Observation of the isospin-violating decay $J/\psi \rightarrow \phi \pi^0 f_0(980)$

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Using a sample of $1.31 \times 10^9 J/\psi$ events collected with the BESIII detector at the BEPCII collider, the decays $J/\psi \to \phi \pi^+ \pi^- \pi^0$ and $J/\psi \to \phi \pi^0 \pi^0 \pi^0$ are investigated. The isospin-violating decay $J/\psi \to \phi \pi^0 f_0(980)$ with $f_0(980) \to \pi \pi$ is observed for the first time. The width of the $f_0(980)$ obtained from the dipion mass spectrum is found to be much smaller than the world average value. In the $\pi^0 f_0(980)$ mass spectrum, there is evidence of $f_1(1285)$ production. By studying the decay $J/\psi \to \phi \eta'$, the branching fractions of $\eta' \to \pi^+ \pi^- \pi^0$ and $\eta' \to \pi^0 \pi^0 \pi^0$, as well as their ratio, are also measured.

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I. INTRODUCTION

The nature of the scalar meson $f_0(980)$ is a longstanding puzzle. It has been interpreted as a $q\bar{q}$ state, a $K\bar{K}$ molecule, a glueball, and a four-quark state (see the review in Ref. [1]). Further insights are expected from studies of $f_0(980)$ mixing with the $a_0^0(980)$ [2], evidence for which was found in a recent BESIII analysis of J/ψ and χ_{c1} decays [3]. BESIII also observed a large isospin violation in J/ψ radiatively decaying into $\pi^+\pi^-\pi^0$ and $\pi^0\pi^0\pi^0$ involving the intermediate decay $\eta(1405) \rightarrow \pi^0 f_0(980)$ [4]. In this study, the $f_0(980)$ width was found to be $9.5 \pm 1.1 \text{ MeV}/c^2$. One proposed explanation for this anomalously narrow width and the observed large isospin violation, which cannot be caused by $a_0^0(980) - f_0(980)$ mixing, is the triangle singularity mechanism [5,6].

The decays $J/\psi \rightarrow \phi \pi^+ \pi^- \pi^0$ and $J/\psi \rightarrow \phi \pi^0 \pi^0 \pi^0$ are similar to the radiative decays $J/\psi \rightarrow \gamma \pi^+ \pi^- \pi^0/\pi^0 \pi^0 \pi^0$ as the ϕ and γ share the same spin and parity quantum numbers. Any intermediate $f_0(980)$ would be noticeable in the $\pi\pi$ mass spectra. At the same time, a study of the decay $J/\psi \rightarrow \phi \eta'$ would enable a measurement of the branching fractions for $\eta' \rightarrow \pi^+ \pi^- \pi^0$ and $\eta' \rightarrow \pi^0 \pi^0 \pi^0$. The recently measured $\mathcal{B}(\eta' \rightarrow 3\pi^0) = (3.56 \pm 0.40) \times 10^{-3}$ [4] from a study of the decay $J/\psi \rightarrow \gamma \eta'$ was found to be nearly 4σ higher than the previous value $(1.73 \pm 0.23) \times 10^{-3}$ from studies of the reaction $\pi^- p \rightarrow n(6\gamma)$ [7–9].¹ Additionally, the isospin-violating decays $\eta' \rightarrow \pi^+ \pi^- \pi^0/\pi^0 \pi^0 \pi^0$ provide a means to extract the d, u quark mass difference $m_d - m_u$ [10].

This paper reports a study of $J/\psi \rightarrow \phi \pi^+ \pi^- \pi^0$ and $J/\psi \rightarrow \phi \pi^0 \pi^0 \pi^0 \pi^0$ with $\phi \rightarrow K^+ K^-$ based on a sample of $(1.311 \pm 0.011) \times 10^9$ [11,12] J/ψ events accumulated with the BESIII detector in 2009 and 2012.

II. DETECTOR AND MONTE CARLO SIMULATION

The BESIII detector [13] is a magnetic spectrometer located at the Beijing Electron-Positron Collider (BEPCII), which is a double-ring e^+e^- collider with a design luminosity of 10³³ cm⁻² s⁻¹ at a center-of-mass (c.m.) energy of 3.773 GeV. The cylindrical core of the BESIII detector consists of a helium-based main drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC). All are enclosed in a superconducting solenoidal magnet providing a 1.0 T (0.9 T in 2012) magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identifier modules interleaved with steel. The acceptance for charged tracks and photons is 93% of 4π solid angle. The charged-particle momentum resolution is 0.5% at 1 GeV/c, and the specific energy loss (dE/dx) resolution is better than 6%. The photon energy is measured in the EMC with a resolution of 2.5% (5%) at 1 GeV in the barrel (end caps). The time resolution of the TOF is 80 ps (110 ps) in the barrel (end caps). The BESIII offline software system framework, based on the GAUDI package [14], provides standard interfaces and utilities for event simulation, data processing and physics analysis.

Monte Carlo (MC) simulation, based on the GEANT4 [15] package, is used to simulate the detector response, study the background and determine efficiencies. For this analysis, we use a phase space MC sample to describe the three-body decay $J/\psi \rightarrow \phi \pi^0 f_0(980)$, while the angular distributions are considered in the decays $J/\psi \rightarrow \phi f_1(1285) \rightarrow \phi \pi^0 f_0(980)$ and $J/\psi \rightarrow \phi \eta'$. In the MC samples, the width of the $f_0(980)$ is fixed to be 15.3 MeV/ c^2 , which is obtained from a fit to data as described below. An inclusive MC sample of $1.2 \times 10^9 J/\psi$ decays is used to study the background. For this MC sample, the generator BESEVTGEN [16,17] is used to generate the known J/ψ decays according to their measured branching fractions [1], while LUNDCHARM [18] is used to generate the remaining unknown decays.

¹The PDG [1] gives an average value, $\Gamma(\eta' \to 3\pi^0)/\Gamma(\eta' \to \pi^0\pi^0\eta) = 0.0078 \pm 0.0010$, of three measurements [7–9]. $\mathcal{B}(\eta' \to 3\pi^0)$ is calculated using $\mathcal{B}(\eta' \to \pi^0\pi^0\eta) = 0.222 \pm 0.008$ [1], assuming the uncertainties are independent.

