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Coupling Solid-State NMR with GIPAW ab-initio Calculations in Metal Hydrides and Borohydrides

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Abstract

An integrated experimental-theoretical approach for the solid-state NMR investigation of a series of hydrogen-storage materials is illustrated. Seven experimental room-temperature structures of Group I and II metal hydrides and borohydrides, namely NaH, LiH, NaBH₄, MgH₂, CaH₂, Ca(BH₄)₂ and LiBH₄, were computationally optimized. Periodic lattice calculations were performed by means of the plane-wave method, adopting the DFT Generalized Gradient Approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE) functional, as implemented in the Quantum Espresso package. Projector Augmented Wave (PAW), including the Gauge-Including Projected Augmented-Wave (GIPAW) method for solid-state NMR calculations were used, adopting both Rappe-Rabe-Kaxiras-Joannopoulos (RRKJ) ultrasoft pseudopotentials and new developed pseudopotentials. Computed GIPAW chemical shifts were critically compared with the experimental ones. A good agreement between experimental and computed multinuclear chemical shifts was obtained.

Introduction

Nowadays, the main approaches for internal combustion engine replacement are based on new lithium battery technology and fuel-cell technology, mainly developed around hydrogen-based systems.¹ In fact, hydrogen may be an efficient and non-polluting energy carrier, ideal for clean energy transport and storage.² However, the most challenging bottleneck for a widespread use of hydrogen is the development of safe and efficient storage systems, particularly for mobile applications.³ Among methods for hydrogen-storage,^{4,5} high-pressured gas or cryogenic liquid cannot fulfil safety and efficiency requirements. On the other hand, solid-state hydrogen storage holds great hopes to provide safe and efficient on-board hydrogen delivery.⁶ An intensive research is recently taking place on light metal hydrides⁷⁻¹¹ in order to improve thermodynamic and kinetic properties of hydrogen sorption.¹² Multinuclear solid-state NMR (SSNMR) is a well established technique providing sophisticated qualitative and quantitative information at local level, such as electron shielding around atom nuclei, presence of different environments and molecular mobility.¹³ First principle periodic calculations on condensed matter give a way to interpret and

to predict the behaviour of new materials. The combination of these two techniques could give new insights in the field of hydrogen storage materials.

While the chemical shift calculations in solution or in the gas phase are currently considered somewhat routine, even for transition metal complexes (e.g. Refs.¹⁴⁻¹⁸), *ab initio* calculations of NMR properties in the solid state are less developed. A first attempt to compute the magnetic shielding in molecules was performed by using localized atom-centred basis sets, based on the Molecular Orbital Theory.¹⁹ This approach, however, has soon revealed to be quite limited in the description of solid systems and computationally highly demanding. A reduction of the computational cost for the calculations was obtained introducing the pseudopotential formalism.²⁰ This idea arose from the evidence that the core contribution to the magnetic shielding can be considered approximately as a constant, independently on chemical environments.²¹ Nevertheless, calculation of NMR parameters critically depends on the details of the all-electron wavefunctions in the region close to the nucleus, where pseudo-wavefunctions take an unphysical smooth behaviour. For this reason, a significant improvement of the results has been achieved in 2001, when Pickard and Mauri²² extended the Projector Augmented Wave (PAW)²³ approach to the *ab initio* determination of the NMR parameters, allowing the reconstruction of the all-electron wavefunctions in the core region. This approach was called *Gauge-Including Projected Augmented-Wave* (GIPAW) and it has been recently implemented for ultrasoft pseudopotential scheme.²⁴

First principle calculations on metal hydrides and borohydrides²⁵ have been widely reported in recent years, e.g. LiH,^{26,27} NaBH₄,²⁸⁻³² MgH₂,^{33,34} CaH₂,^{35,36} Ca(BH₄)₂³⁷⁻³⁹ and LiBH₄.^{32,40-44} However, to our knowledge, no first principle calculations of NMR chemical shifts with the GIPAW method have been performed up to now for these compounds. So, this work is mainly focused on the computation of the NMR parameters by means of the GIPAW method in light metal hydrides and borohydrides, aiming to check the reliability of the approach for modelling of NMR spectra. The results will be of interest for the interpretation of experimental data based on unknown intermediates during hydrogen sorption reactions.^{45,46}

