## Study of the $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ Dynamics and Test of Lepton Flavor Universality with $D^{0} \rightarrow K^{-} \ell^{+} \nu_{\ell}$ Decays

M. Ablikim, ${ }^{1}$ M. N. Achasov, ${ }^{9, \mathrm{~d}}$ S. Ahmed, ${ }^{14}$ M. Albrecht, ${ }^{4}$ M. Alekseev, ${ }^{55 \mathrm{a}, 55 \mathrm{c}}$ A. Amoroso, ${ }^{55 \mathrm{a}, 55 \mathrm{c}}$ F. F. An, ${ }^{1}$ Q. An, ${ }_{5}^{52,42}$ J. Z. Bai, ${ }^{1}$ Y. Bai, ${ }^{41}$ O. Bakina, ${ }^{26}$ R. Baldini Ferroli, ${ }^{22 \mathrm{a}}$ Y. Ban, ${ }^{34}$ K. Begzsuren, ${ }^{24}$ D. W. Bennett, ${ }^{21}$ J. V. Bennett, ${ }^{5}$ N. Berger, ${ }^{25}$ M. Bertani, ${ }^{22 \mathrm{a}}$ D. Bettoni, ${ }^{23 \mathrm{a}}$ F. Bianchi, ${ }^{55 \mathrm{a}, 55 \mathrm{c}}$ E. Boger, ${ }^{26, \mathrm{~b}}$ I. Boyko, ${ }^{26}$ R. A. Briere, ${ }^{5}$ H. Cai, ${ }^{57}$ X. Cai, ${ }^{1,42}$
 H. S. Chen, ${ }^{1,46}$ J. C. Chen, ${ }^{1}$ M. L. Chen, ${ }^{1,42}$ P. L. Chen, ${ }^{53}$ S. J. Chen, ${ }^{32}$ X. R. Chen, ${ }^{29}$ Y. B. Chen, ${ }^{1,42}$ W. Cheng, ${ }^{55 \mathrm{c}}$ X. K. Chu, ${ }^{34}$ G. Cibinetto, ${ }^{23 \mathrm{a}}$ F. Cossio, ${ }^{55 \mathrm{c}}$ H. L. Dai, ${ }^{1,42}$ J. P. Dai, ${ }^{37, h}$ A. Dbeyssi, ${ }^{14}$ D. Dedovich, ${ }^{26}$ Z. Y. Deng, ${ }^{1}$ A. Denig, ${ }^{25}$ I. Denysenko, ${ }^{26}$ M. Destefanis, ${ }^{55 a, 55 c}$ F. De Mori, ${ }^{55 a, 55 c}$ Y. Ding, ${ }^{30}$ C. Dong, ${ }^{33}$ J. Dong, ${ }^{1,42}$ L. Y. Dong, ${ }^{1,46}$ M. Y. Dong, ${ }^{1,42,46}$ Z. L. Dou, ${ }^{32}$ S. X. Du, ${ }^{60}$ P. F. Duan, ${ }^{1}$ J. Fang, ${ }^{1,42}$ S. S. Fang, ${ }^{1,46}$ Y. Fang, ${ }^{1}$ R. Farinelli, ${ }^{23 a, 23 b}$ L. Fava, ${ }^{55 b, 55 c}$ S. Fegan, ${ }^{25}$ F. Feldbauer, ${ }^{4}$ G. Felici, ${ }^{22 a}$ C. Q. Feng, ${ }^{52,42}$ E. Fioravanti, ${ }^{23 a}$ M. Fritsch, ${ }^{4}$ C. D. Fu, ${ }^{1}$ Q. Gao, ${ }^{1}$ X. L. Gao, ${ }^{52,42}$ Y. Gao, ${ }^{44}$ Y. G. Gao, ${ }^{6}$ Z. Gao, ${ }^{52,42}$ B. Garillon, ${ }^{25}$ I. Garzia, ${ }^{23 a}$ A. Gilman, ${ }^{49}$ K. Goetzen, ${ }^{10}$ L. Gong, ${ }^{33}$ W. X. Gong, ${ }^{1,42}$ W. Gradl, ${ }^{25}$ M. Greco, ${ }^{55 a, 55 c}$ M. H. Gu, ${ }^{1,42}$ Y. T. Gu, ${ }^{12}$ A. Q. Guo, ${ }^{1}$ R. P. Guo, ${ }^{1,46}$ Y. P. Guo, ${ }^{25}$ A. Guskov, ${ }^{26}$ Z. Haddadi, ${ }^{28}$ S. Han, ${ }^{57}$ X. Q. Hao, ${ }^{15}$ F. A. Harris, ${ }^{47}$ K. L. He,${ }^{1,46}$ X. Q. He, ${ }^{51}$ F. H. Heinsius, ${ }^{4}$ T. Held, ${ }^{4}$ Y. K. Heng, ${ }^{1,42,46}$ T. Holtmann, ${ }^{4}$ Z. L. Hou, ${ }^{1}$ H. M. Hu, ${ }^{1,46}$ J. F. Hu, ${ }^{37, h}$ T. Hu, ${ }^{1,42,46}$ Y. Hu, ${ }^{1}$ G. S. Huang, ${ }^{52,42}$ J. S. Huang, ${ }^{15}$ X. T. Huang, ${ }^{36}$ X. Z. Huang, ${ }^{32}$ Z. L. Huang, ${ }^{30}$
T. Hussain, ${ }^{54}$ W. Ikegami Andersson, ${ }^{56}$ M. Irshad, ${ }^{52,42}$ Q. Ji, ${ }^{1}$ Q. P. Ji, ${ }^{15}$ X. B. Ji, ${ }^{1,46}$ X. L. Ji, ${ }^{1,42}$ X. S. Jiang, ${ }^{1,42,46}$ X. Y. Jiang, ${ }^{33}$ J. B. Jiao, ${ }^{36}$ Z. Jiao, ${ }^{17}$ D. P. Jin, ${ }^{1,42,46}$ S. Jin, ${ }^{1,46}$ Y. Jin, ${ }^{48}$ T. Johansson, ${ }^{56}$ A. Julin, ${ }^{49}$ N. Kalantar-Nayestanaki, ${ }^{28}$ X. S. Kang, ${ }^{33}$ M. Kavatsyuk, ${ }^{28}$ B. C. Ke, ${ }^{1}$ T. Khan, ${ }^{52,42}$ A. Khoukaz, ${ }^{50}$ P. Kiese, ${ }^{25}$ R. Kiuchi, ${ }^{1}$ R. Kliemt, ${ }^{10}$ L. Koch, ${ }^{27}$ O. B. Kolcu, ${ }^{45 b, f}$ B. Kopf, ${ }^{4}$ M. Kornicer, ${ }^{47}$ M. Kuemmel, ${ }^{4}$ M. Kuessner, ${ }^{4}$ A. Kupsc, ${ }^{56}$ M. Kurth, ${ }^{1}$ W. Kühn, ${ }^{27}$ J. S. Lange, ${ }^{27}$ M. Lara, ${ }^{21}$ P. Larin, ${ }^{14}$ L. Lavezzi, ${ }^{55 \mathrm{c}} \mathrm{H}$. Leithoff, ${ }^{25} \mathrm{C} . \operatorname{Li},{ }^{56}$ Cheng Li, ${ }^{52,42}$ D. M. Li, ${ }^{60}$ F. Li, ${ }^{1,42}{ }^{\text {F. Y. Li }}{ }^{34}$ G. Li $,{ }^{1} \mathrm{H} . \mathrm{B} . \mathrm{Li},{ }^{1,46}$ H. J. Li ${ }^{1,46}$ J. C. Li, ${ }^{1}$ J. W. Li, ${ }^{40}$ Jin Li, ${ }^{35}$ K. J. Li, ${ }^{43}$ Kang Li, ${ }^{13}{ }^{3}$ Ke Li, ${ }^{1}$ Lei Li, ${ }^{3}$ P. L. Li, ${ }^{52,42}$ P. R. Li, ${ }^{46,7}$ Q. Y. Li, ${ }^{36}$ W. D. Li, ${ }^{1,46}$ W. G. Li, ${ }^{1}$ X. L. Li, ${ }^{36}$ X. N. Li, ${ }^{1,42}$ X. Q. Li, ${ }^{33}$ Z. B. Li, ${ }^{43}$ H. Liang, ${ }^{52,42}$ Y. F. Liang, ${ }^{39}$ Y. T. Liang, ${ }^{27}$ G. R. Liao, ${ }^{11}$ L. Z. Liao, ${ }^{1,46}$ J. Libby, ${ }^{20}$ C. X. Lin, ${ }^{43}$ D. X. Lin, ${ }^{14}$ B. Liu, ${ }^{37, h}$ B. J. Liu, ${ }^{1}$ C. X. Liu, ${ }^{1}$ D. Liu, ${ }^{52,42}$ D. Y. Liu, ${ }^{37, h}$ F. H. Liu, ${ }^{38}$ Fang Liu, ${ }^{1}$ Feng Liu, ${ }^{6}$ H. B. Liu, ${ }^{12}$ H. L. Liu, ${ }^{41}$ H. M. Liu, ${ }^{1,46}$ Huanhuan Liu, Huihui Liu, ${ }^{16}$ J. B. Liu, ${ }^{52,42}$ J. Y. Liu, ${ }^{1,46}$ K. Liu, ${ }^{44}$ K. Y. Liu, ${ }^{30}$ Ke Liu, ${ }^{6}$ L. D. Liu, ${ }^{34}$ Q. Liu, ${ }^{46}$ S. B. Liu, ${ }^{52,42}$ X. Liu, ${ }^{29}$ Y. B. Liu, ${ }^{33}$ Z. A. Liu, ${ }^{1,42,46}$ Zhiqing Liu, ${ }^{25}$ Y. F. Long, ${ }^{34}$ X. C. Lou, ${ }^{1,42,46}$ H. J. Lu, ${ }^{17}$ J. G. Lu, ${ }^{1,42}$ Y. Lu, ${ }^{1}$ Y. P. Lu, ${ }^{1,42}$ C. L. Luo, ${ }^{31}$ M. X. Luo, ${ }^{59}$ X. L. Luo, ${ }^{1,42}$ S. Lusso, ${ }^{55 \mathrm{c}}$ X. R. Lyu, ${ }^{46}$ F. C. Ma, ${ }^{30}$ H. L. Ma, ${ }^{1}$ L. L. Ma, ${ }^{36}$ M. M. Ma, ${ }^{1,46}$ Q. M. Ma, ${ }^{1}$ T. Ma, ${ }^{1}$ X. N. Ma, ${ }^{33}$ X. Y. Ma,${ }^{1,42}$ Y. M. Ma, ${ }^{36}$ F. E. Maas, ${ }^{14}$ M. Maggiora, ${ }^{55 a, 55 c}$ Q. A. Malik, ${ }^{54}$ A. Mangoni, ${ }^{22 b}$ Y. J. Mao, ${ }^{34}$ Z. P. Mao, ${ }^{1}$ S. Marcello, ${ }^{55 a, 55 \mathrm{c}}$ Z. X. Meng, ${ }^{48}$ J. G. Messchendorp, ${ }^{28}$ G. Mezzadri, ${ }^{23 b}$ J. Min, ${ }^{1,42}$ R. E. Mitchell,,${ }^{21}$ X. H. Mo, ${ }^{1,42,46}$ Y. J. Mo, ${ }^{6}$ C. Morales Morales, ${ }^{14}$ N. Yu. Muchnoi, ${ }^{9, \mathrm{~d}}$ H. Muramatsu, ${ }^{49}$ A. Mustafa, ${ }^{4}$ Y. Nefedov, ${ }^{26}$ F. Nerling, ${ }^{10}$ I. B. Nikolaev, ${ }^{9, \mathrm{~d}}$ Z. Ning, ${ }^{1,42}$ S. Nisar, ${ }^{8}$ S. L. Niu, ${ }^{1,42}$ X. Y. Niu, ${ }^{1,46}$ S. L. Olsen, ${ }^{35, j}$ Q. Ouyang, ${ }^{1,42,46}$ S. Pacetti, ${ }^{22 b}$ Y. Pan, ${ }^{52,42}$ M. Papenbrock, ${ }^{56}$ P. Patteri, ${ }^{22 \mathrm{a}}$ M. Pelizaeus, ${ }^{4}$ J. Pellegrino, ${ }^{55 \mathrm{a}, 55 \mathrm{c}}{ }^{5}$ H. P. Peng, ${ }^{52,42}$ Z. Y. Peng, ${ }^{12}$ K. Peters, ${ }^{10, \mathrm{~g}}$ J. Pettersson, ${ }^{56}$ J. L. Ping, ${ }^{31}$ R. G. Ping, ${ }^{1,46}$ A. Pitka, ${ }^{4}$ R. Poling, ${ }^{49}$ V. Prasad, ${ }^{52,42}$ H. R. Qi, ${ }^{2}$ M. Qi, ${ }^{32}$ T. Y. Qi, ${ }^{2}$ S. Qian, ${ }^{1,42}$ C. F. Qiao, ${ }^{46}$ N. Qin, ${ }^{57}$ X. S. Qin, ${ }^{4}$ Z. H. Qin, ${ }^{1,42}$ J. F. Qiu, ${ }^{1}$ K. H. Rashid, ${ }^{54, i}$ C. F. Redmer, ${ }^{25}$ M. Richter, ${ }^{4}$ M. Ripka, ${ }^{25}$ A. Rivetti, ${ }^{55 c}$ M. Rolo, ${ }^{55 c}$ G. Rong, ${ }^{1,46}$ Ch. Rosner, ${ }^{14}$ A. Sarantsev, ${ }^{26, e}$ M. Savrié, ${ }^{23 b}$ C. Schnier, ${ }^{4}$ K. Schoenning, ${ }^{56}$ W. Shan, ${ }^{18}$ X. Y. Shan, ${ }^{52,42}$ M. Shao, ${ }^{52,42}$ C. P. Shen, ${ }^{2}$ P. X. Shen, ${ }^{33}$ X. Y. Shen, ${ }^{1,46}$ H. Y. Sheng, ${ }^{1}$ X. Shi, ${ }^{1,42}$ J. J. Song, ${ }^{36}$ W. M. Song, ${ }^{36}$
 Y. J. Sun, ${ }^{52,42}$ Y. K. Sun, ${ }^{52,42}$ Y. Z. Sun, ${ }^{1}$ Z. J. Sun, ${ }^{1,42}$ Z. T. Sun, ${ }^{21}$ Y. T. Tan, ${ }^{52,42}$ C. J. Tang, ${ }^{39}$ G. Y. Tang, ${ }^{1}$ X. Tang, ${ }^{1}$ I. Tapan, ${ }^{45 \mathrm{c}}{ }^{46}$. Tiemens, ${ }^{28}$ B. Tsednee, ${ }^{24}$ I. Uman, ${ }^{45 \mathrm{~d}}$ G. S. Varner, ${ }^{47}$ B. Wang, ${ }^{1}$ B. L. Wang, ${ }^{46}$ D. Wang, ${ }^{34}$ D. Y. Wang, ${ }^{34}$ Dan Wang, ${ }^{46}$ K. Wang, ${ }^{1,42}$ L. L. Wang, ${ }^{1}$ L. S. Wang, ${ }^{1}$ M. Wang, ${ }^{36}$ Meng Wang, ${ }^{1,46}$ P. Wang, ${ }^{1}$ P. L. Wang, ${ }^{1}$ W. P. Wang, ${ }^{52,42}$ X. F. Wang, ${ }^{44}$ Y. Wang, ${ }^{52,42}$ Y. F. Wang, ${ }^{1,42,46}$ Y. Q. Wang, ${ }^{25}$ Z. Wang, ${ }^{1,42}$ Z. G. Wang, ${ }^{1,42}$ Z. Y. Wang, Zongyuan Wang, ${ }^{1,46}$
T. Weber, ${ }^{4}$ D. H. Wei, ${ }^{11}$ P. Weidenkaff, ${ }^{25}$ S. P. Wen, ${ }^{1}$ U. Wiedner, ${ }^{4}$ M. Wolke, ${ }^{56}$ L. H. Wu, ${ }^{1}$ L. J. Wu, ${ }^{1,46}$ Z. Wu, ${ }^{1,42}$ L. Xia, ${ }^{52,42}$ Y. Xia, ${ }^{19}$ D. Xiao, ${ }^{1}$ Y. J. Xiao, ${ }^{1,46}$ Z. J. Xiao, ${ }^{31}$ Y. G. Xie, ${ }^{1,42}$ Y. H. Xie, ${ }^{6}$ X. A. Xiong, ${ }^{1,46}$ Q. L. Xiu, ${ }^{1,42}$ G. F. Xu, ${ }^{1}$ J. J. Xu, ${ }^{1,46}$ L. Xu, ${ }^{1}$ Q. J. Xu, ${ }^{13}$ Q. N. Xu, ${ }^{46}$ X. P. Xu, ${ }^{40}$ F. Yan, ${ }^{53}$ L. Yan, ${ }^{55 a, 55 c}$ W. B. Yan, ${ }^{52,42}$ W. C. Yan, ${ }^{2}$ Y. H. Yan, ${ }^{19}$ H. J. Yang, ${ }^{37, h}$ H. X. Yang, ${ }^{1}$ L. Yang, ${ }^{57}$ Y. H. Yang, ${ }^{32}$ Y. X. Yang, ${ }^{11}$ Yifan Yang, ${ }^{1,46}$ Z. Q. Yang, ${ }^{19}$ M. Ye, ${ }^{1,42}$ M. H. Ye, ${ }^{7}$ J. H. Yin, ${ }^{1}$ Z. Y. You, ${ }^{43}$ B. X. Yu, ${ }^{1,42,46}$ C. X. Yu, ${ }^{33}$ J. S. Yu, ${ }^{19}$ J. S. Yu, ${ }^{29}$ C. Z. Yuan, ${ }^{1,46}$ Y. Yuan, ${ }^{1}$ A. Yuncu, ${ }^{45 b, a}$
A. A. Zafar, ${ }^{54}$ Y. Zeng, ${ }^{19}$ Z. Zeng, ${ }^{52,42}$ B. X. Zhang, ${ }^{1}$ B. Y. Zhang, ${ }^{1,42}$ C. C. Zhang, ${ }^{1}$ D. H. Zhang, ${ }^{1}$ H. H. Zhang, ${ }^{43}$ H. Y. Zhang, ${ }^{1,42}$ J. Zhang, ${ }^{1,46}$ J. L. Zhang, ${ }^{58}$ J. Q. Zhang, ${ }^{4}$ J. W. Zhang, ${ }^{1,42,46}$ J. Y. Zhang, ${ }^{1}$ J. Z. Zhang, ${ }^{1,46}$ K. Zhang, ${ }^{1,46}$
L. Zhang, ${ }^{44}$ S.F. Zhang, ${ }^{32}$ T. J. Zhang, ${ }^{37, h}$ X. Y. Zhang, ${ }^{36}$ Y. Zhang, ${ }^{52,42}$ Y. H. Zhang, ${ }^{1,42}$ Y. T. Zhang, ${ }^{52,42}$ Yang Zhang, ${ }^{1}$ Yao Zhang, ${ }^{1}$ Yu Zhang, ${ }^{46}$ Z. H. Zhang, ${ }^{6}$ Z. P. Zhang, ${ }^{52}$ Z. Y. Zhang, ${ }^{57}$ G. Zhao, ${ }^{1}$ J. W. Zhao, ${ }^{1,42}$ J. Y. Zhao, ${ }^{1,46}$ J. Z. Zhao, ${ }^{1,42}$ Lei Zhao, ${ }^{52,42}$ Ling Zhao, ${ }^{1}$ M. G. Zhao, ${ }^{33}$ Q. Zhao, ${ }^{1}$ S. J. Zhao, ${ }^{60}$ T. C. Zhao, ${ }^{1}$ Y. B. Zhao, ${ }^{1,42}$ Z. G. Zhao, ${ }^{52,42}$ A. Zhemchugov, ${ }^{26, b}$ B. Zheng, ${ }^{53}$ J. P. Zheng, ${ }^{1,42}$ W. J. Zheng, ${ }^{36}$ Y. H. Zheng, ${ }^{46}$ B. Zhong, ${ }^{31}$ L. Zhou, ${ }^{1,42}$ Q. Zhou, ${ }^{1,46}$ X. Zhou, ${ }^{57}$ X. K. Zhou, ${ }^{52,42}$ X. R. Zhou, ${ }^{52,42}$ X. Y. Zhou, ${ }^{1}$ Xiaoyu Zhou, ${ }^{19}$ Xu Zhou, ${ }^{19}$ A. N. Zhu, ${ }^{1,46}$ J. Zhu, ${ }^{33}$ J. Zhu, ${ }^{43}$ K. Zhu, ${ }^{1}$ K. J. Zhu, ${ }^{1,42,46}$ S. Zhu, ${ }^{1}$ S. H. Zhu, ${ }^{51}$ X. L. Zhu, ${ }^{44}$ Y. C. Zhu, ${ }^{52,42}$ Y. S. Zhu, ${ }^{1,46}$ Z. A. Zhu, ${ }^{1,46}$ J. Zhuang, ${ }^{1,42}$ B. S. Zou, ${ }^{1}$ and J. H. Zou ${ }^{1}$

