see Appendix A). The total normalisation of the sum of the feed-down processes from $D_{2}^{* 0}$ and $D_{1}^{0}$ decays was fitted relative to the direct signal peak yield from $D_{2}^{* 0}$ decay. The relative yields of the two feed-down contributions were taken to be equal to those for the direct signals in the $D^{*+} \pi^{-}$decay channel.

The wide excited charm states [16] $D_{1}(2430)^{0}$ and $D_{0}^{*}(2400)^{0}$ are expected to contribute to the $M\left(D^{*+} \pi_{a}\right)$ and $M\left(D^{+} \pi_{a}\right)$ distributions, respectively. Even though these states are hardly distinguishable from background due to their large width, they were included in the simultaneous fit with shapes described as relativistic $S$-wave BW functions [1]. Their masses and widths were set to the PDG values [16]. The yield of the $D_{1}(2430)^{0}$ was set to that of the narrow $D_{1}(2420)^{0}$ meson since both have the same spin-parity $J^{P}=1^{+}$. The ratio of $D_{0}^{*}(2400)^{0}$ to the narrow state $D_{2}^{*}(2460)^{0}$ was a free parameter in the fit.

The results of the simultaneous fit are given in Table 2 and shown in Figs. 3 and 5. Systematic uncertainties are discussed in Section 8. All results from the new analysis (HERA II) are consistent with those from the previous ZEUS publication [1] (HERA I). The masses of both $D_{1}^{0}$ and $D_{2}^{* 0}$ are consistent with the PDG values [16] and with a recent BaBar measurement [26]. The $D_{1}^{0}$ width, $\Gamma\left(D_{1}^{0}\right)=38.8 \pm 5.0(\text { stat. })_{-5.4}^{+1.9}$ (syst.) MeV , is also consistent with

Table 2
Results of the simultaneous fit for the yields $(N)$, masses $(M)$, widths $(\Gamma)$ and helicity parameters $(h)$ of the $D_{1}^{0}$ and $D_{2}^{* 0}$ mesons, for the ratios of the wide states $D_{1}(2430)^{0}$ and $D_{0}^{*}(2400)^{0}$ to the narrow states $D_{1}^{0}$ and $D_{2}^{* 0}$, and for the ratio of the feed-down (see text) to the $D_{2}^{* 0} \rightarrow D^{+} \pi^{-}$. The first uncertainties are statistical and the second are systematic. The results (HERA II) are compared to earlier ZEUS results at HERA I [1] and to the PDG [16].

|  | HERA II | HERA I | PDG |
| :--- | :--- | :--- | :--- |
| $N\left(D_{1}^{0} \rightarrow D^{*+} \pi\right)$ | $2732 \pm 285$ | $3110 \pm 340$ |  |
| $N\left(D_{2}^{* 0} \rightarrow D^{*+} \pi\right)$ | $1798 \pm 293$ | $870 \pm 170$ |  |
| $N\left(D_{2}^{* 0} \rightarrow D^{+} \pi\right)$ | $521 \pm 88\left(S\left(D^{+}\right)>3\right)$ | $690 \pm 160$ | $2421.3 \pm 0.6$ |
| $M\left(D_{1}^{0}\right), \mathrm{MeV}$ | $2423.1 \pm 1.5_{-1.0}^{+0.4}$ | $2420.5 \pm 2.1 \pm 0.9$ | $27.1 \pm 2.7$ |
| $\Gamma\left(D_{1}^{0}\right), \mathrm{MeV}$ | $38.8 \pm 5.0_{-5.4}^{+1.9}$ | $53.2 \pm 7.2_{-4.9}^{+3.3}$ |  |
| $h\left(D_{1}^{0}\right)$ | $7.8_{-2.7-1.8}^{+6.7+4.6}$ | $5.9_{-1.7-1.0}^{+3.0+2.4}$ |  |
| $M\left(D_{2}^{* 0}\right), \mathrm{MeV}$ | $2462.5 \pm 2.4_{-1.1}^{+1.3}$ | $2469.1 \pm 3.7_{-1.3}^{+1.2}$ | $2462.6 \pm 0.7$ |
| $\Gamma\left(D_{2}^{* 0}\right), \mathrm{MeV}$ | $46.6 \pm 8.1_{-3.8}^{+5.9}$ | 43 fixed | $49.0 \pm 1.4$ |
| $h\left(D_{2}^{* 0}\right)$ | -1 fixed | -1 fixed |  |
| $D_{1}(2430)^{0} / D_{1}^{0}$ | 1.0 fixed | 1.0 fixed |  |
| $D_{0}^{*}(2400)^{0} / D_{2}^{* 0}$ | $1.1 \pm 1.1$ | 1.7 fixed |  |
| Feed-downs $/ D_{2}^{* 0}$ | $0.3 \pm 0.4$ |  |  |

the PDG value [16] of $27.1 \pm 2.7 \mathrm{MeV}$, and is in good agreement with the BaBar measurement [26] of $31.4 \pm 0.5 \pm 1.3 \mathrm{MeV}$. The $D_{2}^{* 0}$ width, $\Gamma\left(D_{2}^{* 0}\right)=46.6 \pm 8.1$ (stat.) ${ }_{-3.8}^{+5.9}$ (syst.) MeV, is consistent with the PDG value [16] of $49.0 \pm 1.4 \mathrm{MeV}$, and with the BaBar measurement of $50.5 \pm 0.6 \pm 0.7 \mathrm{MeV}$.

The $D_{1}^{0}$ helicity parameter, $h\left(D_{1}^{0}\right)=7.8_{-2.7}^{+6.7}(\text { stat. })_{-1.8}^{+4.6}$ (syst.), is consistent with the BaBar value of $h\left(D_{1}^{0}\right)=5.72 \pm 0.25$ and somewhat above the theoretical prediction of $h=3$ and measurements by CLEO [27] with $h\left(D_{1}^{0}\right)=2.74_{-0.93}^{+1.40}$. The simultaneous fit with $h\left(D_{1}^{0}\right)$ fixed to the theoretical prediction, $h\left(D_{1}^{0}\right)=3$, yielded masses and widths of $D_{2}^{* 0}$ and $D_{1}^{0}$ that are somewhat away from the PDG values [16]. Repeating the simultaneous fit with $h\left(D_{2}^{* 0}\right)$ as a free parameter yielded similar results for all other free parameters with somewhat larger errors and with $h\left(D_{2}^{* 0}\right)=-1.16 \pm 0.35$, in good agreement with the theoretical prediction of $h=-1$.