III. EVENT SELECTION

Charged tracks are reconstructed from hits in the MDC and selected by requiring that $|\cos \theta| < 0.93$, where θ is the polar angle measured in the MDC, and that the point of closest approach to the e^+e^- interaction point is within ± 10 cm in the beam direction and within 1 cm in the plane perpendicular to the beam direction. TOF and dE/dxinformation are combined to calculate the particle identification (PID) probabilities for the pion, kaon and proton hypotheses. For each photon, the energy deposited in the EMC must be at least 25 MeV (50 MeV) in the region of $|\cos \theta| < 0.8 \ (0.86 < |\cos \theta| < 0.92)$. To exclude showers that originate from charged tracks, the angle between a photon candidate and the closest charged track must be larger than 10°. The timing information from the EMC is used to suppress electronics noise and unrelated energy deposits.

To be accepted as a $J/\psi \to K^+ K^- \pi^+ \pi^- \pi^0$ decay, a candidate event is required to have four charged tracks with zero net charge and at least two photons. The two oppositely charged tracks with an invariant mass closest to the nominal mass of the ϕ are assigned as being kaons, while the remaining tracks are assigned as being pions. To avoid misidentification, kaon tracks are required to have a PID probability of being a kaon that is larger than that of being a pion. A five-constraint kinematic fit is applied to the candidate events under the hypothesis $J/\psi \rightarrow$ $K^+K^-\pi^+\pi^-\gamma\gamma$. This includes a constraint that the total four-momenta of the selected particles must be equal to the initial four-momentum of the colliding beams (fourconstraint) and that the invariant mass of the two photons must be the nominal mass of the π^0 (one-constraint). If more than two photon candidates are found in the event, the combination with the minimum $\chi^2(5C)$ from the kinematic fit is retained. Only events with a $\chi^2(5C)$ less than 100 are accepted. Events with a $K^{\pm}\pi^{\mp}$ invariant mass satisfying $|M(K^{\pm}\pi^{\mp}) - M(K^{*0})| < 0.050 \text{ GeV}/c^2$ are rejected in order to suppress the background containing K^{*0} or \bar{K}^{*0} intermediate states.

To be accepted as a $J/\psi \to K^+ K^- \pi^0 \pi^0 \pi^0$ decay, a candidate event is required to have two oppositely charged tracks and at least six photons. For both tracks, the PID probability of being a kaon must be larger than that of being a pion. The six photons are selected and paired by minimizing the quantity $\frac{(M(\gamma_1\gamma_2)-M_{\pi^0})^2}{\sigma_{\pi^0}^2} + \frac{(M(\gamma_3\gamma_4)-M_{\pi^0})^2}{\sigma_{\pi^0}^2} + \frac{(M(\gamma_5\gamma_6)-M_{\pi^0})^2}{\sigma_{\pi^0}^2}$, where $M(\gamma_i\gamma_j)$ is the mass of $\gamma_i\gamma_j$, and M_{π^0} and σ_{π^0} are the nominal mass and reconstruction resolution of the π^0 , respectively. A seven-constraint kinematic fit is performed on the $J/\psi \to K^+ K^- 6\gamma$ hypothesis, where the constraints include the four-momentum constraint to the four-momentum of the colliding beams and three constraints of photon pairs to have invariant

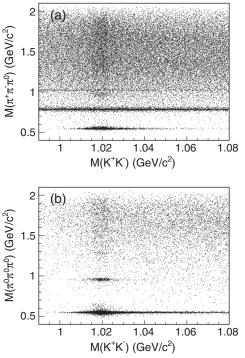


FIG. 1. Scatter plots of (a) $M(\pi^+\pi^-\pi^0)$ versus $M(K^+K^-)$ and (b) $M(\pi^0\pi^0\pi^0)$ versus $M(K^+K^-)$.

masses equal to the π^0 . Events with a $\chi^2(7C)$ less than 90 are accepted.

Figures 1(a) and 1(b) show $M(3\pi)$ versus $M(K^+K^-)$ for the two final states, respectively. Clear signals from $\phi\eta$ and $\phi\eta'$ with $\eta' \to 3\pi^0$ are noticeable. In Fig. 1(a), horizontal bands are noticeable from ω and ϕ decaying into $\pi^+\pi^-\pi^0$ in the background channel $J/\psi \to \omega/\phi K^+K^-$.

To search for the decay $J/\psi \rightarrow \phi \pi^0 f_0(980)$, we focus on the region $0.99 < M(K^+K^-) < 1.06 \text{ GeV}/c^2$ and $0.850 < M(\pi\pi) < 1.150 \text{ GeV}/c^2$. The $M(K^+K^-)$ spectra are shown in Fig. 2. Clear ϕ signals are visible. The $M(\pi^+\pi^-)$ and $M(\pi^0\pi^0)$ spectra for the ϕ signal region, which is defined by requiring $1.015 < M(K^+K^-) <$ $1.025 \text{ GeV}/c^2$, are presented in Figs. 3(a) and 3(b), respectively. A clear $f_0(980)$ peak exists for the $\pi^+\pi^$ mode. The $M(f_0(980)[\pi\pi]\pi^0)$ spectra for the $f_0(980)$ signal region, defined as $0.960 < M(\pi\pi) < 1.020 \text{ GeV}/c^2$, are presented in Fig. 4. There is evidence of a resonance around $1.28 \text{ GeV}/c^2$ for the decay $f_0(980) \rightarrow \pi^+\pi^-$, which will be identified as the $f_1(1285)$.²

To ensure that the observed f_0 and f_1 signals do not originate from background processes, the same selection criteria as described above are applied to a MC sample of 1.2×10^9 inclusive J/ψ decays which does not contain the signal decay. As expected, neither an f_1 nor an f_0 is

²For simplicity, $f_0(980)$ and $f_1(1285)$ will be written as f_0 and f_1 , respectively, throughout this paper.