## (BESIII Collaboration)

${ }^{1}$ Institute of High Energy Physics, Beijing 100049, People's Republic of China<br>${ }^{2}$ Beihang University, Beijing 100191, People's Republic of China<br>${ }^{3}$ Beijing Institute of Petrochemical Technology, Beijing 102617, People's Republic of China<br>${ }^{4}$ Bochum Ruhr-University, D-44780 Bochum, Germany<br>${ }^{5}$ Carnegie Mellon University, Pittsburgh, Pennsylvania 15213, USA<br>${ }^{6}$ Central China Normal University, Wuhan 430079, People's Republic of China<br>${ }^{7}$ China Center of Advanced Science and Technology, Beijing 100190, People's Republic of China<br>${ }^{8}$ COMSATS Institute of Information Technology, Lahore, Defence Road, Off Raiwind Road, 54000 Lahore, Pakistan<br>${ }^{9}$ G.I. Budker Institute of Nuclear Physics SB RAS (BINP), Novosibirsk 630090, Russia<br>${ }^{10}$ GSI Helmholtzcentre for Heavy Ion Research GmbH, D-64291 Darmstadt, Germany<br>${ }^{11}$ Guangxi Normal University, Guilin 541004, People's Republic of China<br>${ }^{12}$ Guangxi University, Nanning 530004, People's Republic of China<br>${ }^{13}$ Hangzhou Normal University, Hangzhou 310036, People's Republic of China<br>${ }^{14}$ Helmholtz Institute Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany<br>${ }^{15}$ Henan Normal University, Xinxiang 453007, People's Republic of China<br>${ }^{16}$ Henan University of Science and Technology, Luoyang 471003, People's Republic of China<br>${ }^{17}$ Huangshan College, Huangshan 245000, People's Republic of China<br>${ }^{18}$ Hunan Normal University, Changsha 410081, People's Republic of China<br>${ }^{19}$ Hunan University, Changsha 410082, People's Republic of China<br>${ }^{20}$ Indian Institute of Technology Madras, Chennai 600036, India<br>${ }^{21}$ Indiana University, Bloomington, Indiana 47405, USA<br>${ }^{22}$ INFN Laboratori Nazionali di Frascati, I-00044 Frascati, Italy<br>${ }^{22 b}$ INFN and University of Perugia, I-06100 Perugia, Italy<br>${ }^{23 a}$ INFN Sezione di Ferrara, I-44122 Ferrara, Italy<br>${ }^{233}$ University of Ferrara, I-44122 Ferrara, Italy<br>${ }^{24}$ Institute of Physics and Technology, Peace Ave. 54B, Ulaanbaatar 13330, Mongolia<br>${ }^{25}$ Johannes Gutenberg University of Mainz, Johann-Joachim-Becher-Weg 45, D-55099 Mainz, Germany<br>${ }^{26}$ Joint Institute for Nuclear Research, 141980 Dubna, Moscow region, Russia<br>${ }^{27}$ Justus-Liebig-Universitaet Giessen, II. Physikalisches Institut, Heinrich-Buff-Ring 16, D-35392 Giessen, Germany<br>${ }^{28}$ KVI-CART, University of Groningen, NL-9747 AA Groningen, The Netherlands<br>${ }^{29}$ Lanzhou University, Lanzhou 730000, People's Republic of China<br>${ }^{30}$ Liaoning University, Shenyang 110036, People's Republic of China<br>${ }^{31}$ Nanjing Normal University, Nanjing 210023, People's Republic of China<br>${ }^{32}$ Nanjing University, Nanjing 210093, People's Republic of China<br>${ }^{33}$ Nankai University, Tianjin 300071, People's Republic of China<br>${ }^{34}$ Peking University, Beijing 100871, People's Republic of China<br>${ }^{35}$ Seoul National University, Seoul 151-747 Korea<br>${ }^{36}$ Shandong University, Jinan 250100, People's Republic of China<br>${ }^{37}$ Shanghai Jiao Tong University, Shanghai 200240, People's Republic of China<br>${ }^{38}$ Shanxi University, Taiyuan 030006, People's Republic of China<br>${ }^{39}$ Sichuan University, Chengdu 610064, People's Republic of China<br>${ }^{40}$ Soochow University, Suzhou 215006, People's Republic of China<br>${ }^{41}$ Southeast University, Nanjing 211100, People's Republic of China<br>${ }^{42}$ State Key Laboratory of Particle Detection and Electronics, Beijing 100049, Hefei 230026, People's Republic of China<br>${ }^{43}$ Sun Yat-Sen University, Guangzhou 510275, People's Republic of China<br>${ }^{44}$ Tsinghua University, Beijing 100084, People's Republic of China<br>${ }^{45 \mathrm{a}}$ Ankara University, 06100 Tandogan, Ankara, Turkey<br>${ }^{45 \mathrm{I}}$ Istanbul Bilgi University, 34060 Eyup, Istanbul, Turkey<br>${ }^{45 \mathrm{c}}$ Uludag University, 16059 Bursa, Turkey