The helicity angular distribution for a $J^{P}=1^{+}$state with a mixture of $D$ - and $S$-wave is

$$
\begin{equation*}
\frac{d N}{d \cos \alpha} \propto r+(1-r)\left(1+3 \cos ^{2} \alpha\right) / 2+\sqrt{2 r(1-r)} \cos \phi\left(1-3 \cos ^{2} \alpha\right) \tag{1}
\end{equation*}
$$

where $r=\Gamma_{S} /\left(\Gamma_{S}+\Gamma_{D}\right), \Gamma_{S}\left(\Gamma_{D}\right)$ is the $S(D)$-wave partial width and $\phi$ is relative phase between the two amplitudes. The relation between $h, r$ and $\phi$ is given by

$$
\begin{equation*}
\cos \phi=\frac{(3-h) /(3+h)-r}{2 \sqrt{2 r(1-r)}} . \tag{2}
\end{equation*}
$$

The range of the measured $h\left(D_{1}^{0}\right)$ restricted to one standard deviation is shown in Fig. 6 in a plot of $\cos \phi$ versus $r$. This range is consistent with the BaBar measurement [26]. The range restricted by CLEO [27] is outside the range of this measurement and that of BaBar. A similar measurement by the Belle Collaboration [5] is consistent with a pure $D$-wave, i.e. $\Gamma_{S} /\left(\Gamma_{S}+\Gamma_{D}\right)=0$.

In a recent paper [26] the BaBar Collaboration searched for excited $D$ meson states in $e^{+} e^{-} \rightarrow c \bar{c} \rightarrow D^{(*)} \pi+X$ with very large statistics. In addition to the $D_{1}^{0}$ and $D_{2}^{* 0}$ resonances, they saw two new structures near 2.6 GeV in the $D^{+} \pi^{-}$and $D^{*+} \pi^{-}$mass distributions,

## ZEUS



Fig. 6. The allowed region of $\cos \phi$, where $\phi$ is the relative phase of $S$ - and $D$-wave amplitudes, versus the fraction of $S$-wave in the $D_{1}^{0} \rightarrow D^{*} \pi$ decay for ZEUS, BaBar and CLEO measurements.
$D(2550)^{0}$ and $D^{*}(2600)^{0}$, and interpreted them as being radial excitations of the well-known $D^{0}$ and $D^{* 0}$, respectively. A small enhancement of events above the solid curve in the region near 2.6 GeV is seen in the $M\left(D^{*+} \pi^{-}\right)$distribution (Figs. 3(a), 5). Adding the new BaBar states to the fit gave insignificant yields of the states and did not significantly change the results of the other fit parameters.

### 6.2. Fitting procedure for $D_{1}^{+}$and $D_{2}^{*+}$

To extract the $D_{1}^{+}$and $D_{2}^{*+}$ masses and yields, a minimal $\chi^{2}$ fit was performed using the $M\left(D^{0} \pi_{a}\right)$ distribution (Fig. 4). Both resonances were fitted to relativistic $D$-wave Breit-Wigner (BW) functions [1] convoluted with a Gaussian resolution function with a width fixed to the corresponding MC prediction. Yields of the $D_{2}^{*+} \rightarrow D^{0} \pi^{+}$and the two feed-downs $D_{1}^{+}, D_{2}^{*+} \rightarrow$ $D^{* 0} \pi^{+}$(see Appendix A) and the $D_{1}^{+}$and $D_{2}^{*+}$ masses were free parameters of the fit. The $D_{1}^{+}$and $D_{2}^{*+}$ widths were fixed to the PDG values [16] and the $D_{1}^{+}$and $D_{2}^{*+}$ helicities were fixed to the theoretical prediction $[3,4], h\left(D_{1}^{+}\right)=3$ and $h\left(D_{2}^{*+}\right)=-1$. The background was parametrised with four parameters $a, b, c, d$ as $B(x)=a x^{b} \exp \left(-c x-d x^{2}\right)$, where $x=\Delta M^{\text {ext }}-$ $M_{\pi^{+}}$.

The results of the fit (yields and masses) are given in Table 3 and shown in Fig. 4. The masses of $D_{1}^{+}$and $D_{2}^{*+}$ are consistent with the PDG values [16]. The $D_{2}^{*+}$ mass is also consistent with the BaBar measurement [26].

## 7. $D_{2}^{*}$ decay branching ratios and $D_{1} / D_{2}^{*}$ fragmentation fractions

### 7.1. The neutral excited mesons

The branching ratio for $D_{2}^{* 0}$ and the fragmentation fractions for $D_{1}^{0}$ and $D_{2}^{* 0}$ were measured using the channels $D_{2}^{* 0} \rightarrow D^{+} \pi^{-}$and $D_{1}^{0}, D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}$with $D^{*+} \rightarrow D^{0} \pi_{s}^{+} \rightarrow\left(K^{-} \pi^{+}\right) \pi_{s}^{+}$. The numbers of reconstructed $D_{1}^{0}, D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}$and $D_{2}^{* 0} \rightarrow D^{+} \pi^{-}$decays were divided by the numbers of reconstructed $D^{*+}$ and $D^{+}$mesons, yielding the fractions of $D^{*+}$ and $D^{+}$

Table 3
Results of the fit for the yields ( $N$ ), masses ( $M$ ), widths $(\Gamma)$ and helicity parameters ( $h$ ) of the $D_{1}^{+}$and $D_{2}^{*+}$ mesons. The first uncertainties are statistical and the second are systematic. The results are compared to those of the PDG [16].

|  | HERA II | PDG |
| :--- | :--- | :--- |
| $N\left(D_{1}^{+} \rightarrow D^{* 0} \pi^{+}\right)$ | $759 \pm 183$ |  |
| $N\left(D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}\right)$ | $634 \pm 223$ |  |
| $N\left(D_{2}^{*+} \rightarrow D^{0} \pi^{+}\right)$ | $737 \pm 164$ | $2423.4 \pm 3.1$ |
| $M\left(D_{1}^{+}\right), \mathrm{MeV}$ | $2421.9 \pm 4.7_{-1.2}^{+3.4}$ | $25 \pm 6$ |
| $\Gamma\left(D_{1}^{+}\right), \mathrm{MeV}$ | 25 fixed |  |
| $h\left(D_{1}^{+}\right)$ | 3.0 fixed | $2464.4 \pm 1.9$ |
| $M\left(D_{2}^{*+}\right), \mathrm{MeV}$ | $2460.6 \pm 4.4_{-0.8}^{+3.6}$ | $37 \pm 6$ |
| $\Gamma\left(D_{2}^{*+}\right), \mathrm{MeV}$ | 37 fixed |  |
| $h\left(D_{2}^{*+}\right)$ | -1.0 fixed |  |

mesons originating from the $D_{1}^{0}$ and $D_{2}^{* 0}$ decays. To correct the measured fractions for detector effects, ratios of acceptances were calculated using the MC simulation for the $D_{1}^{0}, D_{2}^{* 0} \rightarrow$ $D^{*+} \pi^{-}$and $D_{2}^{* 0} \rightarrow D^{+} \pi^{-}$states to the inclusive $D^{*+}$ and $D^{+}$acceptances, respectively.