Experimental and Computational Methods

All the measurements were performed using commercial samples. Compounds of 95% purity were purchased from Alfa-Aesar or Sigma-Aldrich and used as received. Ca(BH₄)₂ purchased from Sigma-Aldrich was a mixture of α and β phases. For sake of comparison, pure α -Ca(BH₄)₂ was also investigated. All samples were stored in a dry argon glove-box and loaded into NMR rotors while inside the glove-box. Solid-state NMR measurements were run on a Bruker Advance II 400 instrument operating at 400.23, 128.41 and 105.87 MHz for ¹H, ¹¹B and ²³Na, respectively. ¹¹B and ²³Na spectra were recorded at room temperature at the spinning speed of 14 kHz. Cylindrical 4 mm o.d. zirconia rotors with sample volume of 80 µL were employed. The single pulse excitation (SPE) or the DEPTH (for suppressing the probe background signal) sequences were used with a 90° pulse of 3.75 (¹¹B) and 2.7 µs (²³Na), recycle delays of 30-140 (¹¹B) or 1-20 s

(²³Na), and about 16 transients. ¹¹B spectra of LiBH₄ and Ca(BH₄)₂ (either α and β phases) were acquired using the Hahn-echo pulse sequence $(\pi/2)_{x}$ - τ_{1} - $(\pi)_{y}$ - τ_{2} -acq, where τ represents interpulse delays of 138 µs. ¹H MAS spectra were acquired in a 2.5 mm probe with a spinning speed of 32 kHz using the DEPTH sequence for suppressing the probe background signal. A 90° pulse of 1.8 µs, recycle delays of 1-60 s, and 16 transients were used. The ¹H, and ¹¹B and ²³Na chemical shift scales were calibrated using adamantane (¹H signal at 1.87 ppm vs. TMS), and NaBH₄ (¹¹B signal at -42.0 ppm with respect to BF₃·Et₂O⁴⁷ and ²³Na signal at -15.85 ppm with respect to NaCl⁴⁸) as external standards, respectively. Experimental ⁶Li data were not performed by us, but they were taken from the literature⁴⁹ and were referred vs LiH.

Periodic lattice calculations were performed by means of Quantum Espresso version 4.3.2.⁵⁰ The Generalized Gradient Approximation (GGA) with the Perdew–Burke–Ernzerhof (PBE) functional⁵¹ was used in all calculations. For geometry optimizations, experimental data at room temperature for NaH,⁵² LiH,⁵³ NaBH₄, ⁵⁴ MgH₂, ³³ CaH₂, ⁵⁵ Ca(BH₄)₂ ^{38,56} and LiBH₄ ⁵⁷ were considered as starting structures. Calculations were performed with the variable-cell scheme, adopting the Rappe-Rabe-Kaxiras-Joannopoulos (RRKJ)⁵⁸ ultrasoft pseudopotentials (USPP) (for Li with s semicore state; for B and Mg with non-linear core correction; for Na and Ca with s and p semicore states and non-linear core correction) available at the Quantum Espresso web site⁵⁹ (indicated as QE PP below), and the Projector Augmented Wave (PAW)²³ pseudopotentials (PP) generated by the *atompaw* code⁶⁰⁻⁶² (version 3.0.1.8). We generated Troullier-Martins norm-conserving PAW PP for H and Ca, and USPP for the other atoms. For the PAW augmentation, two projectors in each angular momentum channel were used (except for H and Li). Vanderbilt's scheme was used to build the projectors and pseudo partial waves, whereas for sodium a RRKJ pseudization scheme was used. The generated PAW PP were also tested for transferability, checking the corresponding logarithmic derivatives. A cut-off of 60 Ry was used for structural optimization, since higher cut-off values (i.e. 200 and 120 Ry) did not affect significantly the results. The NMR chemical shifts were calculated using a 120 Ry energy cut-off by the generated PAW PP (previously used for geometry optimizations) and the available Ceresoli's PP 63, via the GIPAW method.²² A 60 Ry cut-off for NMR calculations gave unsatisfactory results, but values higher than 120 Ry did not significantly improved the quality of the data. The theoretical absolute magnetic shielding (σ) values were converted into chemical shifts (δ) relative to the absolute magnetic shielding of the reference substance NaBH₄, computed at the same level (absolute shielding σ = 145.25 and 146.49 ppm for B, σ = 588.84 and 578.22 ppm for Na, σ = 30.33 and 30.83 ppm for H, computed with PAW and Ceresoli's PP, respectively). For practical purposes the ¹H chemical shifts were reported against TMS (the experimental value of ¹H shift for NaBH₄ vs. TMS is –0.4 ppm), whereas the ¹¹B chemical shifts were reported against BF₃·Et₂O (the experimental ¹¹B shift value for NaBH₄ vs. BF₃·Et₂O is -42.00 ppm), in a similar way as previously described.¹⁴ As for ⁶Li nucleus in LiH, used as a reference, we adopted the absolute shielding σ = 88.83 and σ = 89.23 ppm, computed with PAW and Ceresoli's PP, respectively.