${ }^{45 \mathrm{~d}}$ Near East University, Nicosia, North Cyprus, Mersin 10, Turkey<br>${ }^{46}$ University of Chinese Academy of Sciences, Beijing 100049, People's Republic of China<br>${ }^{47}$ University of Hawaii, Honolulu, Hawaii 96822, USA<br>${ }^{48}$ University of Jinan, Jinan 250022, People's Republic of China<br>${ }^{49}$ University of Minnesota, Minneapolis, Minnesota 55455, USA<br>${ }^{50}$ University of Muenster, Wilhelm-Klemm-Str. 9, 48149 Muenster, Germany<br>${ }^{51}$ University of Science and Technology Liaoning, Anshan 114051, People's Republic of China<br>${ }^{52}$ University of Science and Technology of China, Hefei 230026, People's Republic of China<br>${ }^{53}$ University of South China, Hengyang 421001, People's Republic of China<br>${ }^{54}$ University of the Punjab, Lahore-54590, Pakistan<br>${ }^{55 a}$ University of Turin, I-10125 Turin, Italy<br>${ }^{55 b}$ University of Eastern Piedmont, I-15121 Alessandria, Italy<br>${ }^{55 \mathrm{c}}$ INFN, I-10125 Turin, Italy<br>${ }^{56}$ Uppsala University, Box 516, SE-75120 Uppsala, Sweden<br>${ }^{57}$ Wuhan University, Wuhan 430072, People's Republic of China<br>${ }^{58}$ Xinyang Normal University, Xinyang 464000, People's Republic of China<br>${ }^{59}$ Zhejiang University, Hangzhou 310027, People's Republic of China<br>${ }^{60}$ Zhengzhou University, Zhengzhou 450001, People's Republic of China

(Received 7 October 2018; revised manuscript received 30 November 2018; published 10 January 2019)
Using $e^{+} e^{-}$annihilation data of $2.93 \mathrm{fb}^{-1}$ collected at center-of-mass energy $\sqrt{s}=3.773 \mathrm{GeV}$ with the BESIII detector, we measure the absolute branching fraction of $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ with significantly improved precision: $\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}}=\left(3.413 \pm 0.019_{\text {stat }} \pm 0.035_{\text {syst }}\right) \%$. Combining with our previous measurement of $\mathcal{B}_{D^{0} \rightarrow K^{-} e^{+} \nu_{e}}$, the ratio of the two branching fractions is determined to be $\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}} / \mathcal{B}_{D^{0} \rightarrow K^{-} e^{+} \nu_{e}}=$ $0.974 \pm 0.007_{\text {stat }} \pm 0.012_{\text {syst }}$, which agrees with the theoretical expectation of lepton flavor universality within the uncertainty. A study of the ratio of the two branching fractions in different four-momentum transfer regions is also performed, and no evidence for lepton flavor universality violation is found with current statistics. Taking inputs from global fit in the standard model and lattice quantum chromodynamics separately, we determine $f_{+}^{K}(0)=0.7327 \pm 0.0039_{\text {stat }} \pm 0.0030_{\text {syst }}$ and $\left|V_{c s}\right|=0.955 \pm 0.005_{\text {stat }} \pm 0.004_{\text {syst }} \pm 0.024_{\mathrm{LQCD}}$.

DOI: 10.1103/PhysRevLett.122.011804

In the standard model (SM), lepton flavor universality (LFU) requires equality of couplings between three families of leptons and gauge bosons. Semileptonic (SL) decays of pseudoscalar mesons, well understood in the SM, offer an excellent opportunity to test LFU and search for new physics effects. Recently, various LFU tests in SL $B$ decays were reported at $B A B A R$, Belle, and LHCb. The measured branching fraction (BF) ratios $\mathcal{R}_{D^{(*)}}^{\tau / \ell}=\mathcal{B}_{B \rightarrow \bar{D}^{(*)} \tau^{+} \nu_{\tau}} / \mathcal{B}_{B \rightarrow \bar{D}^{(+)} \ell^{+} \nu_{\ell}}$ $(\ell=\mu, e)$ [1-5] and $\mathcal{R}_{K^{(+)}}^{\mu \mu / e e}=\mathcal{B}_{B \rightarrow K^{(*)} \mu^{+} \mu^{-}} / \mathcal{B}_{B \rightarrow K^{(4)} e^{+} e^{-}}$ [6,7] deviate from SM predictions by $3.9 \sigma$ [8] and $2.1-2.5 \sigma$, respectively. Various models [9-14] were proposed to explain these tensions. Precision measurements of SL $D$ decays provide critical and complementary tests of LFU. Reference [15] states that observable LFU violations may exist in $D^{0} \rightarrow K^{-} \ell^{+} \nu_{\ell}$ decays. In the SM, Ref. [16] predicts

[^0]$\mathcal{R}_{\mu / e}=\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}} / \mathcal{B}_{D^{0} \rightarrow K^{-} e^{+} \nu_{e}}=0.975 \pm 0.001$. Above $q^{2}=0.1 \mathrm{GeV}^{2} / c^{4} \quad(q$ is the total four momentum of $\ell^{+} \nu_{\ell}$ ), one expects $\mathcal{R}_{\mu / e}$ close to 1 with negligible uncertainty [17]. This Letter presents an improved measurement of $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ [18], and LFU test with $D^{0} \rightarrow K^{-} \ell^{+} \nu_{\ell}$ decays in the full kinematic range and various separate $q^{2}$ intervals.

Moreover, experimental studies of the $D^{0} \rightarrow K^{-} \ell^{+} \nu_{\ell}$ dynamics help to determine the $c \rightarrow s$ quark mixing matrix element $\left|V_{c s}\right|$ and the hadronic form factors (FFs) $f_{ \pm}^{K}(0)$ [16,19,20]. The $D^{0} \rightarrow K^{-} e^{+} \nu_{e}$ dynamics was well studied by CLEO-c, Belle, BABAR, and BESIII [21-24]. However, the $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ dynamics was only investigated by Belle and FOCUS [21,25], with relatively poor precision. By analyzing the $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ dynamics, we determine $\left|V_{c s}\right|$ and $f_{+}^{K}(0)$ incorporating the inputs from global fit in the SM [26] and lattice quantum chromodynamics (LQCD) [27]. These are critical to test quark mixing matrix unitarity and validate LQCD calculations on FFs. This analysis is performed using $2.93 \mathrm{fb}^{-1}$ of data taken at center-of-mass energy $\sqrt{s}=3.773 \mathrm{GeV}$ with the BESIII detector.

Details about the design and performance of the BESIII detector are given in Ref. [28]. The Monte Carlo (MC) simulated events are generated with a GEANT4-based [29] detector simulation software package, BOOST. An inclusive MC sample, which includes the $D^{0} \bar{D}^{0}, D^{+} D^{-}$, and non$D \bar{D}$ decays of $\psi(3770)$, the initial state radiation (ISR) production of $\psi(3686)$ and $J / \psi$, and the $q \bar{q}(q=u, d, s)$ continuum process, along with Bhabha scattering, $\mu^{+} \mu^{-}$ and $\tau^{+} \tau^{-}$events, is produced at $\sqrt{s}=3.773 \mathrm{GeV}$ to determine the detection efficiencies and to estimate the potential backgrounds. The production of the charmonium states is simulated by the MC generator KKMC [30]. The measured decay modes of the charmonium states are generated using EVTGEN [31] with BFs from the Particle Data Group (PDG) [26], and the remaining unknown decay modes are generated by LundChARM [32]. The $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ decay is simulated with the modified pole model [33].

At $\sqrt{s}=3.773 \mathrm{GeV}$, the $\psi(3770)$ resonance decays predominately into $D^{0} \bar{D}^{0}$ or $D^{+} D^{-}$meson pairs. If a $\bar{D}^{0}$ meson is fully reconstructed by $\bar{D}^{0} \rightarrow K^{+} \pi^{-}, K^{+} \pi^{-} \pi^{0}$ or $K^{+} \pi^{-} \pi^{-} \pi^{+}$, a $D^{0}$ meson must exist in the recoiling system of the reconstructed $\bar{D}^{0}$ [called the single-tag (ST) $\bar{D}^{0}$ ]. In the presence of the ST $\bar{D}^{0}$, we select and study $D^{0} \rightarrow$ $K^{-} \mu^{+} \nu_{\mu}$ decay [called the double-tag (DT) events]. The BF of the SL decay is given by

$$
\begin{equation*}
\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}}=N_{\mathrm{DT}} /\left(N_{\mathrm{ST}}^{\mathrm{tot}} \times \varepsilon_{\mathrm{SL}}\right), \tag{1}
\end{equation*}
$$

where $N_{\mathrm{ST}}^{\text {tot }}$ and $N_{\mathrm{DT}}$ are the ST and DT yields, $\varepsilon_{\mathrm{SL}}=$ $\varepsilon_{\mathrm{DT}} / \varepsilon_{\mathrm{ST}}$ is the efficiency of reconstructing $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ in the presence of the $\operatorname{ST} \bar{D}^{0}$, and $\varepsilon_{\mathrm{ST}}$ and $\varepsilon_{\mathrm{DT}}$ are the efficiencies of selecting ST and DT events.