Beauty production at HERA is smaller than charm production by two orders of magnitude. A subtraction of the $b$-quark relative contribution in a previous ZEUS analysis [1] changed the relative acceptances by less than $1.5 \%$ of their values. Consequently, no such subtraction was performed in this analysis and the MC simulation included the beauty production processes. A variation of this contribution was considered for the systematics (Section 8).

The fractions, $\mathcal{F}$, of $D^{*+}$ mesons originating from $D_{1}^{0}$ and $D_{2}^{* 0}$ decays were calculated in the kinematic range $\left|\eta\left(D^{*+}\right)\right|<1.6$ and $p_{T}\left(D^{*+}\right)>1.5 \mathrm{GeV}$ for the $D^{*+}$ decay and the fraction of $D^{+}$mesons originating from $D_{2}^{* 0}$ decays was calculated in the kinematic range $p_{T}\left(D^{+}\right)>$ 2.8 GeV and $\left|\eta\left(D^{+}\right)\right|<1.6$.

The fractions measured in the restricted $p_{T}\left(D^{*+}, D^{+}\right)$and $\eta\left(D^{*+}, D^{+}\right)$kinematic ranges were extrapolated to the fractions in the full kinematic phase space using the Bowler modification [17] of the Lund symmetric fragmentation function [18] as implemented in Pythia [28]. Pythia assumes flat $(h=0)$ helicity angle distributions for all excited charm states. It was checked that the acceptance in these distributions is flat and the extrapolation factors are helicity independent. Applying the estimated extrapolation factors, $\sim 1.12$ for $\mathcal{F}_{D_{1}^{0} \rightarrow D^{*+} \pi^{-} / D^{*+}}, \sim 1.16$ for $\mathcal{F}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-} / D^{*+}}$ and $\sim 1.34$ for $\mathcal{F}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-} / D^{+}}$, gives

$$
\begin{align*}
& \mathcal{F}_{D_{1}^{0} \rightarrow D^{*+} \pi^{-} / D^{*+}}^{\mathrm{extr}}=8.5 \pm 1.4(\text { stat. })_{-1.6}^{ \pm 1.2}(\text { syst. }) \%  \tag{3}\\
& \mathcal{F}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-} / D^{*+}}^{\mathrm{extr}}=4.7 \pm 1.3(\text { stat. })_{-0.8}^{+1.2}(\text { syst. }) \%,  \tag{4}\\
& \mathcal{F}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-} / D^{+}}^{\mathrm{ext}}=6.7 \pm 2.4(\text { stat. })_{-1.1}^{+1.5}(\text { syst. }) \% \tag{5}
\end{align*}
$$

In the full kinematic phase space, the extrapolated fractions of $D^{*+}$ originating from $D_{1}^{0}$ and $D_{2}^{* 0}$ and of $D^{+}$originating from $D_{2}^{* 0}$ can be expressed [1] in terms of the rates of $c$-quarks hadronising to a given charm meson ("fragmentation fractions"), $f\left(c \rightarrow D_{1}^{0}\right), f\left(c \rightarrow D_{2}^{* 0}\right), f(c \rightarrow$ $\left.D^{*+}\right)$ and $f\left(c \rightarrow D^{+}\right)$and the corresponding branching fractions $\mathcal{B}_{D_{1}^{0} \rightarrow D^{*+} \pi^{-}}, \mathcal{B}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}}$ and $\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-}}$.

From the expressions used in a previous ZEUS publication [1], the fragmentation fractions $f\left(c \rightarrow D_{1}^{0}\right)$ and $f\left(c \rightarrow D_{2}^{* 0}\right)$ and the ratio of the two branching fractions for the $D_{2}^{* 0}$ meson can be shown to be:

$$
\begin{align*}
& f\left(c \rightarrow D_{1}^{0}\right)=\frac{\mathcal{F}_{D_{1}^{0} \rightarrow D^{*+} \pi^{-} / D^{*+}}^{\text {extr }}}{\mathcal{B}_{D_{1}^{0} \rightarrow D^{*+} \pi^{-}}} f\left(c \rightarrow D^{*+}\right),  \tag{6}\\
& f\left(c \rightarrow D_{2}^{* 0}\right)=\frac{\mathcal{F}_{D_{2}^{* *} \rightarrow D^{*+} \pi^{-} / D^{*+}}^{\mathrm{extr}} f\left(c \rightarrow D^{*+}\right)+\mathcal{F}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-} / D^{+}}^{\mathrm{extr}} f\left(c \rightarrow D^{+}\right)}{\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}}+\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-}}},  \tag{7}\\
& \frac{\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-}}}{\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{*+\pi^{-}}}}=\frac{\mathcal{F}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-} / D^{+}}^{\mathrm{extr}} f\left(c \rightarrow D^{+}\right)}{\mathcal{F}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-} / D^{*+}}^{\mathrm{extr}} f\left(c \rightarrow D^{*+}\right)} . \tag{8}
\end{align*}
$$

The $f\left(c \rightarrow D^{*+}\right)$ and $f\left(c \rightarrow D^{+}\right)$values used were obtained as a combination of data from HERA and $e^{+} e^{-}$colliders [29]:

$$
\begin{aligned}
& f\left(c \rightarrow D^{*+}\right)=22.87 \pm 0.56(\text { stat. } \oplus \text { syst. })_{-0.56}^{+0.45}(\text { br. }) \% \\
& f\left(c \rightarrow D^{+}\right)=22.56 \pm 0.77(\text { stat. } \oplus \text { syst. }) \pm 1.00(\text { br. }) \%
\end{aligned}
$$

where the third uncertainties are due to the branching-ratio uncertainties.
Taking into account the correlations in the simultaneous fit performed to obtain the values in Eqs. (4) and (5) yields

$$
\frac{\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-}}}{\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}}}=1.4 \pm 0.3 \text { (stat.) } \pm 0.3 \text { (syst.) }
$$

in good agreement with the PDG world-average value $1.56 \pm 0.16$ [16]. Theoretical models [30-32] predict the ratio to be in the range from 1.5 to 3 .