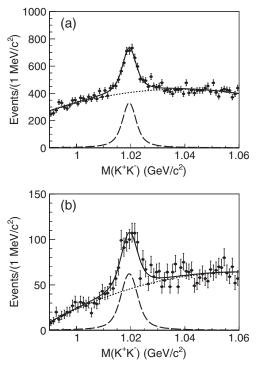


FIG. 2. Fits to the $M(K^+K^-)$ mass spectra for the modes (a) $f_0(980) \rightarrow \pi^+\pi^-$ and (b) $f_0(980) \rightarrow \pi^0\pi^0$. The solid curve is the full fit, the long-dashed curve is the ϕ signal, and the shortdashed curve is the background.

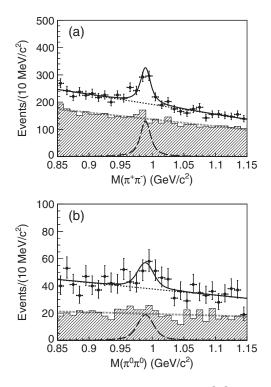


FIG. 3. The spectra (a) $M(\pi^+\pi^-)$ and (b) $M(\pi^0\pi^0)$ (three entries per event) with K^+K^- in the ϕ signal region (black dots) and in the ϕ sideband regions (hatched histogram). The solid curve is the full fit, the long-dashed curve is the $f_0(980)$ signal, the dotted line is the non- ϕ background, and the short-dashed line is the total background.

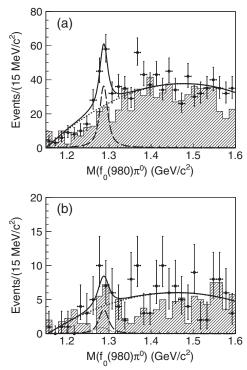


FIG. 4. The spectra of (a) $M(\pi^+\pi^-\pi^0)$ and (b) $M(\pi^0\pi^0\pi^0)$ in the ϕ and $f_0(980)$ signal region (black dots with error bars) and in the sideband regions (hatched histogram). The solid curve is the result of the fit, the long-dashed curve is the $f_1(1285)$ signal, and the short-dashed curve is the background. In (b), the dotted curve represents the peaking background from the decay $f_1(1285) \rightarrow \pi^0 \pi^0 \eta / \pi^0 a_0^0$ with $\eta \rightarrow \gamma \gamma$.

observed from the inclusive MC sample. The non- ϕ background is studied using data from the ϕ sideband regions $[0.990 < M(K^+K^-) < 1.000 \text{ GeV}/c^2$ and $1.040 < M(K^+K^-) < 1.050 \text{ GeV}/c^2]$, which are given by the hatched histograms in Figs. 3 and 4 and in which no f_0 or f_1 signals are observed.

IV. SIGNAL EXTRACTION OF $J/\psi \rightarrow \phi \pi^0 f_0(980)$

Figures 3(a) and 3(b) show the $\pi^+\pi^-$ and $\pi^0\pi^0$ mass spectra for events with $M(K^+K^-)$ in the ϕ signal region (black dots) and sideband regions (the hatched histogram scaled by a normalization factor, *C*). Events in the ϕ sideband regions are normalized in the following way. A fit is performed on the K^+K^- mass spectrum, where the ϕ signal is described by a Breit-Wigner function convoluted with a Gaussian resolution function and the background is described by a second-order polynomial. The mass and width of the ϕ resonance are fixed to their world average values [1], and the mass resolution is allowed to float. The normalization factor *C* is defined as $A_{\text{sig}}/A_{\text{sbd}}$, where A_{sig} (A_{sbd}) is the area of the background function from the fits in the signal (sideband) region. The results of the fits are shown in Figs. 2(a) and 2(b).

To extract the signal yield of $J/\psi \rightarrow \phi \pi^0 f_0$, a simultaneous unbinned maximum likelihood fit is performed on the $\pi^+\pi^-$ and $\pi^0\pi^0$ mass spectra. The line shape of the f_0 signal is different from that of the Flatté-form resonance observed in the decays $J/\psi \to \phi \pi^+ \pi^-$ and $J/\psi \to \phi K^+ K^-$ [19]. A Breit-Wigner function convoluted with a Gaussian mass resolution function is used to describe the f_0 signal. The mass resolutions of the f_0 in the $M(\pi^+\pi^-)$ and $M(\pi^0\pi^0)$ spectra are determined from MC simulations. The non- ϕ background is parametrized with a straight line, which is determined from a fit to the data in the ϕ sideband regions. The size of this polynomial is fixed according to the normalized number of background events under the ϕ peak, $N_{\rm bkg} = CN_{\rm sbd}$, where $N_{\rm sbd}$ is the number of events falling in the ϕ sideband regions and C is the normalization factor obtained above. Another straight line is used to account for the remaining background from $J/\psi \rightarrow \phi \pi^0 \pi \pi$ without f_0 decaying into $\pi\pi$.

The mass and width of the f_0 are constrained to be the same for both the $K^+K^-\pi^+\pi^-\pi^0$ and the $K^+K^-\pi^0\pi^0\pi^0$ final states. The fit yields the values $M(f_0) = 989.4 \pm$ 1.3 MeV/ c^2 and $\Gamma(f_0) = 15.3 \pm 4.7$ MeV/ c^2 , with the number of events $N = 354.7 \pm 63.3$ for the $\pi^+\pi^-$ mode and 69.8 ± 21.1 for the $\pi^0 \pi^0$ mode. The statistical significance is determined by the changes of the log likelihood value and the number of degrees of freedom in the fit with and without the signal [20]. The significance of the f_0 signal is 9.4 σ in the $K^+K^-\pi^+\pi^-\pi^0$ final state and 3.2 σ in the $K^+K^-\pi^0\pi^0\pi^0$ final state. The measured mass and width obtained from the invariant dipion mass spectrum are consistent with those from the study of the decay $J/\psi \rightarrow$ $\gamma\eta(1405) \rightarrow \gamma\pi^0 f_0(980)$ [4]. It is worth noting that the measured width of the f_0 observed in the dipion mass spectrum is much smaller than the world average value of 40-100 MeV [1].