All charged tracks must originate from the interaction point with a distance of closest approach less than 1 cm in the transverse plane and less than 10 cm along the $z$ axis. Their polar angles $(\theta)$ are required to satisfy $|\cos \theta|<0.93$. Charged particle identification (PID) is performed by combining the time-of-flight information and the specific ionization energy loss measured in the main drift chamber. The information of the electromagnetic calorimeter (EMC) is also included to identify muon candidates. Combined confidence levels for electron, muon, pion and kaon hypotheses $\left(\mathrm{CL}_{e}, \mathrm{CL}_{\mu}, \mathrm{CL}_{\pi}\right.$, and $\left.\mathrm{CL}_{K}\right)$ are calculated individually. Kaon (pion) and muon candidates must satisfy $\mathrm{CL}_{K(\pi)}>\mathrm{CL}_{\pi(K)}$ and $\mathrm{CL}_{\mu}>0.001, \mathrm{CL}_{e}$, and $\mathrm{CL}_{K}$, respectively. In addition, the deposited energy in the EMC of the muon is required to be within $(0.02,0.29) \mathrm{GeV}$. The $\pi^{0}$ meson is reconstructed via $\pi^{0} \rightarrow \gamma \gamma$ decay. The energy deposited in the EMC of each photon is required to be greater than 0.025 GeV in the barrel $(|\cos \theta|<0.80)$ region or 0.050 GeV in the end cap $(0.86<|\cos \theta|<0.92)$ region, and the shower time has to be within 700 ns of the event start time. The $\pi^{0}$ candidates with both photons


FIG. 1. Fits to [(a)-(c)] the $M_{\text {BC }}$ distributions for the three ST modes, and (d) the $U_{\text {miss }}$ distribution for $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ candidates. Dots with error bars are data, solid curves show the fit results, dashed curves show the fitted non-peaking background shapes, the dash-dotted curve in (d) is the peaking background shape of $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ and the red arrows in (a)-(c) give the $M_{\mathrm{BC}}$ windows.
from the end cap are rejected because of poor resolution. The $\gamma \gamma$ combination with an invariant mass $\left(M_{\gamma \gamma}\right)$ in the range $(0.115,0.150) \mathrm{GeV} / c^{2}$ is regarded as a $\pi^{0}$ candidate, and a kinematic fit by constraining the $M_{\gamma \gamma}$ to the $\pi^{0}$ nominal mass [26] is performed to improve the mass resolution. For $\bar{D}^{0} \rightarrow K^{+} \pi^{-}$, the backgrounds from cosmic ray events, radiative Bhabha scattering and dimuon events are suppressed with the same requirements as used in Ref. [34].

The ST $\bar{D}^{0}$ mesons are identified by the energy difference $\Delta E \equiv E_{\bar{D}^{0}}-E_{\text {beam }}$ and the beam-constrained mass $M_{\mathrm{BC}} \equiv \sqrt{E_{\text {beam }}^{2}-\left|\vec{p}_{\bar{D}^{0}}\right|^{2}}$, where $E_{\text {beam }}$ is the beam energy, and $E_{\bar{D}^{0}}$ and $\vec{p}_{\bar{D}^{0}}$ are the total energy and momentum of the ST $\bar{D}^{0}$ in the $e^{+} e^{-}$rest frame. If there are multiple combinations in an event, the combination with the smallest $|\Delta E|$ is chosen for each tag mode and for $D^{0}$ and $\bar{D}^{0}$. For one event, there may be up to six ST $D$ candidates selected. To determine the ST yield, we fit the $M_{\mathrm{BC}}$ distributions of the accepted candidates after imposing mode dependent $\Delta E$ requirements. The signal is described by the MC-simulated shape convolved with a doubleGaussian function accounting for the resolution difference between data and MC simulation, and the background is modeled by an ARGUS function [35]. Fit results are shown in Figs. 1(a)-1(c). The corresponding $\Delta E$ and $M_{\mathrm{BC}}$ requirements, ST yields and efficiencies for various ST modes are summarized in Table I. The total ST yield is $N_{\mathrm{ST}}^{\mathrm{tot}}=$ $2341408 \pm 2056$.

Candidates for $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ must contain two oppositely charged tracks which are identified as a kaon and a muon, respectively. The muon must have the same charge as the kaon on the ST side. To suppress the peaking

TABLE I. $\Delta E$ and $M_{\mathrm{BC}}$ requirements, ST yields $N_{\mathrm{ST}}$, ST efficiencies $\varepsilon_{\mathrm{ST}}$ and signal efficiencies $\varepsilon_{\mathrm{SL}}$ for different ST modes. Uncertainties are statistical only.

| ST mode | $\Delta E(\mathrm{MeV})$ | $M_{\mathrm{BC}}\left(\mathrm{GeV} / c^{2}\right)$ | $N_{\mathrm{ST}}$ | $\varepsilon_{\mathrm{ST}}(\%)$ | $\varepsilon_{\mathrm{SL}}(\%)$ |
| :--- | :---: | :---: | ---: | :---: | :---: |
| $K^{+} \pi^{-}$ | $(-29,27)$ | $(1.858,1.874)$ | $538865 \pm 785$ | $65.37 \pm 0.09$ | $57.74 \pm 0.09$ |
| $K^{+} \pi^{-} \pi^{0}$ | $(-69,38)$ | $(1.858,1.874)$ | $1080050 \pm 1532$ | $34.67 \pm 0.04$ | $61.23 \pm 0.09$ |
| $K^{+} \pi^{-} \pi^{-} \pi^{+}$ | $(-31,28)$ | $(1.858,1.874)$ | $722493 \pm 1126$ | $38.20 \pm 0.06$ | $56.42 \pm 0.09$ |

backgrounds from $D^{0} \rightarrow K^{-} \pi^{+}\left(\pi^{0}\right)$, the $K^{-} \mu^{+}$invariant mass $\left(M_{K^{-} \mu^{+}}\right)$is required to be less than $1.56 \mathrm{GeV} / c^{2}$, and the maximum energy of any photon that is not used in the ST selection ( $E_{\text {extray }}^{\max }$ ) must be less than 0.25 GeV .

The kinematic quantity $U_{\text {miss }} \equiv E_{\text {miss }}-\left|\vec{p}_{\text {miss }}\right|$ is calculated for each event, where $E_{\text {miss }}$ and $\vec{p}_{\text {miss }}$ are the energy and momentum of the missing particle, which can be calculated by $E_{\text {miss }} \equiv E_{\text {beam }}-E_{K^{-}}-E_{\mu^{+}} \quad$ and $\quad \vec{p}_{\text {miss }} \equiv$ $\vec{p}_{D^{0}}-\vec{p}_{K^{-}}-\vec{p}_{\mu^{+}}$in the $e^{+} e^{-}$center-of-mass frame, where $E_{K^{-}\left(\mu^{+}\right)}$and $\vec{p}_{K^{-}\left(\mu^{+}\right)}$are the energy and momentum of the kaon (muon) candidates. To improve the $U_{\text {miss }}$ resolution, the $D^{0}$ energy is constrained to the beam energy and $\vec{p}_{D^{0}} \equiv-\hat{p}_{\bar{D}^{0}} \sqrt{E_{\text {beam }}^{2}-m_{\bar{D}^{0}}^{2}}$, where $\hat{p}_{\bar{D}^{0}}$ is the unit vector in the momentum direction of the ST $\bar{D}^{0}$ and $m_{\bar{D}^{0}}$ is the $\bar{D}^{0}$ nominal mass [26].

The SL decay yield is obtained from an unbinned fit to the $U_{\text {miss }}$ distribution of the accepted events of data, as shown in Fig. 1(d). In the fit, the signal, the peaking background of $D^{0} \rightarrow K^{-} \pi^{+} \pi^{0}$ decay and other backgrounds are described by the corresponding MC-simulated shapes. The former two are convolved with the same Gaussian function to account for the resolution difference between data and MC simulation. All parameters are left free. The fitted signal yield is $N_{\mathrm{DT}}=47100 \pm 259$.

The efficiencies of finding $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ for different ST modes are summarized in Table I. They are weighted by the ST yields and give the average efficiency $\varepsilon_{\text {SL }}=(58.93 \pm 0.07) \%$. To verify the reliability of the efficiency, typical distributions of the SL decay, e.g., momenta and $\cos \theta$ of $K^{-}$and $\mu^{+}$, are checked and good consistency between data and MC simulation has been found (see Fig. 1 of Ref. [36]).