The Brillouin zones were automatically sampled with the Monkhorst–Pack scheme.⁶⁴ For each system we performed preliminary calculations: given a starting geometry and a fixed energy cutoff, the optimal number of k-points has been obtained by repeating simple SCF calculations with higher and higher grid mesh size until the total energy has converged within a threshold of 10^{-4} Ry (1.3605 $\cdot 10^{-3}$ eV). By this method, applied to all the investigated compounds, the final calculated cell and NMR parameters did not change significantly. We found that the optimal effective number of k-points is inversely proportional to the volume of the cell in the real space. Geometry optimization and NMR chemical shift calculations for NaH, LiH, NaBH₄, MgH₂, CaH₂, α -Ca(BH₄)₂, β -Ca(BH₄)₂ and LiBH₄ were performed with a grid mesh of $6\times6\times6$, $8\times8\times8$, $4\times4\times4$, $6\times6\times6$, $4\times7\times4$, $3\times2\times3$, $3\times3\times5$ and $3\times6\times4$, respectively.

Simulations of the NMR spectra were carried out using TopSpin (Bruker) taking into account the quadrupolar interaction and anisotropic chemical shifts under MAS conditions. The tensors describing the different anisotropic interactions were all oriented in the EFG principal axis frame (PAS). The quadrupolar interaction is defined by C_Q (MHz) and η_Q . The chemical shift anisotropy, following the Haeberlen Convention,⁶⁵ is characterized by δ_{iso} , the reduced anisotropy ($\delta = \delta_{zz} - \delta_{iso}$), the asymmetry parameter [$\eta_{CSA} = (\delta_{yy} - \delta_{xx})/\delta$; ($0 \le \eta \le +1$)] (with $|\delta_{zz} - \delta_{iso}| \ge |\delta_{xx} - \delta_{iso}| \ge |\delta_{yy} - \delta_{iso}|$) and the three Euler angles { α , β , γ }. Owing to the very small effects of the Euler angles on the spectra, they were not considered during the simulation. Thus, five independent parameters were used to characterize a single site. The simulation of the β -Ca(BH₄)₂ was performed on the commercial Ca(BH₄)₂ (purchased from Sigma-Aldrich) spectrum by using the values obtained from the simulation of the α form fixed and optimizing only the β site.

Results and Discussion

Geometry optimizations

Calculated lattice parameters and volumes for selected metal hydrides and borohydrides are reported in Table 1. The experimental cubic NaH, LiH and NaBH₄, tetragonal MgH₂, and orthorhombic CaH₂, LiBH₄ and α -Ca(BH₄)₂ structures at room temperature fit reasonably well with calculated geometries.