V. SIGNAL EXTRACTION OF $J/\psi \rightarrow \phi f_1(1285)$ WITH $f_1(1285) \rightarrow \pi^0 f_0(980)$

Figures 4(a) and 4(b) show the $\pi^+\pi^-\pi^0$ and $\pi^0\pi^0\pi^0$ mass spectra in the ϕ and f_0 signal region (black dots) and sideband regions (hatched histogram). The f_0 sideband regions are defined as $0.850 < M(\pi\pi) < 0.910 \text{ GeV}/c^2$ and $1.070 < M(\pi\pi) < 1.130 \text{ GeV}/c^2$. In Fig. 4, events in the two-dimensional sideband regions are weighted as follows. Events that fall in only the ϕ or $f_0(980)$ sideband regions are given a weight 0.5 to take into account the non- ϕ or non- $f_0(980)$ background, while those that fall in both the ϕ and the $f_0(980)$ sideband regions are given a weight -0.25 to compensate for the double counting of the non- ϕ and non- $f_0(980)$ background. There is evidence of a resonance around 1.28 GeV/ c^2 that is not noticeable in the two-dimensional sideband regions. By studying a MC sample of the decay $J/\psi \rightarrow \phi f_1 \rightarrow$ anything, we find that

TABLE I. Summary of the observed number of events (N^{obs} , the errors are statistical only).

Decay mode	$N^{ m obs}$
$\frac{1}{J/\psi \to \phi \pi^0 f_0, f_0 \to \pi^+ \pi^-}$	354.7 ± 63.3
$J/\psi \rightarrow \phi \pi^0 f_0, f_0 \rightarrow \pi^0 \pi^0$	69.8 ± 21.1
$J/\psi \rightarrow \phi f_1, f_1 \rightarrow \pi^0 f_0, f_0 \rightarrow \pi^+ \pi^-$	78.2 ± 19.3
$J/\psi \rightarrow \phi f_1, f_1 \rightarrow \pi^0 f_0, f_0 \rightarrow \pi^0 \pi^0$	8.7 ± 6.8
	<18.2 (90% C.L.)
$J/\psi ightarrow \phi \eta', \eta' ightarrow \pi^+ \pi^- \pi^0$	183.3 ± 21.0
$J/\psi \to \phi \eta', \eta' \to \pi^0 \pi^0 \pi^0$	77.6 ± 9.6

the decay $f_1 \rightarrow \pi^0 \pi^0 \eta / \pi^0 a_0^{03}$ with $\eta \rightarrow \gamma \gamma$ contributes as a peaking background for the decay $f_1 \rightarrow \pi^0 \pi^0 \pi^0$. The yield of this peaking background is calculated to be 3.1 ± 0.6 using the relevant branching fractions⁴ [1], and the efficiency is determined from a MC simulation. A simultaneous unbinned maximum likelihood fit is performed on the $M(\pi^+\pi^-\pi^0)$ and $M(\pi^0\pi^0\pi^0)$ distributions. The f_1 signal is described by a Breit-Wigner function convoluted with a Gaussian mass resolution function. The shape of the peaking background $f_1 \rightarrow \pi^0 \pi^0 \eta / \pi^0 a_0^0$ is determined from an exclusive MC sample and its size is fixed to be 3.1. A second-order polynomial function is used to describe the remaining background. The mass resolutions of the f_1 in $M(\pi^+\pi^-\pi^0)$ and $M(\pi^0\pi^0\pi^0)$ are determined from MC simulations.

The fit to $M(\pi^+\pi^-\pi^0)$ and $M(\pi^0\pi^0\pi^0)$ distributions yields the values $M(f_1) = 1287.4 \pm 3.0 \text{ MeV}/c^2$ and $\Gamma(f_1) = 18.3 \pm 6.3 \text{ MeV}/c^2$, with the number of events $N = 78.2 \pm 19.3$ for the $K^+K^-\pi^+\pi^-\pi^0$ final state and N = 8.7 ± 6.8 [<18.2 at the 90% confidence level (C.L.)] for the $K^+K^-\pi^0\pi^0\pi^0$ final state. The mass and width are consistent with those of the axial-vector meson f_1 [1].⁵ The statistical significance of the f_1 signal is 5.2 σ for the $K^+K^-\pi^+\pi^-\pi^0$ final state and 1.8σ for the $K^+K^-\pi^0\pi^0\pi^0$ final state. From the fit results, summarized in Table I, it is clear that the production of a single f_1 resonance cannot account for all of the $f_0\pi^0$ events above the background.

VI. SIGNAL EXTRACTION OF $J/\psi \rightarrow \phi \eta'$

For the decay $J/\psi \to \phi \eta' \to K^+ K^- \pi^+ \pi^- \pi^0$, the decays $J/\psi \to \phi \eta' \to K^+ K^- \gamma \rho[(\gamma) \pi^+ \pi^-]$ and $J/\psi \to \phi \eta' \to$ $K^+K^-\gamma\omega[\pi^+\pi^-\pi^0]$ produce peaking background. To reduce

³For simplicity, $a_0(980)$ and $a_0^0(980)$ are written as a_0 and

^a⁰, respectively, throughout this paper. ⁴We assume that $\mathcal{B}(f_1 \to \pi^0 \pi^0 \eta) = \frac{1}{3}\mathcal{B}(f_1 \to \pi \pi \eta),$ $\mathcal{B}(f_1 \to \pi^0 a_0^0) = \frac{1}{3}\mathcal{B}(f_1 \to \pi a_0),$ and $\mathcal{B}(a_0^0 \to \pi^0 \eta) = 100\%.$

Here we assume that the contribution of the pseudoscalar $\eta(1295)$ is small as no significant $\eta(1295)$ signals were found in the $\pi^+\pi^-\eta$ mass spectrum from a study of $J/\psi \to \phi \pi^+\pi^-\eta$ [21].

the former peaking background which is dominant, events with $0.920 < M(\gamma \pi^+ \pi^-) < 0.970 \text{ GeV}/c^2$ are rejected.