By inserting $N_{\mathrm{DT}}, \varepsilon_{\mathrm{SL}}$ and $N_{\mathrm{ST}}^{\text {tot }}$ into Eq. (1), one obtains

$$
\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}}=\left(3.413 \pm 0.019_{\text {stat }} \pm 0.035_{\mathrm{syst}}\right) \%
$$

The systematic uncertainties in the BF measurement are described as follows. The uncertainty in $N_{\mathrm{ST}}^{\mathrm{tot}}$ is taken as $0.5 \%$ by examining the changes of the fitted yields by varying the fit range, the signal shape, and the endpoint of the ARGUS function. The efficiencies of muon and kaon tracking (PID) are studied with $e^{+} e^{-} \rightarrow \gamma \mu^{+} \mu^{-}$events and DT hadronic events, respectively. The uncertainties of tracking and PID efficiencies each are assigned as 0.3\% per kaon or muon. The differences of the momentum and
$\cos \theta$ distributions between $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ and the control samples have been considered. The uncertainty of the $E_{\text {extray }}^{\max }$ requirement is estimated to be $0.1 \%$ by analyzing the DT hadronic events. The uncertainty in the $M_{K^{-} \mu^{+}}$ requirement is estimated with the alternative $M_{K^{-} \mu^{+}}$ requirements of 1.51 or $1.61 \mathrm{GeV} / c^{2}$, and the larger change on the BF $0.4 \%$ is taken as the systematic uncertainty. The uncertainty of the $U_{\text {miss }}$ fit is estimated to be $0.5 \%$ by applying different fit ranges, and signal and background shapes. The uncertainty of the limited MC size is $0.1 \%$. The uncertainty in the MC model is estimated to be $0.1 \%$, which is the difference between our nominal DT efficiency and that determined by reweighting the $q^{2}$ distribution of the signal MC events to data with the obtained FF parameters (see below). The total uncertainty is $1.02 \%$, which is obtained by adding these uncertainties in quadrature.

The BFs of $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ and $\bar{D}^{0} \rightarrow K^{+} \mu^{-} \bar{\nu}_{\mu}$ are measured separately. The results are $\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}}=$ $\left(3.433 \pm 0.026_{\text {stat }} \pm 0.039_{\text {syst }}\right) \%$ and $\quad \mathcal{B}_{\bar{D}^{0} \rightarrow K^{+} \mu^{-} \bar{\nu}_{\mu}}=$ $\left(3.392 \pm 0.027_{\text {stat }} \pm 0.034_{\text {syst }}\right) \%$. The BF asymmetry is determined to be $\mathcal{A}=\left[\left(\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}}-\mathcal{B}_{\bar{D}^{0} \rightarrow K^{+} \mu^{-} \bar{\nu}_{\mu}}\right) /\right.$ $\left.\left(\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}}+\mathcal{B}_{\bar{D}^{0} \rightarrow K^{+} \mu^{-} \bar{\nu}_{\mu}}\right)\right]=\left(0.6 \pm 0.6_{\text {stat }} \pm 0.8_{\text {syst }}\right) \%$, and no asymmetry in the BFs of $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ and $\bar{D}^{0} \rightarrow$ $K^{+} \mu^{-} \bar{\nu}_{\mu}$ decays is found. All the systematic uncertainties except for those in the $E_{\text {extray }}^{\max }$ requirement and MC model are studied separately and are not canceled out in the BF asymmetry calculation.

The $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$ dynamics is studied by dividing the SL candidate events into various $q^{2}$ intervals. The measured partial decay rate (PDR) in the $i$ th $q^{2}$ interval, $\Delta \Gamma_{\mathrm{msr}}^{i}$, is determined by

$$
\begin{equation*}
\Delta \Gamma_{\mathrm{msr}}^{i} \equiv \int_{i}\left(d \Gamma / d q^{2}\right) d q^{2}=N_{\mathrm{pro}}^{i} /\left(\tau_{D^{0}} \times N_{\mathrm{ST}}^{\mathrm{tot}}\right) \tag{2}
\end{equation*}
$$

where $N_{\text {pro }}^{i}$ is the SL decay signal yield produced in the $i$ th $q^{2}$ interval, $\tau_{D^{0}}$ is the $D^{0}$ lifetime and $N_{\mathrm{ST}}^{\mathrm{tot}}$ is the ST yield. The signal yield produced in the $i$ th $q^{2}$ interval in data is calculated by

$$
\begin{equation*}
N_{\mathrm{pro}}^{i}=\sum_{j}^{N_{\text {intervals }}}\left(\varepsilon^{-1}\right)_{i j} N_{\mathrm{obs}}^{j} \tag{3}
\end{equation*}
$$



FIG. 2. (a) Fit to the PDRs, (b) projection to $f_{+}^{K}\left(q^{2}\right)$ for $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$, and (c) the measured $\mathcal{R}_{\mu / e}$ in each $q^{2}$ interval. Dots with error bars are data. Solid curves are the fit, the projection or the $\mathcal{R}_{\mu / e}$ expected with the parameters in Ref. [17] where the uncertainty is negligible due to strong correlations in hadronic FFs.
where the observed DT yield in the $j$ th $q^{2}$ interval $N_{\text {obs }}^{j}$ is obtained from the similar fit to the corresponding $U_{\text {miss }}$ distribution of data (see Fig. 2 of Ref. [36]). $\varepsilon$ is the efficiency matrix (Table I of Ref. [36]), which is obtained by analyzing the signal MC events and is given by
$\varepsilon_{i j}=\sum_{k}\left(1 / N_{\mathrm{ST}}^{\mathrm{tot}}\right) \times\left[\left(N_{\mathrm{rec}}^{i j} \times N_{\mathrm{ST}}\right) /\left(N_{\mathrm{gen}}^{j} \times \varepsilon_{\mathrm{ST}}\right)\right]_{k}$,
where $N_{\text {rec }}^{i j}$ is the DT yield generated in the $j$ th $q^{2}$ interval and reconstructed in the $i$ th $q^{2}$ interval, $N_{\text {gen }}^{j}$ is the total signal yield generated in the $j$ th $q^{2}$ interval, and the index $k$ denotes the $k$ th ST mode. The measured PDRs are shown in Fig. 2(a) and details can be found in Table II of Ref. [36].

The FF is parametrized as the series expansion parameterization [37] (SEP), which has been shown to be consistent with constraints from QCD [22,24,38]. The 2-parameter SEP is chosen and is given by

$$
\begin{align*}
f_{+}^{K}(t)= & \frac{1}{P(t) \Phi\left(t, t_{0}\right)} \frac{f_{+}^{K}(0) P(0) \Phi\left(0, t_{0}\right)}{1+r_{1}\left(t_{0}\right) z\left(0, t_{0}\right)} \\
& \times\left\{1+r_{1}\left(t_{0}\right)\left[z\left(t, t_{0}\right)\right]\right\} . \tag{5}
\end{align*}
$$

Here, $P(t)=z\left(t, m_{D_{s}^{*}}^{2}\right)$ and $\Phi$ is given by

$$
\begin{align*}
\Phi\left(t, t_{0}\right)= & \sqrt{\frac{1}{24 \pi \chi_{V}}}\left(\frac{t_{+}-t}{t_{+}-t_{0}}\right)^{1 / 4}\left(\sqrt{t_{+}-t}+\sqrt{t_{+}}\right)^{-5} \\
& \times\left(\sqrt{t_{+}-t}+\sqrt{t_{+}-t_{0}}\right)\left(\sqrt{t_{+}-t}+\sqrt{t_{+}-t_{-}}\right)^{3 / 2} \\
& \times\left(t_{+}-t\right)^{3 / 4}, \tag{6}
\end{align*}
$$

where $z\left(t, t_{0}\right)=\left[\left(\sqrt{t_{+}-t}-\sqrt{t_{+}-t_{0}}\right) /\left(\sqrt{t_{+}-t}+\sqrt{t_{+}-t_{0}}\right)\right]$, $t_{ \pm}=\left(m_{D} \pm m_{K}\right)^{2}, t_{0}=t_{+}\left(1-\sqrt{1-t_{-} / t_{+}}\right), m_{D}$ and $m_{K}$ are the masses of $D$ and $K$ particles, $m_{D_{s}^{t}}$ is the pole mass of the vector FF accounting for the strong interaction between $D$ and $K$ mesons and usually taken as the mass of the lowest lying $c \bar{s}$ vector meson $D_{s}^{*}$ [26], and $\chi_{V}$ can be obtained from dispersion relations using perturbative QCD [39].