Table 1. Comparison between the	experimental and computed	l (by using PAW an	nd QE PP) structur	al lattice parameters
(Å) and volumes (Å ³).				

Comula	Space Group		Experir	nental			PA	W		QE a b c V 6.124 229.7 112.8 3.990 63.5 4.831 112.8 63.5 4512 63.5			
Sample	and Ref.	а	b	с	v	а	b	с	v	а	b	с	v
NaBH₄	F43m ⁵⁴	6.138			231.2	6.085			225.3	6.124			229.7
NaH	Fm-3m ⁵²	4.880			116.2	4.792			110.1	4.831			112.8
LiH	Fm-3m ⁵³	4.086			68.2	4.062			67.0	3.990			63.5
MgH₂	P4₂/mnm ³³	4.518		3.021	61.6	4.519		3.039	62.1	4.512		3.009	61.3
CaH₂	Pnma ⁵⁵	5.960	3.601	6.817	146.3	5.907	3.575	6.772	143.0	5.891	3.566	6.754	141.9
LiBH₄	Pnma ⁵⁷	7.179	4.437	6.803	216.7	7.448	4.398	6.598	216.1	7.419	4.382	6.522	212.0
α -Ca(BH ₄) ₂	Fddd ³⁸	8.778	13.129	7.489	863.1	8.754	13.127	7.481	859.6	8.754	13.154	7.493	862.9
u	F2dd ^{38,56}	8.776	13.023	7.413	847.3	8.748	13.118	7.485	858.9	8.752	13.154	7.496	862.9
β -Ca(BH ₄) ₂	P-4 ⁵⁶	6.919		4.347	208.1	6.893		4.362	207.2	6.951		4.354	210.4
	P42/m ³⁸	6.951		4.369	211.1	6.896		4.363	207.5	6.951		4.354	210.4

Under ambient conditions, NaH⁵², LiH⁵³ and NaBH₄⁵⁴ have similar NaCl-type structures, crystallizing in the *Fm-3m* (LiH and NaH) and *F43m* (NaBH₄) space groups. On the contrary, the unit cell of the α -structure of MgH₂, as derived from a synchrotron-radiation-based X-ray diffraction study³³, is tetragonal (rutile-type structure that crystallizes in the *P4₂/mnm* space group) and contains two formula-units of MgH₂, in which the hydrogen atoms are crystallographically equivalent. The variable-cell optimization of these crystal structures was performed using the generated PAW PP. The results obtained, shown in Table 1, revealed to be very close not only to the experimental ones, but also to the optimized structures achieved by using the available QE PP. In addition, the structural data for LiH, MgH₂ and NaBH₄ do not differ significantly from the results of DFT calculations already published in other papers. For example, Zhang et al.²⁶ and van Setten et al.⁶⁶ obtained fully optimized structures of LiH lattice parameters of 3.998 and 4.020 Å, respectively. As for NaBH₄, theoretically predicted cubic geometries with lattice parameters of 6.02³⁰, 6.05³¹ and 6.14²⁸ Å can be found in the literature. Finally, the PAW PP provided a very little overestimation of the cell volume of MgH₂ (around 0.8%) with respect to the experimental data, but a reasonable agreement appears by the comparison with other DFT-based calculations on MgH₂ reported previously.^{33,34}

The stable α -polymorph of CaH₂⁵⁵ (determined by neutron powder diffraction at 295 K) has an orthorhombic symmetry and crystallizes in the PbCl₂-type structure (space group *Pnma*). The α -CaH₂ unit cell contains four formula-units, where the hydrogen atoms bonded to the same Ca atom are crystallographically not equivalent. They are located within pseudo-tetrahedral and square-pyramidal interstices (see Figure 1). As summarized in Table 1, PAW PP describe quite well the ground-state structure of α -CaH₂ with respect to the experimental geometry, providing less than 1% error on predicting the lattice parameters and about 2% on cell volume. A similar minimum-energy structure can be achieved by using the QE PP. In addition, there is also a good agreement with the DFT calculations previously reported.³⁶ The reliability of the α -CaH₂ optimized structure can be further confirmed by looking at selected geometric details, belonging to the pseudo-tetrahedral and square-pyramid regions (see Table 2).