As the amount of background for the decay $J/\psi \rightarrow \phi \eta' \rightarrow K^+ K^- \pi^0 \pi^0 \pi^0$ is relatively small, the ϕ signal and sideband regions are expanded to be $1.010 < M(K^+K^-) < 1.030 \text{ GeV}/c^2$ and $1.040 < M(K^+K^-) < 1.060 \text{ GeV}/c^2$, respectively. A peaking background for this decay comes from the decay $J/\psi \rightarrow \phi \eta' \rightarrow K^+ K^- \pi^0 \pi^0 \eta [\gamma \gamma]$. To reduce this background, events with any photon pair mass in the range $0.510 < M(\gamma \gamma) < 0.580 \text{ GeV}/c^2$ are rejected.

Figures 5(a) and 5(b) show the final $\pi^+\pi^-\pi^0$ and $\pi^0\pi^0\pi^0$ mass spectra for the ϕ signal (black dots) and sideband (hatched histogram) regions. By analyzing data in the ϕ sideband regions and the inclusive MC sample, we find that the contribution from the decay $J/\psi \to K^+K^-\eta'$ is negligible.

An unbinned likelihood fit is performed to obtain the signal yields. The η' signal shape is determined by sampling a histogram from a MC simulation convoluted with a Gaussian function to compensate for the resolution difference between the data and the MC sample. The shape of the peaking background is determined from exclusive MC samples, where the relative size of the

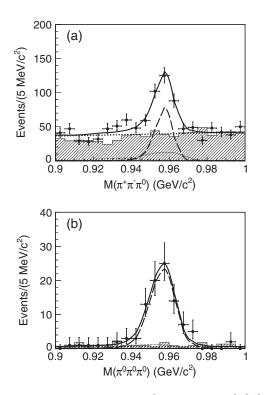


FIG. 5. The spectra (a) $M(\pi^+\pi^-\pi^0)$ and (b) $M(\pi^0\pi^0\pi^0)$ with K^+K^- in the ϕ signal region (black dots) and sideband regions (hatched histogram). The solid curve is the result of the fit, the long-dashed curve is the η' signal, and the short-dashed line is the polynomial background. In (a), the dotted and dot-dashed curves represent the peaking background $\eta' \to \gamma \rho \to \gamma(\gamma)\pi^+\pi^-$ and $\eta' \to \gamma \omega \to \gamma \pi^+\pi^-\pi^0$, respectively. In (b), the dotted curve represents the peaking background $\eta' \to \pi^0\pi^0\eta$ with $\eta \to \gamma\gamma$.

background shape is determined using the relevant branching fractions in the PDG [1]. The nonpeaking background is described by a first-order (zeroth-order) polynomial for the $\eta' \rightarrow \pi^+\pi^-\pi^0$ ($\pi^0\pi^0\pi^0$) decay. The number of events is determined to be $N = 183.3 \pm 21.0$ for the $K^+K^-\pi^+\pi^-\pi^0$ final state and 77.6 \pm 9.6 for the $K^+K^-\pi^0\pi^0\pi^0$ final state.

VII. BRANCHING FRACTION MEASUREMENT

Table I summarizes the signal yields extracted from the fits for each decay. Equations (1) and (2) give the formulas used to calculate the branching fractions, where *n* is the number of π^0 s in the final state *X*. N^{obs} and ϵ are the signal yield from the fits and efficiency from the MC simulation for each decay, respectively. B_{YZ}^X is the branching fraction of the decay $X \to YZ$. $N_{J/\psi}$ is the number of J/ψ events. The upper limit of $\mathcal{B}(J/\psi \to \phi f_1, f_1 \to \pi^0 f_0, f_0 \to \pi^0 \pi^0)$ is determined according to Eq. (3), where $N_{\text{upp}}^{\text{obs}}$ is the signal yield at the 90% C.L. and σ^{sys} is the total systematic uncertainty, which is described in the next section. Equation (4) is used to calculate the ratio between the branching fraction for $\eta' \to \pi^0 \pi^0 \pi^0$ and that for $\eta' \to \pi^+ \pi^- \pi^0$.

$$\mathcal{B}(J/\psi \to \phi X) = \frac{N^{\text{obs}}}{N_{J/\psi} \epsilon B^{\phi}_{K^+ K^-} (B^{\pi^0}_{\gamma\gamma})^n}, \qquad (1)$$

$$\mathcal{B}(\eta' \to X) = \frac{N^{\text{obs}}}{N_{J/\psi} \epsilon B^{J/\psi}_{\phi\eta'} B^{\phi}_{K^+K^-} (B^{\pi^0}_{\gamma\gamma})^n}, \qquad (2)$$

$$\mathcal{B}(J/\psi \to \phi X) < \frac{N_{\rm upp}^{\rm obs}}{N_{J/\psi} \epsilon B_{K^+K^-}^{\phi} (B_{\gamma\gamma}^{\pi^0})^n (1 - \sigma^{\rm sys})}, \quad (3)$$

$$r_{3\pi} \equiv \mathcal{B}(\eta' \to \pi^0 \pi^0 \pi^0) / \mathcal{B}(\eta' \to \pi^+ \pi^- \pi^0) \\ = \frac{N^{\text{obs}}(\pi^0 \pi^0 \pi^0)}{N^{\text{obs}}(\pi^+ \pi^- \pi^0)} \frac{\epsilon(\pi^+ \pi^- \pi^0)}{\epsilon(\pi^0 \pi^0 \pi^0)} \frac{1}{(B^{\pi^0}_{\gamma\gamma})^2}.$$
 (4)

VIII. ESTIMATION OF THE SYSTEMATIC UNCERTAINTIES

- (1) *MDC tracking*: The tracking efficiency of kaon tracks is studied using a high purity sample of $J/\psi \rightarrow K_S K \pi$ events. The tracking efficiency of the low-momentum pion tracks is studied using a sample of $J/\psi \rightarrow \pi^+ \pi^- p \bar{p}$ while that of the high-momentum pion tracks is studied using a high statistics sample of $J/\psi \rightarrow \rho \pi$. The MC samples and data agree within 1% for each kaon or pion track.
- (2) *Photon detection*: The photon detection efficiency is studied using a sample of $J/\psi \rightarrow \rho \pi$ events. The systematic uncertainty for each photon is 1% [22].