Neglecting the contributions of the non-dominant decay mode $D_{1}^{0} \rightarrow D^{0} \pi^{+} \pi^{-}[16]$ and assuming isospin conservation, for which

$$
\mathcal{B}_{D_{1}^{0} \rightarrow D^{*+} \pi^{-}}=2 / 3, \quad \mathcal{B}_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}}+\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-}}=2 / 3
$$

and using Eqs. (6) and (7) yields

$$
\begin{aligned}
& f\left(c \rightarrow D_{1}^{0}\right)=2.9 \pm 0.5(\text { stat. }) \pm 0.5(\text { syst. }) \% \\
& \left.f\left(c \rightarrow D_{2}^{* 0}\right)=3.9 \pm 0.9 \text { (stat. }\right)_{-0.6}^{+0.8}(\text { syst. }) \%
\end{aligned}
$$

The measured fragmentation fractions were found to be consistent with those obtained in $e^{+} e^{-}$ annihilations [33]. The sum of the two fragmentation fractions,

$$
\left.f\left(c \rightarrow D_{1}^{0}\right)+f\left(c \rightarrow D_{2}^{* 0}\right)=6.8 \pm 1.0(\text { stat. })_{-0.8}^{+0.9} \text { (syst. }\right) \%,
$$

agrees with the prediction of the tunneling model of $8.5 \%$ [34].
Assuming uncorrelated errors, the ratio

$$
f\left(c \rightarrow D_{1}^{0}\right) / f\left(c \rightarrow D_{2}^{* 0}\right)=0.8 \pm 0.2 \text { (stat.) } \pm 0.2 \text { (syst.) }
$$

is in good agreement with the simple spin-counting prediction of $3 / 5$.

### 7.2. The charged excited mesons

The branching ratio for $D_{2}^{*+}$ and the fragmentation fractions for $D_{1}^{+}$and $D_{2}^{*+}$ were measured using the channels $D_{2}^{*+} \rightarrow D^{0} \pi^{+}$and $D_{1}^{+}, D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}$with $D^{* 0} \rightarrow D^{0} \pi^{0} / \gamma$, where the $\pi^{0} / \gamma$ are not measured directly. Since $D^{* 0}$ decays always to $D^{0}$ [16], the number of $D^{* 0}$ and $D^{0}$ originating from $D_{1}^{+} / D_{2}^{*+}$ are identical. The number of reconstructed $D_{1}^{+} / D_{2}^{*+} \rightarrow$ $D^{* 0} \pi^{+} ; D^{* 0} \rightarrow D^{0} \pi^{0} / \gamma$ and $D_{2}^{*+} \rightarrow D^{0} \pi^{+}$decays were thus divided by the total number of reconstructed $D^{0}$ mesons, yielding the fractions of $D^{0}$ mesons originating from $D_{1}^{+} / D_{2}^{*+}$ decays. Detector effects were corrected as described in Section 7.1. The above fractions were calculated in the kinematic range $p_{T}\left(D^{0}\right)>2.6 \mathrm{GeV}$ and $\left|\eta\left(D^{0}\right)\right|<1.6$ and extrapolated to the fractions in the full kinematic phase space as for the $D_{1}^{0}$ and $D_{2}^{* 0}$ (Section 7.1). Applying the extrapolation factors, $\sim 1.28$ for $D_{1}^{+} \rightarrow D^{* 0} \pi^{+}, \sim 1.18$ for $D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}$and $\sim 1.35$ for $D_{2}^{*+} \rightarrow D^{0} \pi^{+}$ gives

$$
\begin{align*}
& \left.\mathcal{F}_{D_{1}^{+} \rightarrow D^{* 0} \pi^{+} / D^{0}}^{\text {extr }}=5.4 \pm 2.1 \text { (stat. }\right)_{-0.3}^{+2.3}(\text { syst. }) \%  \tag{9}\\
& \left.\mathcal{F}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+} / D^{0}}^{\text {extr }}=1.8 \pm 0.9 \text { (stat. }\right)_{-0.3}^{+0.5}(\text { syst. }) \%  \tag{10}\\
& \mathcal{F}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+} / D^{0}}^{\text {extr }}=2.0 \pm 0.5(\text { stat. })_{-0.2}^{+0.4}(\text { syst. }) \% \tag{11}
\end{align*}
$$

The fractions of $D^{* 0} / D^{0}$ mesons originating from $D_{1}^{+} / D_{2}^{*+}$ decays can be expressed as

$$
\begin{align*}
& \mathcal{F}_{D_{1}^{+} \rightarrow D^{* 0} \pi^{+} / D^{* 0}}^{\mathrm{extr}} \equiv \frac{N\left(D_{1}^{+} \rightarrow D^{* 0} \pi^{+}\right)}{N\left(D^{* 0}\right)}=\frac{f\left(c \rightarrow D_{1}^{+}\right)}{f\left(c \rightarrow D^{* 0}\right)} \mathcal{B}_{D_{1}^{+} \rightarrow D^{* 0} \pi^{+}},  \tag{12}\\
& \mathcal{F}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+} / D^{* 0}}^{\mathrm{extr}} \equiv \frac{N\left(D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}\right)}{N\left(D^{* 0}\right)}=\frac{f\left(c \rightarrow D_{2}^{*+}\right)}{f\left(c \rightarrow D^{* 0}\right)} \mathcal{B}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}},  \tag{13}\\
& \mathcal{F}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+} / D^{0}}^{\mathrm{extr}} \equiv \frac{N\left(D_{2}^{*+} \rightarrow D^{0} \pi^{+}\right)}{N\left(D^{0}\right)}=\frac{f\left(c \rightarrow D_{2}^{*+}\right)}{f\left(c \rightarrow D^{0}\right)} \mathcal{B}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+}}, \tag{14}
\end{align*}
$$

where $N$ denotes the acceptance-corrected number of events.
The ratio of the fragmentation fractions $f\left(c \rightarrow D^{* 0}\right)$ and $f\left(c \rightarrow D^{0}\right)$ can be expressed as

$$
\frac{f\left(c \rightarrow D^{* 0}\right)}{f\left(c \rightarrow D^{0}\right)}=\frac{N\left(D^{* 0}\right)}{N\left(D^{0}\right)} .
$$