Figure 1. Minimum-energy crystal structure of α -CaH₂. This pictorial representation highlights the different crystallographic behaviour for H1 and H2 (both in orange): they are located in the centre of a pseudo-tetrahedron (green) and a square-pyramid (red), respectively. Atoms: H (white) and Ca (blue).

Coorrectric unit	Bonds and Angles			Во	nd length	and Angle	values	(Å)		
Geometric unit	bonds and Angles	Experimental			PAW			QE		
H1Ca ₄ pseudo – tetrahedral	Ca-H1 (Å)	2.27	2.32	2.26	2.26	2.28	2.24	2.25	2.28	2.24
	<ca-h1> (Å)</ca-h1>	2.28			2.26			2.25		
	Ca-H1-Ca (°)	101.24	116.73		101.29	116.70		101.30	116.67	
H2Ca₅ square-pyramid	Ca-H2 (Å)	2.38	2.52	2.65	2.39	2.50	2.62	2.38	2.50	2.61
	<ca-h2> (Å)</ca-h2>	2.54			2.52			2.52		
	Ca-H2-Ca (°)	99.23	103.63		99.67	104.13		99.65	104.18	

Table 2. Comparison between calculated and experimental Ca-H bond lengths (mean values in <>) and selected angles in H1Ca₄ tetrahedra and H2Ca₅ square-pyramids. The experimental data are taken from ref.⁵⁵

A *Fddd* orthorhombic crystal structure has been assumed for calcium borohydride, α -Ca(BH₄)₂, as determined by X-ray synchrotron powder diffraction at 300 K.³⁸ Eight formula-units of Ca(BH₄)₂ are enclosed within the unit cell, for a total of 88 atoms. X-ray diffraction experiments revealed that there are two non equivalent hydrogen atoms in the cell. The calculations performed with Quantum-ESPRESSO provided similar crystal geometries for the ground-state structures (Table 1), in good agreement with the experimental results. In fact, less than 1% errors occur for the minimum-energy structures found by using both our PAW and QE PP. Furthermore, it should be noted that the structure of α -Ca(BH₄)₂, resulted from calculations with the lowest energy, is in accordance with the optimized structures obtained by other plane-wave calculations. For instance, starting from a Fddd orthorhombic geometry, a fully relaxed structure with a = 8.765, b = 13.129 and c = 7.491 Å has been obtained.³⁷ In addition, all the optimized structures are characterized by a nearly ideal tetrahedral configuration of the $[BH_4]^-$ units, with B-H bond lengths approximately equal to 1.22-1.23 Å. Nevertheless, some literature suggests that the F2dd structure provided a better fit than the Fddd structure for the description of the experimental room-temperature crystal structure of α -Ca(BH₄)₂.⁵⁶ Therefore, we performed a full geometry optimization on α -Ca(BH₄)₂, by using a F2dd starting structure; a minimum-energy geometry that is very similar to that previously obtained by adopting the Fddd structure was achieved, with lattice parameters a = 8.748, b = 13.118 and c = 7.485 Å. This structure also revealed to be in good agreement with other fully optimized geometries found in the literature.³⁷ In addition to the α -polymorph, we focused also on the crystal structure of β -Ca(BH₄)₂, as the commercial calcium borohydride is actually a mixture of α and β phases (see also NMR data below). Two formula units of $Ca(BH_4)_2$ are contained within the tetragonal unit cell, for a total of 22 atoms. Synchrothron powder diffraction analysis at 305 K suggested that this structure crystallizes in the P-4 space group.⁵⁶ However, more recently, the crystal structure of β -Ca(BH₄)₂ was refined by Noritake et al. from synchrothron X-ray diffraction data at 433 K, arguing that it is better described by the $P4_2/m$ space group.³⁸ Four and three structurally different hydrogen atoms were found within the unit cell of the two structures, respectively. Although the two starting geometries slightly differ from each other, the same minimumenergy structure was reached employing both the sets of PP.