- (3) *PID efficiency*: To study the PID efficiency for kaon tracks, we select a clean sample of $J/\psi \rightarrow \phi \eta \rightarrow K^+ K^- \gamma \gamma$. The PID efficiency is the ratio of the number of events with and without the PID requirement for both kaon tracks. MC simulation is found to agree with data within 0.5%.
- (4) Kinematic fit: The performance of the kinematic fit is studied using a sample J/ψ → φη → K⁺K⁻π⁺π⁻π⁰/K⁺K⁻π⁰π⁰π⁰, which has the same final states as the signal channel J/ψ → φπ⁰f₀ with φ → K⁺K⁻ and f₀ → π⁺π⁻/π⁰π⁰. The control sample is selected without using the kinematic constraints. We then apply the same kinematic constraints and the same requirement on the χ² from the kinematic fit. The efficiency is the ratio of the yields with and without the kinematic fit. It contributes a systematic uncertainty of 1.0% for f₀ → π⁺π⁻ and 2.0% for f₀ → π⁰π⁰.
- (5) Veto neutral K^* : In selecting the candidate events $J/\psi \rightarrow \phi \pi^0 f_0 \rightarrow K^+ K^- \pi^+ \pi^- \pi^0$, the events with $|M(K^{\pm}\pi^{\mp}) M(K^{*0})| < 0.050 \text{ GeV}/c^2$ are vetoed to suppress the background containing K^{*0} or \bar{K}^{*0} intermediate states. The requirement is investigated using a clean sample $J/\psi \rightarrow \phi \eta \rightarrow K^+ K^- \pi^+ \pi^- \pi^0$. The efficiency is given by the yield ratio with and without the requirement $|M(K^{\pm}\pi^{\mp}) M(K^{*0})| < 0.050 \text{ GeV}/c^2$. The efficiency difference between data and MC is 0.1%.
- (6) φ signal region: The uncertainty due to the restriction on the φ signal region is studied with a high purity sample of J/ψ → φη' → K⁺K⁻π⁺π⁻η events as this sample is free of the background J/ψ → K⁺K⁻η' without the intermediate state φ.
- (7) *Veto peaking background*: The uncertainties due to the restrictions used to remove peaking background in the mode $\eta' \rightarrow 3\pi$ are studied with a control sample of $J/\psi \rightarrow \omega\eta \rightarrow 2(\pi^+\pi^-\pi^0)$ events. For each sample, the efficiency is estimated by comparing the yields with and without the corresponding requirement. The difference in efficiency between the data and MC samples is taken as the systematic uncertainty.
- (8) *Background shape*: To study the effect of the background shape, the fits are repeated with a different fit range or polynomial order. The largest difference in signal yield is taken as the systematic uncertainty.
- (9) Mass resolution: The mass resolutions $\sigma_{\rm MC}$ from a MC simulation of the modes $f_0 \rightarrow \pi^+ \pi^- / \pi^0 \pi^0$ and $f_1 \rightarrow \pi^0 f_0$ have an associated systematic uncertainty. The difference in mass resolution, σ_G , between the data and the MC simulation is determined using a sample of $J/\psi \rightarrow \phi \eta$ events where

 $\eta \rightarrow \pi^+ \pi^- \pi^0 / \pi^0 \pi^0 \pi^0$. The fit is repeated using different mass resolutions, which are defined as $\sqrt{\sigma_{\rm MC}^2 + \sigma_G^2}$ assuming σ_G is the same for the twopion and three-pion mass spectra. The difference in yield is taken as a systematic uncertainty.

- (10) *MC simulation*: For the decay $J/\psi \rightarrow \phi \pi^0 f_0$, the dominant systematic uncertainty is from the efficiency ϵ_0 determined by a phase space MC simulation. The $\pi^0 f_0$ invariant mass spectrum is divided into 5 bins, each with a bin width of 0.2 GeV/ c^2 . The f_0 signal yields, N_i , are determined by fits to the $\pi\pi$ spectra for each bin *i* using the mass and width of the f_0 obtained above. The corrected efficiency is $\epsilon_M \equiv \sum_{i} N_i N_i$, where ϵ_i is the efficiency in the *i*th bin. The same procedure is applied to the angular distribution of the $\pi^0 f_0$ system in the c.m. frame of the J/ψ to obtain another corrected efficiency ϵ_{θ} . The difference $\sqrt{(\epsilon_M \epsilon_0)^2 + (\epsilon_{\theta} \epsilon_0)^2}$ is taken as the systematic uncertainty due to the imperfection of the MC simulation.
- (11) f_0 signal region: For the decay $J/\psi \rightarrow \phi f_1$ with $f_1 \rightarrow \pi^0 f_0$, the f_0 signal region is 0.960 < $M(\pi\pi) < 1.020 \text{ GeV}/c^2$. The branching fraction measurements are repeated after varying this region to $0.970 < M(\pi\pi) < 1.010 \text{ GeV}/c^2$ and 0.950 < $M(\pi\pi) < 1.030 \text{ GeV}/c^2$. The differences from the nominal results are taken as the systematic uncertainties due to the signal region of the f_0 . For the decay $f_1 \rightarrow \pi^0 \pi^0 \pi^0$, the number of the peaking background $f_1 \rightarrow \pi^0 \pi^0 \eta [\gamma \gamma]$ is determined to be 3.1 ± 0.6 . Varying the number of the peaking background within ± 0.6 in the fit, the largest difference of the signal yield gives a systematic uncertainty. The systematic uncertainty values related to the f_1 are shown in brackets in Table II.
- (12) About $\mathcal{B}(J/\psi \to \phi f_1, f_1 \to \pi^0 f_0, f_0 \to \pi^0 \pi^0)$: For the decay $J/\psi \to \phi f_1, f_1 \to \pi^0 f_0$ with $f_0 \to \pi^0 \pi^0$, the signal yield at the 90% C.L., N_{upp}^{obs} in Eq. (3), is the largest one among the cases with varying the fit ranges, the order of the polynomial describing the background, the number of the peaking background, and the signal region of the f_0 resonance. The total systematic uncertainty, σ^{sys} in Eq. (3), is the quadratic sum of the rest of the systematic uncertainties in the third column of Table II (the values in the brackets). We obtain $N_{upp}^{obs} = 29.0$ and $\sigma^{sys} = 6.9\%$ with the efficiency $(7.21 \pm 0.08)\%$, determined from a MC simulation. $\mathcal{B}(J/\psi \to \phi f_1, f_1 \to \pi^0 f_0, f_0 \to \pi^0 \pi^0)$ is calculated to be less than 6.98×10^{-7} at the 90% C.L. according to Eq. (3).
- (13) Uncertainty of $\mathcal{B}(J/\psi \to \phi \eta')$: For the decay $\eta' \to 3\pi$, the dominant systematic uncertainty arises from