Consequently, Eqs. (12) and (13) can be written as

$$
\begin{aligned}
& \frac{N\left(D_{1}^{+} \rightarrow D^{* 0} \pi^{+}\right)}{N\left(D^{0}\right)}=\frac{f\left(c \rightarrow D_{1}^{+}\right)}{f\left(c \rightarrow D^{0}\right)} \mathcal{B}_{D_{1}^{+} \rightarrow D^{* 0} \pi^{+}}, \\
& \frac{N\left(D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}\right)}{N\left(D^{0}\right)}=\frac{f\left(c \rightarrow D_{2}^{*+}\right)}{f\left(c \rightarrow D^{0}\right)} \mathcal{B}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}},
\end{aligned}
$$

yielding

$$
\begin{aligned}
& f\left(c \rightarrow D_{1}^{+}\right)=\frac{f\left(c \rightarrow D^{0}\right)}{N\left(D^{0}\right)} \frac{N\left(D_{1}^{+} \rightarrow D^{* 0} \pi^{+}\right)}{\mathcal{B}_{D_{1}^{+} \rightarrow D^{* 0} \pi^{+}}} \\
& f\left(c \rightarrow D_{2}^{*+}\right)=\frac{f\left(c \rightarrow D^{0}\right)}{N\left(D^{0}\right)} \frac{N\left(D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}\right)+N\left(D_{2}^{*+} \rightarrow D^{0} \pi^{+}\right)}{\mathcal{B}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}}+\mathcal{B}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+}}},
\end{aligned}
$$

$$
\frac{\mathcal{B}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+}}}{\mathcal{B}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}}}=\frac{N\left(D_{2}^{*+} \rightarrow D^{0} \pi^{+}\right)}{N\left(D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}\right)} .
$$

Neglecting the non-dominant decay mode $D_{1}^{+} \rightarrow D^{+} \pi^{+} \pi^{-}$[16], assuming isospin conservation, for which

$$
\mathcal{B}_{D_{1}^{+} \rightarrow D^{* 0} \pi^{+}}=2 / 3, \quad \mathcal{B}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}}+\mathcal{B}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+}}=2 / 3,
$$

and using Eqs. (9)-(11) and the fragmentation fraction [29]

$$
f\left(c \rightarrow D^{0}\right)=56.43 \pm 1.51(\text { stat. } \oplus \text { syst. })_{-1.64}^{+1.35}(\text { br. }) \%,
$$

gives

$$
\begin{aligned}
& f\left(c \rightarrow D_{1}^{+}\right)=4.6 \pm 1.8(\text { stat. })_{-0.3}^{+2.0}(\text { syst. }) \%, \\
& f\left(c \rightarrow D_{2}^{*+}\right)=3.2 \pm 0.8(\text { stat. })_{-0.2}^{+0.5}(\text { syst. }) \%, \\
& \left.f\left(c \rightarrow D_{1}^{+}\right)+f\left(c \rightarrow D_{2}^{*+}\right)=7.8 \pm 2.0(\text { stat. })_{-0.4}^{+2.0} \text { (syst.) }\right) \%, \\
& \left.f\left(c \rightarrow D_{1}^{+}\right) / f\left(c \rightarrow D_{2}^{*+}\right)=1.4 \pm 0.7 \text { (stat. }\right)_{-0.1}^{+0.7}(\text { syst. }) \%,
\end{aligned}
$$

in agreement with the fragmentation fractions of the neutral excited charm mesons (Section 7.1).
The ratio of the branching fractions of the two dominant decay modes of the $D_{2}^{*+}$,

$$
\begin{equation*}
\frac{\mathcal{B}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+}}}{\mathcal{B}_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}}}=1.1 \pm 0.4(\text { stat. })_{-0.2}^{+0.3} \text { (syst.) } \tag{15}
\end{equation*}
$$

significantly improves on the accuracy of the PDG [16] value of $1.9 \pm 1.1 \pm 0.3$. BaBar mea-
 assumptions and is not included in the PDG averages [16]. Using the value given in Eq. (15)
 the BaBar result.

## 8. Systematic uncertainties

The systematic uncertainties were determined by appropriate variations of the analysis procedure, generally by the uncertainties in our knowledge of the variables considered, and repeating the calculation of the results. The following sources of uncertainty were considered:

- $\left\{\delta_{1}\right\}$ The stability of the fit results was checked by a variation of the selection cuts which are most sensitive to the ratio of signal and background in the data:
- the cut on the minimal transverse momentum of the $D^{*+}, D^{+}$and $D^{0}$ candidates was varied by $\pm 100 \mathrm{MeV}$;
- the cut on the minimal transverse momentum of the extra pion in the excited $D$ meson analysis was varied by $\pm 10 \mathrm{MeV}$;
- the selection cut on the cosine of angle between extra pions and charged (neutral) excited $D$ meson candidates was changed by $\pm 0.1$ ( $\pm 0.05$ );
- the widths of the mass windows used for the selection of $D^{*+}$ and $D^{0}$ candidates in the excited charm meson analyses were varied by $\pm 5 \%$ for each $p_{T}$ dependent window (see Table 1), while for the $D^{+}$candidates it was varied by $\pm 12.5 \%$.
- $\left\{\delta_{2}\right\}$ The CAL energy scale is known with $\pm 2 \%$ uncertainty and was varied accordingly in the simulation.
- $\left\{\delta_{3}\right\}$ The uncertainties related to the fit procedure were obtained as follows:
- the ranges for the signal fits were reduced on either side by 16 MeV for the $D^{*+} \pi$ and $D^{+} \pi$ mass spectra and 24 MeV for the $D^{0} \pi$ mass spectrum;
- the background shape was changed to that used by BaBar (Eq. 1 in Ref. [26]);
- the widths of the Gaussians used to parametrise the mass resolutions were changed by $\pm 20 \%$;
- all the masses and widths of wide states were set free in the fit. Since with the present data alone these parameters are not determined well, the world-average values from PDG [16] were used as additional constraints. This was implemented by adding for each parameter $P$ (width or mass) a term $\frac{\left(P-P_{\mathrm{PDG}}\right)^{2}}{\sigma\left(P_{\mathrm{PDG}}\right)^{2}}$ to the $\chi^{2}$-function. Here $P_{\mathrm{PDG}}$ and $\sigma\left(P_{\mathrm{PDG}}\right)$ denote the parameter value and its uncertainty from PDG [16];
- the background functions in the four helicity intervals were allowed to have separate normalisations;
- the helicity parameter of the $D_{2}^{* 0}$ meson in the fit was set free (Section 5.1).
- $\left\{\delta_{4}\right\}$ The uncertainties of $M\left(D^{*+}\right)_{\text {PDG }}, M\left(D^{0}\right)_{\text {PDG }}, M\left(D^{+}\right)_{\text {PDG }}$ were taken into account.
- $\left\{\delta_{5}\right\}$ The widths of $D_{1}^{+}$and $D_{2}^{*+}$ were varied within their uncertainties taken from PDG [16].
- $\left\{\delta_{6}\right\}$ The uncertainty of the beauty contamination was determined by varying the beauty fraction in the MC sample between 0 and $200 \%$ of the reference amount.
- $\left\{\delta_{7}\right\}$ The extrapolation uncertainties were determined by varying relevant parameters of the Pythia simulation using the Bowler modification [17] of the Lund symmetric fragmentation function [18]. The following variations were performed:
- the mass of the $c$ quark was varied from its nominal value of 1.5 GeV by $\pm 0.2 \mathrm{GeV}$;
- the strangeness suppression factor was varied from its nominal value of 0.3 by $\pm 0.1$;
- the fraction of the lowest-mass charm mesons produced in a vector state was varied from its nominal value of 0.6 by $\pm 0.1$;
- the Bowler fragmentation function parameter $r_{c}$ was varied from the predicted value 1 to 0.5 ; the $a$ and $b$ parameters of the Lund symmetric function were varied by $\pm 20 \%$ around their default values [28].