The *Pnma* orthorhombic structure of lithium borohydride, LiBH₄, was refined by Souliè et al.⁵⁷ from synchrotron X-ray powder diffraction at room temperature, and it has been selected as starting geometry for variable-cell optimization. The unit cell contains four formula-units of LiBH₄, and three hydrogen atoms are crystallographically not equivalent. The [BH₄]⁻ units form strongly distorted tetrahedrons with H-B-H angles going approximately from 85° to 120°. However, the calculated results do not reproduce the experimental structure. Although the cell volume is only 0.25% smaller than the experimental one, the lattice parameters of the structure with minimum of energy differ significantly from those experimentally determined by Souliè et al.,⁵⁷ varying in opposite directions of almost the same amount. In fact, in the optimized structure, the *a* parameter is enlarged of about 3.75% and the *c* parameter (along the *z*-axis) is shortened of about 3% with respect to the corresponding experimental values. Furthermore, the calculated bond lengths and angles of the borohydride anions are similar to an ideal tetrahedron, rather than the distorted geometry observed experimentally at ambient temperature,^{54,57} with almost constant B-H bond lengths of 1.22-1.23 Å and H-B-H angles close to the ideal value of 109.5°. Quite interestingly, an analogous description of the ground-state structure of α -LiBH₄ resulted from other DFT plane-wave based calculations,⁴¹⁻⁴³ and also from some experiments at low temperature.^{67,68}

SSNMR experiments and GIPAW calculations

SSNMR chemical shifts (δ) of light metal hydrides and borohydrides have been measured and the results are reported in Table 3. The corresponding experimental spectra are reported in the Supporting Information (Figure SI1). Calculations of the NMR chemical shifts have been performed by means of the GIPAW²² method, implemented as a module in the Quantum-Espresso⁵⁰ distribution, on the optimized geometries previously described. For comparison and validation, the GIPAW calculations were repeated on the same structures employing the Ceresoli's QE PP. Theoretical results, summarized in Table 3 (computed chemical shift tensor values are reported in Table SI1 in the Supporting Information), are in good agreement with the experimental data.⁶⁹ It should be emphasized that geometry optimizations and NMR calculations are often performed with different sets of PP. On the contrary, a single set of PP suitable to give acceptable results in both types of calculations have been used in this case. By using our PAW PP, we found that for NaH, LiH and NaBH₄ at 60 Ry cut-off, the absolute magnetic shielding (¹H and ²³Na) cannot reach a convergence. On the other hand, energy cut-offs of 200 and 120 Ry provided almost the same results. Similar results were obtained by using the Ceresoli's QE PP. As a consequence, 120 Ry was selected as energy cut-off for all NMR calculations.

For the Group I hydrides (NaH and LiH), the calculated ¹H SSNMR δ values are in good agreement with experimental data. Similar issues can be outlined for the alkali-earth hydrides MgH₂ and CaH₂. It is worth noting that in MgH₂, a single value of the isotropic total magnetic shielding (σ) is expected, whereas for

CaH₂ different σ values correspond to crystallographically (and so magnetically) different hydrogen atoms. In the latter case, since the experimental spectrum shows only a single broad peak due to an intrinsic large linewidth of the proton signals in the solid state,¹³ the computed signals (at 4.72 and 4.64 ppm with PAW PP) are reported as a mean δ value in Table 3 (see Supporting Information). Nevertheless, these different values for CaH₂ revealed to be very close to each other (i.e. under the NMR spectral resolution). In any case, for MgH₂ and CaH₂, calculated values close to the experimental ones were obtained by using our PAW PP, with an overestimation for the calculated δ values of 0.4 and 0.2 ppm, respectively. The use of the Ceresoli's QE PP for GIPAW calculations on these systems brought to similar results.