TABLE II. Summary of systematic uncertainties (%). For $f_0 \rightarrow \pi\pi$, the values in the brackets are for the decay $f_1 \rightarrow \pi^0 f_0$. For $\eta' \rightarrow 3\pi$, the systematic uncertainty from the uncertainty of the branching fraction (B.F.) of $J/\psi \rightarrow \phi\eta'$ is not included in the total quadratic sum. The last column lists the systematic uncertainties for the ratio between the branching fraction of $\eta' \rightarrow \pi^0 \pi^0 \pi^0$ and the branching fraction of $\eta' \rightarrow \pi^+ \pi^- \pi^0$, denoted by $r_{3\pi}$.

Sources	$f_0 \rightarrow \pi^+ \pi^-$	$f_0 \to \pi^0 \pi^0$	$\eta' ightarrow \pi^+ \pi^- \pi^0$	$\eta' \to 3\pi^0$	$r_{3\pi}$
MDC tracking	4.0	2.0	4.0	2.0	2.0
Photon detection	2.0	6.0	2.0	6.0	4.0
PID efficiency	0.5	0.5	0.5	0.5	
Kinematic fit	1.0	2.0	1.0	2.0	1.5
Veto neutral K^*	0.1				
ϕ signal region	1.1	1.1	1.1	0.5	0.5
Veto peaking bkg.			0.3	0.9	0.9
Background shape	5.4 (15.5)	4.4 (15.6)	1.3	0.3	1.4
Mass resolution	0.3 (0.4)	1.0 (0.1)			
MC simulation	11.4 (-)	11.4 (-)			
f_0 signal region	-(2.4)	-(68.2)			
$\mathcal{B}(J/\psi \to \phi \eta')$	••••	•••	25.6	22.8	
Peaking bkg.		-(6.9)			2.2
Number of J/ψ	0.8	0.8	0.8	0.8	
Other B.F.	1.0	1.0	1.0	1.0	0.1
Total	13.6 (16.5)	14.5 (70.6)	5.1	6.9	5.5

the uncertainty of $\mathcal{B}(J/\psi \to \phi \eta') = (4.0 \pm 0.7) \times 10^{-4}$ [1]. A variation in $\mathcal{B}(J/\psi \to \phi \eta')$ will change the size of the peaking background and thus the signal yield. In Eq. (2), it is reasonable to consider a change in the quantity $N^{\text{obs}}/B_{\phi\eta'}^{J/\psi}$ with any variation in $\mathcal{B}(J/\psi \to \phi \eta')$. The fit to the data is repeated after varying the number of peaking background to correspond with 1σ variations in $\mathcal{B}(J/\psi \to \phi \eta')$ [1]. The largest difference of $N^{\text{obs}}/B_{\phi\eta'}^{J/\psi}$ from the nominal result is taken as the systematic uncertainty.

(14) Systematic uncertainties for $r_{3\pi}$: In the measurement of the ratio $r_{3\pi}$ of $\mathcal{B}(\eta' \to \pi^0 \pi^0 \pi^0)$ over $\mathcal{B}(\eta' \to \pi^+ \pi^- \pi^0)$, the systematic uncertainties due to the reconstruction and identification of kaon tracks and photon detection cancel as the efficiency ratio $\epsilon(\pi^0 \pi^0 \pi^0)/\epsilon(\pi^+ \pi^- \pi^0)$ appears in Eq. (4). The effect of the uncertainty in the number of peaking background due to the uncertainty of $\mathcal{B}(J/\psi \rightarrow \phi \eta')$ is also considered.

All systematic uncertainties including those on the number of J/ψ events [12] and other relevant branching fractions from the PDG [1] are summarized in Table II, where the total systematic uncertainty is the quadratic sum of the individual contributions, assuming they are independent. Efficiency and branching fraction measurements are summarized in Table III.

IX. SUMMARY

In summary, we have studied the decay $J/\psi \rightarrow \phi 3\pi \rightarrow K^+ K^- 3\pi$. The isospin-violating decay $J/\psi \rightarrow \phi \pi^0 f_0$ is observed for the first time. In the $\pi^0 f_0$ mass spectrum, there is evidence of the axial-vector meson f_1 , but not all $\pi^0 f_0$ pairs come from the decay of

TABLE III. Summary of the efficiencies and the branching fractions. For the branching fractions, the first error indicates the statistical error and the second the systematic error. For $\mathcal{B}(\eta' \to 3\pi)$, the third error is due to the uncertainty of $\mathcal{B}(J/\psi \to \phi\eta')$ [1]. The last line gives the measured value of $r_{3\pi}$, defined as $\mathcal{B}(\eta' \to \pi^0 \pi^0 \pi^0)/\mathcal{B}(\eta' \to \pi^+ \pi^- \pi^0)$.