A possible model dependence of the acceptance corrections was checked by reweighting the $D$ meson transverse momentum distribution in the MC to match the distribution observed in the data; no significant effect on any result was found. As a further cross check the selected pseudorapidity range of the extra pion, which is not the same for the different decay channels (see Section 5), was varied, and again no significant effect on any result was observed. The uncertainties of the fragmentation fractions $f\left(c \rightarrow D^{*+}\right), f\left(c \rightarrow D^{+}\right)$and $f\left(c \rightarrow D^{0}\right)$ were included by adding in quadrature their statistical and systematic uncertainties and the uncertainties originating from the branching-ratio uncertainties. The resulting uncertainty is included in $\delta_{7}$.

The contributions from all systematic uncertainties were calculated separately for positive and negative variations and added in quadrature. The obtained values are listed in Tables 4-7. There is no single dominating source of systematic uncertainty. The total systematic uncertainties are comparable to the statistical errors.

Table 4
Total and $\delta_{1}-\delta_{4}$ (see text) systematic uncertainties for the mass, width and helicity parameters of the neutral excited charm mesons.

|  | total | $\delta_{1}$ | $\delta_{2}$ | $\delta_{3}$ | $\delta_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $M\left(D_{1}^{0}\right), \mathrm{MeV}$ | $\begin{aligned} & +0.4 \\ & { }_{-1.0}^{+0} \end{aligned}$ | $\begin{gathered} { }_{-0.3}^{+0.4} \end{gathered}$ | $\begin{aligned} & { }_{-0.8}^{+0.0} \end{aligned}$ | $\begin{aligned} & { }_{-0.5}^{+0.1} \end{aligned}$ | ${ }_{-0.1}^{+0.1}$ |
| $M\left(D_{2}^{* 0}\right), \mathrm{MeV}$ | $\begin{aligned} & +1.3 \\ & { }_{-1.1}^{+} \end{aligned}$ | $\begin{aligned} & +0.9 \\ & { }_{-0.9}^{+0} \end{aligned}$ | $\begin{aligned} & +0.9 \\ & { }_{-0.5}^{+0} \end{aligned}$ | $\begin{aligned} & +0.2 \\ & -0.2 \end{aligned}$ | ${ }_{-0.1}^{+0.0}$ |
| $\Gamma\left(D_{1}^{0}\right), \mathrm{MeV}$ | $\begin{aligned} & +1.9 \\ & { }_{-5.4} \end{aligned}$ | $\begin{aligned} & +1.6 \\ & { }_{-2.3}^{+1} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-1.6} \end{aligned}$ | +1.0 -4.5 | ${ }_{-0.0}^{+0.0}$ |
| $\Gamma\left(D_{2}^{* 0}\right), \mathrm{MeV}$ | $\begin{aligned} & +5.9 \\ & -3.8 \end{aligned}$ | ${ }_{-3.5}^{+4.0}$ | ${ }_{-0.2}^{+0.1}$ | +4.3 -1.7 | ${ }_{-0.0}^{+0.0}$ |
| $h\left(D_{1}^{0}\right)$ | $\begin{aligned} & +4.6 \\ & -1.8 \\ & \hline \end{aligned}$ | +3.1 -1.3 | $\begin{aligned} & +2.4 \\ & -0.3 \\ & \hline \end{aligned}$ | +2.3 -1.3 | ${ }_{-0.1}^{+0.1}$ |

Table 5
Total and $\delta_{1}-\delta_{5}$ (see text) systematic uncertainties for the mass, width and helicity parameters of the charged excited charm mesons.

|  | total | $\delta_{1}$ | $\delta_{2}$ | $\delta_{3}$ | $\delta_{4}$ | $\delta_{5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $M\left(D_{1}^{+}\right), \mathrm{MeV}$ | ${ }_{-1.2}^{+3.4}$ | ${ }_{-0.1}^{+3.2}$ | ${ }_{-0.7}^{+0.0}$ | ${ }_{-0.1}^{+0.6}$ | ${ }_{-0.1}^{+0.1}$ | ${ }_{-0.9}^{+0.6}$ |
| $M\left(D_{2}^{*+}\right), \mathrm{MeV}$ | ${ }_{-0.8}^{+3.7}$ | ${ }_{-0.5}^{+1.7}$ | ${ }_{-0.0}^{+3.1}$ | ${ }_{-0.2}^{+0.4}$ | ${ }_{-0.1}^{+0.1}$ | ${ }_{-0.6}^{+0.9}$ |

Table 6
Total and $\delta_{1}-\delta_{7}$ (see text) systematic uncertainties for extrapolated fractions, for ratios of the dominant branching fractions and for fragmentation fractions of the $D_{1}^{0}$ and $D_{2}^{* 0}$ mesons.