Calculations of the ¹H SSNMR chemical shifts for borohydride systems, LiBH₄ and Ca(BH₄)₂, are more challenging. This is mainly due to the presence of non equivalent hydrogen atoms in the unit cell, leading to the need of considering the average-weighted σ value, as well as to the difficulties in their structural optimization (see above). In spite of these disadvantages, the results of computation of the chemical shift for Ca(BH₄)₂ are rather good, with a calculated δ value 0.5 ppm smaller than the experimental one. On the contrary, a maximum error of about 1.0 ppm occurred on the calculation of the ¹H SSNMR δ value of LiBH₄, obtained from the weighted mean of the σ values associated to the three non equivalent hydrogen atoms contained in the asymmetric unit. Comparable results for orthorhombic borohydride systems were obtained performing the same calculations with the Ceresoli's QE PPs. The Ca(BH₄)₂ sample purchased from Aldrich was characterized as a mixture of the α and β phases (see above) as observed by the presence of a signal at -32.5 ppm with a shoulder at -29.9 ppm in the ¹¹B MAS spectrum (Figure 2, top spectrum). By running the spectrum of pure α -Ca(BH₄)₂ (Figure 2, bottom spectrum) it was possible to correctly assign the former to the β and the latter to the α form, as reported in the literature.^{46,70}



Figure 2. ¹¹B MAS (Hahn echo) spectra (central peak) of α -Ca(BH₄)₂ (bottom) and Ca(BH₄)₂ from Aldrich (top) recorded with a spinning speed of 14 kHz.

However, no differences between the commercial and pure α phase were observed in the experimental ¹H MAS spectra. Concerning α -Ca(BH₄)₂, the results derived from GIPAW calculation (Table 3) performed on the optimized structure are based on the *Fddd* structure. In this case there are two magnetically non

equivalent protons within the cell that produce two different σ values; the mean δ value for ¹H is –0.2 ppm. Conversely, the *F2dd* structure is characterized by the presence of four non equivalent hydrogen atoms in the unit cell. For this space group, QE PP provides four different σ values in pairs very similar (0.11, 0.10 and 0.31, –0.30 ppm, respectively) while PAW PP gives only three δ values, two of which are very close to each other (0.04, 0.03 and –0.37 ppm) (Table SI1). Nevertheless, by considering only the mean values, the same results were achieved by starting from both the *Fddd* and *F2dd* structures.

For the considered metal hydrides and borohydrides, a good correlation between ¹H experimental (δ_{exp}) and calculated (δ_{calc}) values was obtained for both PAW ($\delta_{exp} = 0.76 \cdot \delta_{calc} + 0.60$, R² = 0.986) and QE ($\delta_{exp} = 0.89 \cdot \delta_{calc} + 0.35$, R² = 0.974) PP (Figure 3), with a mean error of about 0.48 and 0.35 ppm, respectively.



Figure 3. Experimental vs. calculated ¹H chemical shifts (TMS as reference).

Typically, errors of ¹H δ calculations for molecules in solutions are close to 0.2 ppm,^{71,72} but larger values are expected for calculations in the solid state. Taking into account the experimental uncertainties on ¹H SSNMR δ_{iso} values, obtained correlations can efficiently predict the experimental ¹H SSNMR chemical shifts. A similar procedure was adopted for the calculation of the ⁶Li, ²³Na and ¹¹B chemical shifts (see Table 3). From a comparison of calculated values with ⁶Li experimental results ⁴⁹ on LiH and LiBH₄, it turned out that accurate results can be obtained with Quantum-ESPRESSO, by using both our PAW PP and the GIPAW standard ones. However, while our PP tend to underestimate the ⁶Li chemical shift of LiBH₄ of 0.3 ppm, the GIPAW standards provided a value which is higher than the experimental one of the same quantity. As for ¹¹B results, PAW PP allowed to obtain a substantial improvement in the description of the chemical shift values for the compounds under investigation. In particular, for ¹¹B shift value of LiBH₄, an error of less than 2 ppm occurred by employing our PAW PP, whereas the isotropic chemical shift value calculated by using QE PP was about 4.3 ppm higher than the experimental one. A similar behaviour was achieved also about the prediction of the NMR parameters of Ca(BH₄)₂, as it can be seen in the Table 3. Moreover, our NMR computed results are able to reliably reproduce the ¹¹B experimental spectrum of commercial Ca(BH₄)₂; in fact, as observed from experiments (see Figure 2), the GIPAW calculations confirmed that the ¹¹B signal derived from the β -phase is about 2 ppm more shielded than the signal corresponding to the α -phase.