Decay mode	Efficiency (%)	Branching fractions
$\overline{J/\psi ightarrow \phi \pi^0 f_0, f_0 ightarrow \pi^+ \pi^-}$	12.44 ± 0.10	$(4.50 \pm 0.80 \pm 0.61) imes 10^{-6}$
$J/\psi \rightarrow \phi \pi^0 f_0, f_0 \rightarrow \pi^0 \pi^0$	6.76 ± 0.08	$(1.67 \pm 0.50 \pm 0.24) \times 10^{-6}$
$J/\psi \rightarrow \phi f_1, f_1 \rightarrow \pi^0 f_0 \rightarrow \pi^0 \pi^+ \pi^-$	13.19 ± 0.11	$(9.36 \pm 2.31 \pm 1.54) \times 10^{-7}$
$J/\psi \rightarrow \phi f_1, f_1 \rightarrow \pi^0 f_0 \rightarrow \pi^0 \pi^0 \pi^0$	6.76 ± 0.08	$(2.08 \pm 1.63 \pm 1.47) \times 10^{-7}$
		$<6.98 \times 10^{-7}$ (90% C. L.)
$\eta' ightarrow \pi^+ \pi^- \pi^0$	16.92 ± 0.12	$(4.28 \pm 0.49 \pm 0.22 \pm 1.09) \times 10^{-3}$
$\eta' o \pi^0 \pi^0 \pi^0$	6.55 ± 0.08	$(4.79 \pm 0.59 \pm 0.33 \pm 1.09) \times 10^{-3}$
$r_{3\pi}$		$1.12 \pm 0.19 \pm 0.06$

an f_1 . Using $\mathcal{B}(J/\psi \to \phi f_1) = (2.6 \pm 0.5) \times 10^{-4}$ and $\mathcal{B}(f_1 \to \pi a_0 \to \pi \pi \eta) = (36 \pm 7)\%$ from the PDG [1], the ratio $\mathcal{B}(f_1 \to \pi^0 f_0 \to \pi^0 \pi^+ \pi^-) / \mathcal{B}(f_1 \to \pi^0 a_0^0 \to \pi^0 \pi^0 \eta)$ is determined to be $(3.6 \pm 1.4)\%$ assuming isospin symmetry in the decay $f_1 \rightarrow a_0 \pi$. This value is only about 1/5 $\pi^0 \pi^0 \eta$ = (17.9 ± 4.2)% [4]. On the other hand, the measured mass and width of the f_0 obtained from the invariant dipion mass spectrum are consistent with those in the decay $J/\psi \rightarrow \gamma \eta (1405) \rightarrow \gamma \pi^0 f_0$ [4]. The measured f_0 width is much narrower than the world average value of 40–100 MeV [1]. It seems that there is a contradiction in the isospin-violating decays $f_1/\eta(1405) \rightarrow \pi^0 f_0$. However, a recent theoretical work [23], based on the triangle singularity mechanism as proposed in Refs. [5,6], analyzes the decay $f_1 \rightarrow \pi^0 f_0 \rightarrow \pi^0 \pi^+ \pi^$ and predicts that the width of the peaking structure in the f_0 region is about 10 MeV. It also derives $\mathcal{B}(f_1 \to \pi^0 f_0 \to \pi^0 \pi^+ \pi^-) / \mathcal{B}(f_1 \to \pi^0 a_0^0 \to \pi^0 \pi^0 \eta) \simeq 1\%,$ which is close to our measurement. This analysis supports the argument that the nature of the resonances a_0^0 and f_0 as dynamically generated makes the amount of isospin breaking strongly dependent on the physical process [23]. In addition, we have measured the branching fractions $\mathcal{B}(n' \rightarrow \pi^+ \pi^- \pi^0) = (4.28 \pm 0.49(\text{stat}) \pm 0.22(\text{syst}) \pm$ $(1.09) \times 10^{-3}$ and $\mathcal{B}(\eta' \to \pi^0 \pi^0 \pi^0) = (4.79 \pm 0.59 (\text{stat}) \pm 0.59 (\text{stat}))$ $0.33(\text{syst}) \pm 1.09) \times 10^{-3}$, where the last uncertainty is due to $\mathcal{B}(J/\psi \to \phi \eta')$. The ratio between them, $r_{3\pi} = 1.12 \pm 0.19 (\text{stat}) \pm 0.06 (\text{syst})$, is also measured for the first time. These results are consistent with those measured in the decay $J/\psi \rightarrow \gamma \eta'$ [4].

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- K. A. Olive *et al.* (Particle Data Group), Chin. Phys. C 38, 090001 (2014).
- [2] N. N. Achasov, S. A. Devyanin, and G. N. Shestakov, Phys. Lett. 88B, 367 (1979).
- [3] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D 83, 032003 (2011).
- [4] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. Lett. 108, 182001 (2012).
- [5] J. J. Wu, X. H. Liu, Q. Zhao, and B. S. Zou, Phys. Rev. Lett. 108, 081803 (2012).
- [6] F. Aceti, W. H. Liang, E. Oset, J. J. Wu, and B. S. Zou, Phys. Rev. D 86, 114007 (2012).
- [7] F. Binon *et al.* (IHEP-IISN-LAPP Collaboration), Phys. Lett. **140B**, 264 (1984).
- [8] D. Alde *et al.* (IHEP-IISN-LANL-LAPP Collaboration), Z. Phys. C **36**, 603 (1987).
- [9] A. Blik et al., Phys. At. Nucl. 71, 2124 (2008).

- [10] D. J. Gross, S. B. Treiman, and F. Wilczek, Phys. Rev. D 19, 2188 (1979).
- [11] M. Ablikim *et al.* (BESIII Collaboration), Chin. Phys. C 36, 915 (2012).
- [12] The total number of J/ψ events taken in 2009 and 2012 is determined to be 1.311×10^9 with an uncertainty of 0.8% using the same approach as in Ref. [11].
- [13] M. Ablikim *et al.*, Nucl. Instrum. Methods Phys. Res., Sect. A **614**, 345 (2010).
- [14] G. Barrand *et al.*, Comput. Phys. Commun. **140**, 45 (2001).
- [15] S. Agostinelli *et al.* (GEANT4 Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
- [16] D. J. Lange, Nucl. Instrum. Methods Phys. Res., Sect. A 462, 152 (2001).
- [17] R. G. Ping, Chin. Phys. C 32, 599 (2008).

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- [18] J. C. Chen, G. S. Huang, X. R. Qi, D. H. Zhang, and Y. S. Zhu, Phys. Rev. D 62, 034003 (2000).
- [19] M. Ablikim *et al.* (BES Collaboration), Phys. Lett. B 607, 243 (2005).
- [20] F. James *et al.*, *Statistic Methods in Experimental Physics*, 2nd ed. (World Scientific, Singapore, 2007).
- [21] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D 91, 052017 (2015).
- [22] M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D 83, 112005 (2011).
- [23] F. Aceti, J. M. Dias, and E. Oset, Eur. Phys. J. A 51, 48 (2015).