|  | total, \% | $\delta_{1}, \%$ | $\delta_{2}$, \% | $\delta_{3}, \%$ | $\delta_{4}$, \% | $\delta_{6}$, \% | $\delta_{7}$, \% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathcal{F}$ extr | +19.2 | +16.4 | +6.7 | +3.4 | +0.3 | +1.5 | +6.5 |
| ${ }^{-} D_{1}^{0} \rightarrow D^{*+} \pi^{-} / D^{*+}$ | -14.5 | -12.2 | -0.0 | -7.5 | -0.0 | -2.0 | -0.0 |
| $\mathcal{F}^{\text {extr }}$ | +13.5 | +11.9 | +3.7 | +1.2 | +4.9 | $+0.9$ | $+0.1$ |
| $D_{2}^{* 0} \rightarrow D^{*+} \pi^{-} / D^{*+}$ | -18.2 | -12.9 | -5.0 | -11.8 | -0.0 | -1.5 | -0.0 |
| $\mathcal{F}^{\text {extr }}$ | +25.2 | +18.6 | +11.9 | +5.4 | +1.0 | +0.5 | +10.7 |
| $D_{2}^{* 0} \rightarrow D^{+} \pi^{-} / D^{+}$ | -17.3 | -7.8 | -0.0 | -15.4 | -0.0 | -0.8 | -0.0 |
| $\mathcal{B}_{D_{2}^{* 0} \rightarrow D^{+} \pi^{-}}$ | +20.1 | +9.9 | +0.0 | +9.6 | +0.0 | +2.3 | +14.4 |
| $\overline{\mathcal{B}}{ }_{D_{2}^{* 0} \rightarrow D^{*+} \pi^{-}}$ | -19.5 | -13.5 | -4.7 | -3.3 | -0.7 | -2.5 | -12.7 |
| $f\left(c \rightarrow D_{1}^{0}\right)$ | $\begin{aligned} & +15.8 \\ & { }_{-18.6} \end{aligned}$ | $\begin{array}{r} +11.9 \\ -12.9 \end{array}$ | $\begin{aligned} & +3.7 \\ & { }_{-5.0} \end{aligned}$ | $\begin{aligned} & +11.2 \\ & { }_{-11.8}^{+} \end{aligned}$ | $\begin{aligned} & +4.9 \\ & -0.0 \end{aligned}$ | $\begin{aligned} & +0.9 \\ & { }_{-1.5}^{+0} \end{aligned}$ | $\begin{aligned} & +8.1 \\ & { }_{-3.6} \end{aligned}$ |
| $\underline{f\left(c \rightarrow D_{2}^{* 0}\right)}$ | $\begin{array}{r} +22.4 \\ -15.1 \end{array}$ | $\begin{aligned} & +16.1 \\ & { }_{-9.1} \end{aligned}$ | $\begin{array}{r} +8.9 \\ -0.0 \\ \hline \end{array}$ | $\begin{aligned} & +4.0 \\ & -10.7 \end{aligned}$ | $\begin{aligned} & +0.6 \\ & { }_{-0.0}^{+0.6} \end{aligned}$ | $\begin{array}{r} +0.6 \\ -1.0 \end{array}$ | $\begin{aligned} & +12.2 \\ & { }_{-5.3} \\ & \hline \end{aligned}$ |

Table 7
Total and $\delta_{1}-\delta_{7}$ (see text) systematic uncertainties for extrapolated fractions, for ratios of the dominant branching fractions and for fragmentation fractions of the $D_{1}^{+}$and $D_{2}^{*+}$ mesons.

|  | total, \% | $\delta_{1}, \%$ | $\delta_{2}$, \% | $\delta_{3}, \%$ | $\delta_{4}$, \% | $\delta_{5}$, \% | $\delta_{6}$, \% | $\delta_{7}$, \% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathcal{F}^{\text {extr }}$ | +42.6 | +30.5 | +18.3 | +3.7 | $+0.0$ | +22.2 | +1.8 | +6.0 |
| $D_{1}^{+} \rightarrow D^{* 0} \pi^{+} / D^{0}$ | -6.1 | -0.0 | -0.0 | -2.6 | -0.0 | -0.0 | -5.2 | -1.9 |
| $\mathcal{F}^{\text {extr }}$ | +24.6 | +14.7 | +6.3 | +1.2 | +0.0 | +13.5 | +3.5 | +12.5 |
| ${ }^{\text {D }}$ 2+ $\rightarrow D^{* 0} \pi^{+} / D^{0}$ | -14.8 | $-1.3$ | -2.4 | -7.9 | -0.0 | -4.6 | -4.0 | -10.5 |
| $\mathcal{F}^{\text {extr }}$ | +18.0 | +13.4 | +5.6 | +0.2 | +0.0 | +3.6 | +1.6 | +9.8 |
| $D_{2}^{*+} \rightarrow D^{0} \pi^{+} / D^{0}$ | -8.0 | -0.8 | -4.3 | -5.2 | -0.0 | -0.0 | -1.4 | -3.9 |
| $\mathcal{B}_{D_{2}^{*+} \rightarrow D^{0} \pi^{+}}$ | +23.8 | +10.5 | +8.3 | +7.0 | +0.0 | +6.9 | +2.7 | +16.9 |
| $\overline{\mathcal{B}}{ }_{D_{2}^{*+} \rightarrow D^{* 0} \pi^{+}}$ | -19.1 | -8.5 | -10.0 | -4.7 | -0.0 | -9.1 | -1.9 | -9.3 |
| $f\left(c \rightarrow D_{1}^{+}\right)$ | ${ }_{-7.3}^{+42.7}$ | ${ }_{-0.0}^{+30.5}$ | ${ }_{-0.0}^{+18.3}$ | $\begin{aligned} & +3.7 \\ & { }_{-2.6}^{+} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0}^{+0} \end{aligned}$ | ${ }_{-0.0}^{+22.2}$ | $\begin{aligned} & +1.8 \\ & { }_{-5.2} \end{aligned}$ | +7.1 -4.4 |
| $\underline{f\left(c \rightarrow D_{2}^{*+}\right)}$ | $\begin{aligned} & +16.7 \\ & { }_{-7.1}^{+} \end{aligned}$ | ${ }_{-0.0}^{+12.0}$ | $\begin{aligned} & +1.8 \\ & { }_{-0.0}^{+1} \end{aligned}$ | $\begin{aligned} & +0.5 \\ & { }_{-5.4}^{+0} \end{aligned}$ | $\begin{aligned} & +0.0 \\ & { }_{-0.0}^{+0.0} \end{aligned}$ | $\begin{aligned} & +8.2 \\ & -1.2 \end{aligned}$ | $\begin{aligned} & +2.5 \\ & -2.7 \end{aligned}$ | $\begin{aligned} & +7.7 \\ & -3.6 \end{aligned}$ |

## 9. Summary

The full HERA data taken from 2003 to 2007 with an integrated luminosity of $373 \mathrm{pb}^{-1}$ has been used to study the production of excited charm mesons. Signals of $D_{1}(2420)^{0}$ and $D_{2}^{*}(2460)^{0}$ were seen in the $D^{*+} \pi^{-}$decay mode and a clear $D_{2}^{*}(2460)^{0}$ signal was seen in the $D^{+} \pi^{-}$decay mode. The measured $D_{1}^{0}$ and $D_{2}^{* 0}$ masses and widths are in good agreement with the latest PDG values. The measured $D_{1}^{0}$ helicity parameter allows for some $S$-wave mixing in its decay to $D^{*+} \pi^{-}$. The result is also consistent with a pure $D$-wave hypothesis. The helicity of $D_{2}^{* 0}$, when set free in the fit, is consistent with the HQET prediction, $h=-1$.