The PDRs are fitted by assuming the ratio $f_{+}^{K}\left(q^{2}\right) / f_{-}^{K}\left(q^{2}\right)$ to be independent of $q^{2}$, and minimizing the $\chi^{2}$ constructed as

$$
\begin{equation*}
\chi^{2}=\sum_{i, j=1}^{N_{\text {ineverals }}}\left(\Delta \Gamma_{\mathrm{msr}}^{i}-\Delta \Gamma_{\text {exp }}^{i}\right) C_{i j}^{-1}\left(\Delta \Gamma_{\mathrm{msr}}^{j}-\Delta \Gamma_{\text {exp }}^{j}\right), \tag{7}
\end{equation*}
$$

where $\Delta \Gamma_{\text {exp }}^{i}$ is the expected PDR in the $i$ th $q^{2}$ interval given by $[40,41]$

$$
\begin{align*}
\Delta \Gamma_{\text {exp }}^{i}= & \int_{i} \frac{G_{F}^{2}\left|V_{c s}\right|^{2}}{8 \pi^{3} m_{D}}\left|\vec{p}_{K}\right|\left|f_{+}^{K}\left(q^{2}\right)\right|^{2}\left(\frac{W_{0}-E_{K}}{F_{0}}\right)^{2} \\
& \times\left\{\frac{1}{3} m_{D}\left|\vec{p}_{K}\right|^{2}+\frac{m_{\ell}^{2}}{8 m_{D}}\left(m_{D}^{2}+m_{K}^{2}+2 m_{D} E_{K}\right)\right. \\
& +\frac{1}{3} m_{\ell}^{2} \frac{\left|\vec{p}_{K}\right|^{2}}{F_{0}}+\frac{1}{4} m_{\ell}^{2} \frac{m_{D}^{2}-m_{K}^{2}}{m_{D}} \operatorname{Re}\left[\frac{f_{-}^{K}\left(q^{2}\right)}{f_{+}^{K}\left(q^{2}\right)}\right] \\
& \left.+\frac{1}{4} m_{\ell}^{2} F_{0}\left|\frac{f_{-}^{K}\left(q^{2}\right)}{f_{+}^{K}\left(q^{2}\right)}\right|^{2}\right\} d q^{2}, \tag{8}
\end{align*}
$$

and $C_{i j}=C_{i j}^{\text {stat }}+C_{i j}^{\text {syst }}$ is the covariance matrix of the measured PDRs among $q^{2}$ intervals. In Eq. (8), $G_{F}$ is the Fermi coupling constant, $m_{\ell}$ is the mass of the lepton, $\left|\vec{p}_{K}\right|$ and $E_{K}$ are the momentum and energy of the kaon in the $D$ rest frame, $W_{0}=\left(m_{D}^{2}+m_{K}^{2}-m_{\ell}^{2}\right) /\left(2 m_{D}\right)$ is the maximum energy of the kaon in the $D$ rest frame, and $F_{0}=W_{0}-E_{K}+m_{\ell}^{2} /\left(2 m_{D}\right)=q^{2} /\left(2 m_{D}\right)$. The statistical covariance matrix (Table III of Ref. [36]) is constructed as

$$
\begin{equation*}
C_{i j}^{\mathrm{stat}}=\left(\frac{1}{\tau_{D^{0}} N_{\mathrm{ST}}^{\mathrm{tot}}}\right)^{2} \sum_{\alpha} \varepsilon_{i \alpha}^{-1} \varepsilon_{j \alpha}^{-1}\left[\sigma\left(N_{\mathrm{obs}}^{\alpha}\right)\right]^{2} . \tag{9}
\end{equation*}
$$

The systematic covariance matrix (Table IV of Ref. [36]) is obtained by summing all the covariance matrices for each source of systematic uncertainty. In general, it has the form

$$
\begin{equation*}
C_{i j}^{\text {syst }}=\delta\left(\Delta \Gamma_{\mathrm{msI}}^{i}\right) \delta\left(\Delta \Gamma_{\mathrm{msr}}^{j}\right), \tag{10}
\end{equation*}
$$

where $\delta\left(\Delta \Gamma_{\mathrm{msr}}^{i}\right)$ is the systematic uncertainty of the PDR in the $i$ th $q^{2}$ interval. The systematic uncertainties in $N_{\mathrm{ST}}^{\text {tot }}, \tau_{D^{0}}$
and $E_{\text {extray }}^{\max }$ requirement are considered to be fully correlated across $q^{2}$ intervals while others are studied separately in each $q^{2}$ interval with the same method used in the BF measurement.

Figures 2(a) and 2(b) show the fit to the PDRs of $D^{0} \rightarrow$ $K^{-} \mu^{+} \nu_{\mu}$ and the projection to $f_{+}^{K}\left(q^{2}\right)$. The goodness of fit is $\chi^{2} / \mathrm{NDOF}=15.0 / 15$, where NDOF is the number of degrees of freedom. From the fit, we obtain the product of $f_{+}^{K}(0)\left|V_{c s}\right|=0.7133 \pm 0.0038_{\text {stat }} \pm 0.0030_{\text {syst }}$, the first order coefficient $r_{1}=-1.90 \pm 0.21_{\text {stat }} \pm 0.07_{\text {syst }}$, and the FF ratio $f_{-}^{K} / f_{+}^{K}=-0.6 \pm 0.8_{\text {stat }} \pm 0.2_{\text {syst. }}$. The nominal fit parameters are taken from the results obtained by fitting with the combined statistical and systematic covariance matrix, and the statistical uncertainties of the fit parameters are taken from the fit with only the statistical covariance matrix. For each parameter, the systematic uncertainty is obtained by calculating the quadratic difference of uncertainties between these two fits.

Combining $\mathcal{B}_{D^{0} \rightarrow K^{-} \mu^{+} \nu_{\Lambda}}$ with our previous measurement $\mathcal{B}_{D^{0} \rightarrow K^{-} e^{+} \nu_{e}}=\left(3.505 \pm 0.014_{\text {stat }} \pm 0.033_{\text {syst }}\right) \%$ [24] gives $\mathcal{R}_{\mu / e}=0.974 \pm 0.007_{\text {stat }} \pm 0.012_{\text {syst }}$, which agrees with the theoretical calculations with $\operatorname{LQCD}[16,17]$ and an SM quark model [42]. Additionally, we determine $\mathcal{R}_{\mu / e}$ in each $q^{2}$ interval, as shown in Fig. 2(c), where the error bars include both statistical and the uncanceled systematic uncertainties. In the $\mathcal{R}_{\mu / e}$ calculation, the uncertainties in $N_{\mathrm{ST}}^{\text {tot }}, \tau_{D^{0}}$ as well as the tracking and PID efficiencies of the kaon cancel. Below $q^{2}=0.1 \mathrm{GeV}^{2} / c^{4}, \mathcal{R}_{\mu / e}$ is significantly lower than 1 due to smaller phase space for $D^{0} \rightarrow$ $K^{-} \mu^{+} \nu_{\mu}$ with nonzero muon mass that cannot be neglected. Above $0.1 \mathrm{GeV}^{2} / c^{4}, \mathcal{R}_{\mu / e}$ is close to 1 . They are consistent with the SM prediction, and no deviation larger than $2 \sigma$ is observed.

In summary, by analyzing $2.93 \mathrm{fb}^{-1}$ of data collected at $\sqrt{s}=3.773 \mathrm{GeV}$ with the BESIII detector, we present an improved measurement of the absolute BF of the SL decay $D^{0} \rightarrow K^{-} \mu^{+} \nu_{\mu}$. Our result is consistent with the PDG value [26] and improves its precision by a factor of three. Combining the previous BESIII measurements of $D^{0} \rightarrow K^{-} e^{+} \nu_{e}$, we calculate $\mathcal{R}_{\mu / e}$ ratios in the full $q^{2}$ range and various $q^{2}$ intervals. No significant evidence of LFU violation is found with current statistics and systematic uncertainties. By fitting the PDRs of this decay, we obtain $f_{+}^{K}(0)\left|V_{c s}\right|=0.7133 \pm 0.0038_{\text {stat }} \pm 0.0029_{\text {syst }}$. Using $\left|V_{c s}\right|$ given by global fit in the SM [26] yields $f_{+}^{K}(0)=$ $0.7327 \pm 0.0039_{\text {stat }} \pm 0.0030_{\text {syst }}$, while using the $f_{+}^{K}(0)$ calculated in LQCD [27] results in $\left|V_{c s}\right|=0.955 \pm$ $0.005_{\text {stat }} \pm 0.004_{\text {syst }} \pm 0.024_{\text {LQCD }}$. These results are consistent with our measurements using $D^{0(+)} \rightarrow \bar{K} e^{+} \nu_{e}$ [24,43,44] and $D_{s}^{+} \rightarrow \mu^{+} \nu_{\mu}$ [45] within uncertainties and are important to test the LQCD calculation of $f_{+}^{K}(0)$ $[17,27,46]$ and quark mixing matrix unitarity with better accuracy.

The BESIII collaboration thanks the staff of BEPCII and the IHEP computing center for their strong support. This work is supported in part by National Key Basic Research Program of China under Contract No. 2015CB856700; National Natural Science Foundation of China (NSFC) under Contracts No. 11305180, No. 11775230, No. 11235011, No. 11335008, No. 11425524, No. 11625523, and No. 11635010; the Chinese Academy of Sciences (CAS) Large-Scale Scientific Facility Program; the CAS Center for Excellence in Particle Physics (CCEPP); Joint Large-Scale Scientific Facility Funds of the NSFC and CAS under Contracts No. U1632109, No. U1332201, No. U1532257, and No. U1532258; CAS under Contracts No. KJCX2-YWN29, No. KJCX2-YW-N45, and No. QYZDJ-SSWSLH003; 100 Talents Program of CAS; National 1000 Talents Program of China; INPAC and Shanghai Key Laboratory for Particle Physics and Cosmology; German Research Foundation DFG under Contracts No. Collaborative Research Center CRC 1044, No. FOR 2359; Instituto Nazionale di Fisica Nucleare, Italy; Koninklijke Nederlandse Akademie van Wetenschappen (KNAW) under Contract No. 530-4CDP03; Ministry of Development of Turkey under Contract No. DPT2006K120470; National Science and Technology fund; The Swedish Research Council; U.S. Department of Energy under Contracts No. DE-FG02-05ER41374, No. DE-SC0010118, No. DE-SC-0010504, and No. DE-SC-0012069; University of Groningen (RuG) and the Helmholtzzentrum fuer Schwerionenforschung GmbH (GSI), Darmstadt; WCU Program of National Research Foundation of Korea under Contract No. R32-2008-000-10155-0.

[^1][2] J. P. Lees et al. (BABAR Collaboration), Phys. Rev. D 88, 072012 (2013).
[3] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 115, 111803 (2015).
[4] M. Huschle et al. (Belle Collaboration), Phys. Rev. D 92, 072014 (2015).
[5] Y. Sato et al. (Belle Collaboration), Phys. Rev. D 94, 072007 (2016).
[6] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 113, 151601 (2014).
[7] R. Aaij et al. (LHCb Collaboration), J. High Energy Phys. 08 (2017) 055.
[8] Y. Amhis et al. (HFLAV Collaboration), Eur. Phys. J. C 77, 895 (2017).
[9] S. Fajfer, J. F. Kamenik, and I. Nisandzic, Phys. Rev. D 85, 094025 (2012).
[10] S. Fajfer, J. F. Kamenik, I. Nisandzic, and J. Zupan, Phys. Rev. Lett. 109, 161801 (2012).
[11] A. Celis, M. Jung, X.-Q. Li, and A. Pich, J. High Energy Phys. 01 (2013) 054.
[12] A. Crivellin, G. D'Ambrosio, and J. Heeck, Phys. Rev. Lett. 114, 151801 (2015).
[13] A. Crivellin, J. Heeck, and P. Stoffer, Phys. Rev. Lett. 116, 081801 (2016).
[14] M. Bauer and M. Neubert, Phys. Rev. Lett. 116, 141802 (2016).
[15] S. Fajfer, I. Nisandzic, and U. Rojec, Phys. Rev. D 91, 094009 (2015).
[16] L. Riggio, G. Salerno, and S. Simula, Eur. Phys. J. C 78, 501 (2018).
[17] V. Lubicz, L. Riggio, G. Salerno, S. Simula, and C. Tarantino (ETM Collaboration), Phys. Rev. D 96, 054514 (2017).
[18] Throughout this Letter, the charge conjugate channels are implied unless otherwise stated.
[19] J. Zhang, C. X. Yue, and C. H. Li, Eur. Phys. J. C 78, 695 (2018).
[20] Y. Fang, G. Rong, H. L. Ma, and J. Y. Zhao, Eur. Phys. J. C 75, 10 (2015).
[21] L. Widhalm et al. (Belle Collaboration), Phys. Rev. Lett. 97, 061804 (2006).
[22] D. Besson et al. (CLEO Collaboration), Phys. Rev. D 80, 032005 (2009).
[23] B. Aubert et al. (BABAR Collaboration), Phys. Rev. D 76, 052005 (2007).
[24] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 92, 072012 (2015).
[25] J. M. Link et al. (FOCUS Collaboration), Phys. Lett. B 607, 233 (2005).
[26] M. Tanabashi et al. (Particle Data Group), Phys. Rev. D 98, 030001 (2018).
[27] H. Na, C. T. H. Davies, E. Follana, G. P. Lepage, and J. Shigemitsu (HPQCD Collaboration), Phys. Rev. D 82, 114506 (2010).
[28] M. Ablikim et al. (BESIII Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 614, 345 (2010).
[29] S. Agostinelli et al. (GEANT4 Collaboration), Nucl. Instrum. Methods Phys. Res., Sect. A 506, 250 (2003).
[30] S. Jadach, B. F. L. Ward, and Z. Was, Comput. Phys. Commun. 130, 260 (2000); Phys. Rev. D 63, 113009 (2001).
[31] D. J. Lange, Nucl. Instrum. Methods Phys. Res., Sect. A 462, 152 (2001); R. G. Ping, Chin. Phys. C 32, 599 (2008).
[32] J. C. Chen, G. S. Huang, X. R. Qi, D. H. Zhang, and Y. S. Zhu, Phys. Rev. D 62, 034003 (2000).
[33] D. Becirevic and A. B. Kaidalov, Phys. Lett. B 478, 417 (2000).
[34] M. Ablikim et al. (BESIII Collaboration), Phys. Lett. B 734, 227 (2014).
[35] H. Albrecht et al. (ARGUS Collaboration), Phys. Lett. B 241, 278 (1990).
[36] See Supplemental Material at http://link.aps.org/ supplemental/10.1103/PhysRevLett.122.011804 for the comparisons of some typical distributions between data and MC simulation, efficiency matrix, fits to $U_{\text {miss }}$ distributions in $18 q^{2}$ intervals, PDR and $\mathcal{R}_{\mu / e}$ in each $q^{2}$ interval, and statistical and systematic covariance matrices.
[37] T. Becher and R. J. Hill, Phys. Lett. B 633, 61 (2006).
[38] J. P. Lees et al. (BABAR Collaboration), Phys. Rev. D 91, 052022 (2015).
[39] C. G. Boyd, B. Grinstein, and R.F. Lebed, Nucl. Phys. B461, 493 (1996).
[40] J. M. Link et al. (FOCUS Collaboration), Phys. Lett. B 607, 233 (2005).
[41] J. G. Korner and G. A. Schuler, Z. Phys. C 46, 93 (1990).
[42] N. R. Soni and J. N. Pandya, Phys. Rev. D 96, 016017 (2017).
[43] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 96, 012002 (2017).
[44] M. Ablikim et al. (BESIII Collaboration), Phys. Rev. D 92, 112008 (2015).
[45] M. Ablikim et al. (BESIII Collaboration), arXiv:1811.10890.
[46] C. Aubin et al. (Fermilab Lattice and MILC and HPQCD Collaborations), Phys. Rev. Lett. 94, 011601 (2005).


[^0]:    Published by the American Physical Society under the terms of the Creative Commons Attribution 4.0 International license. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. Funded by SCOAP ${ }^{3}$.

[^1]:    ${ }^{\text {a }}$ Also at Bogazici University, 34342 Istanbul, Turkey.
    ${ }^{\mathrm{b}}$ Also at the Moscow Institute of Physics and Technology, Moscow 141700, Russia.
    ${ }^{\text {c }}$ Also at the Functional Electronics Laboratory, Tomsk State University, Tomsk 634050, Russia.
    ${ }^{\mathrm{d}}$ Also at the Novosibirsk State University, Novosibirsk 630090, Russia.
    ${ }^{\text {e}}$ Also at the NRC "Kurchatov Institute," PNPI, Gatchina 188300, Russia.
    ${ }^{\mathrm{f}}$ Also at Istanbul Arel University, 34295 Istanbul, Turkey.
    ${ }^{\text {g }}$ Also at Goethe University Frankfurt, 60323 Frankfurt am Main, Germany.
    ${ }^{\text {h }}$ Also at Key Laboratory for Particle Physics, Astrophysics and Cosmology, Ministry of Education; Shanghai Key Laboratory for Particle Physics and Cosmology; Institute of Nuclear and Particle Physics, Shanghai 200240, People's Republic of China.
    'Government College Women University, Sialkot 51310, Punjab, Pakistan.
    ${ }^{\mathrm{j}}$ Center for Underground Physics, Institute for Basic Science, Daejeon 34126, Korea.
    [1] J. P. Lees et al. (BABAR Collaboration), Phys. Rev. Lett. 109, 101802 (2012).