A clear $D_{2}^{*}(2460)^{+}$signal is seen for the first time at HERA in the $D^{0} \pi^{+}$decay mode. Feeddowns of both resonances $D_{1}(2420)^{+}$and $D_{2}^{*}(2460)^{+}$in the decay mode $D^{* 0} \pi^{+}$are seen in the expected mass region of $M\left(D^{0} \pi^{+}\right) \approx 2.3 \mathrm{GeV}$. The measured $D_{1}^{+}$and $D_{2}^{*+}$ masses are in good agreement with the PDG values and the $D_{2}^{*+}$ mass is consistent with the BaBar measurement.

The fractions of $c$-quarks hadronising into $D_{1}^{0}$ and $D_{2}^{* 0}$ are consistent with those from the previous ZEUS publication and with $e^{+} e^{-}$annihilation results, in agreement with charm fragmentation universality. The fractions of $c$-quarks hadronising into $D_{1}^{+}$and $D_{2}^{*+}$ were measured for the first time and are consistent, respectively, with the fractions of the neutral charm excited states $D_{1}^{0}$ and $D_{2}^{* 0}$.

The ratios of the neutral and charged $D_{2}^{*}$ branching ratios into $D \pi$ and $D^{*} \pi$ are consistent with the PDG values.

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## Appendix A. Parametrisation of the feed-down contributions

Let us consider the decay chain $D_{1,2} \rightarrow D^{*} \pi, D^{*} \rightarrow D \pi^{0}$ in the $D^{*}$ centre-of-mass system. Here $D_{1,2}$ is a neutral (positively charged) excited charm meson $D_{1}$ or $D_{2}^{*}, D^{*}$ is a positively charged (neutral) $D^{*}, \pi$ is a negatively (positively) charged pion and $D$ is a positively charged (neutral) $D$ (charge conjugation is implied). In this system $D_{1,2}$ and $\pi$ in the initial decay and $D$ and $\pi^{0}$ in the subsequent decay are produced with back-to-back momenta. The momenta of particles in this system are:

$$
P_{\pi}^{2}=\left(\frac{M^{2}-M_{D^{*}}^{2}-M_{\pi}^{2}}{2 M_{D^{*}}}\right)^{2}-M_{\pi}^{2},
$$

where $M$ is the $D_{1,2}$ mass;

$$
P_{D}^{2}=P_{\pi^{0}}^{2}=\left(\frac{M_{D^{*}}^{2}-M_{D}^{2}+M_{\pi^{0}}^{2}}{2 M_{D^{*}}}\right)^{2}-M_{\pi^{0}}^{2} .
$$

The measured $M(D \pi)$ is given by

$$
M_{m}^{2}=M^{2}(D \pi)=M_{D}^{2}+M_{\pi}^{2}+2 \sqrt{\left(P_{D}^{2}+M_{D}^{2}\right)\left(P_{\pi}^{2}+M_{\pi}^{2}\right)}-2 P_{D} P_{\pi} \cos \alpha
$$

where $\alpha$ is the helicity angle between $\pi^{0}$ and $\pi$. Using the equations above, $M_{m}$ can be parametrised as:

$$
\begin{equation*}
M_{m}^{2}=M^{2}(1-a)+b+g \sqrt{\left(M^{2}-d_{1}\right)\left(M^{2}-d_{2}\right)} \cos \alpha, \tag{16}
\end{equation*}
$$

where

$$
\begin{aligned}
& a=\left(M_{D^{*}}^{2}+M_{\pi^{0}}^{2}-M_{D}^{2}\right) /\left(2 M_{D^{*}}^{2}\right), \\
& b=M_{\pi^{0}}^{2}-\left(M_{D^{*}}^{2}-M_{\pi}^{2}\right)\left(M_{D^{*}}^{2}+M_{\pi^{0}}^{2}-M_{D}^{2}\right) /\left(2 M_{D^{*}}^{2}\right), \\
& g=\sqrt{\left(M_{D^{*}}^{2}+M_{\pi^{0}}^{2}-M_{D}^{2}\right)^{2}-4 M_{D^{*}}^{2} M_{\pi^{0}}^{2}} /\left(2 M_{D^{*}}^{2}\right), \\
& d_{1}=\left(M_{D^{*}}+M_{\pi}\right)^{2}, \\
& d_{2}=\left(M_{D^{*}}-M_{\pi}\right)^{2} .
\end{aligned}
$$

From Eq. (16), $M$ is obtained as a function of $M_{m}$ and $\alpha$

$$
M=M\left(M_{m}, \alpha\right) .
$$

If the spectrum shape of $M$ is

$$
\frac{d N}{d M}=f(M),
$$

where $N$ is the number of candidates, then the $M_{m}$ spectrum shape is

$$
\frac{d N}{d M_{m}}=f\left(M\left(M_{m}\right)\right) \frac{d M}{d M_{m}} .
$$

Combining Eq. (16) with the normalised helicity angular distribution

$$
\frac{d N}{d(\cos \alpha)}=\frac{1+h \cos ^{2} \alpha}{2(1+h / 3)}
$$

yields

$$
\frac{d^{2} N}{d M_{m} d(\cos \alpha)}=f\left(M\left(M_{m}, \alpha\right)\right) \frac{d M}{d M_{m}} \frac{1+h \cos ^{2} \alpha}{2(1+h / 3)} .
$$

The fit uses the integral over $\cos \alpha$

$$
\begin{equation*}
\frac{d N}{d M_{m}}=\int_{-1}^{1} f\left(M\left(M_{m}, \alpha\right)\right) \frac{d M}{d M_{m}} \frac{1+h \cos ^{2} \alpha}{2(1+h / 3)} d(\cos \alpha) \tag{17}
\end{equation*}
$$

Here $f(M)$ is parametrised by a relativistic Breit-Wigner function as for the prompt signals.
For the description of the $D^{0} \pi$ spectrum, the $D^{* 0} \rightarrow D^{0} \gamma$ decay was also taken into account by replacing $M_{\pi^{0}}$ with $M_{\gamma}=0$ in the equations above. For the description of the $D^{+} \pi$ spectrum, the contribution of the $D^{*+} \rightarrow D^{+} \gamma$ decay was neglected [16].

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    61 The corresponding anti-particle decays were also measured. Hereafter, charge conjugation is implied.
    62 The ZEUS coordinate system is a right-handed Cartesian system, with the $Z$ axis pointing in the nominal proton beam direction, referred to as the "forward direction", and the $X$ axis pointing left towards the centre of HERA. The coordinate origin is at the centre of the CTD. The pseudorapidity is defined as $\eta=-\ln \left(\tan \frac{\theta}{2}\right)$, where the polar angle, $\theta$, is measured with respect to the $Z$ axis.