Concerning the quadrupolar interaction, which is supposed to be a more accurate parameter for evaluating the quality of computational data, we observed in the ⁶Li, ²³Na and ¹¹B experimental spectra of NaBH₄, NaH, and LiH no evidences of either first or second order quadrupolar interaction, in agreement with a spherically symmetric environment of the nuclei. This has been confirmed by the negligible values obtained by the GIPAW calculation of principal EFG tensor components and the quadrupolar coupling constants (Table SI2 in the Supporting Information). However, this is not the case of ¹¹B spectra of LiBH₄ and Ca(BH₄)₂ (either α and β phases) (black spectra in Figure 4) which show an extensive pattern of spinning sidebands. Simulation of the experimental spectra (red spectra in Figure 4) allowed to extract EFG tensor and quadrupolar coupling constant values together with the chemical shift tensor components, all reported in Table 4. Also for these samples, the GIPAW data reliably reproduce those obtained from the experimental spectra being in the range of commonly reported error.^{73,74}

Sample	¹ H	l, δ (pp	m)	11	Β, δ (ppi	m)	²³ N	a, δ (p	om)	⁶ Li,	i, δ (ppm)	
	Ехр	(1)	(2)	Ехр	(1)	(2)	Ехр	(1)	(2)	Exp. ⁴⁹	(1)	(2)
NaH	3.7	4.5	3.3				26.2	34.1	33.9			
LiH	3.0	3.0	3.3							0.0	0.0	0.0
MgH ₂	3.4	3.8	3.9									
CaH₂	4.5	4.7	4.4									
LiBH ₄	-0.2	-1.2	-0.6	-41.4	-39.5	-37.1				-1.3	-1.6	-1.0
α-Ca(BH ₄) ₂	0.3	-0.2	-0.1	-29.9	-21.9	-19.8						
β-Ca(BH ₄) ₂	0.3	-0.2	0.0	-32.5	-23.8	-21.6						

Table 3. Experimental and GIPAW-calculated NMR chemical shifts (ppm) with (1) generated PAW and (2) Ceresoli's QE PP. δ_{iso} values are referenced to TMS for ¹H, NaBH₄ for ²³Na, BF₃OEt₂ for ¹¹B and LiH for ⁶Li.



Figure 4. Experimental (black) and simulated (red) ¹¹B MAS (Hahn echo) spectra of LiBH₄, α -Ca(BH₄)₂ and Ca(BH₄)₂ Aldrich (α + β form) recorded with a spinning speed of 14 kHz. For simulation details see Experimental and Computational Methods.

Table 4. ¹¹	B simulated and computed chemical shift anisotropy and quadrupolar values for LiBH ₄ ,	α -Ca(BH ₄) ₂ and β -
Ca(BH ₄) ₂ . I	For simulation details see the Experimental and Computational Methods section.	

		δ _{iso} (ppm)	δ _{xx} (ppm)	δ _{γy} (ppm)	δ _{zz} (ppm)	δ _{csa} (ppm)	η _{csa}	C _Q (MHz)	η Q
LiBH ₄	simul.	-41.1	-38.7	-40.2	-44.5	-3.3	0.46	0.10	0.51
	PAW	-39.5	-41.9	-40.2	-36.3	3.2	0.55	0.13	0.64
α-Ca(BH ₄) ₂	simul.	-29.8	-33.4	-30.5	-25.5	4.3	0.68	0.20	0.89
	PAW ^a	-21.9	-16.3	-20.7	-28.7	-6.8	0.64	-0.52	0.89
β -Ca(BH ₄) ₂	simul.	-32.5	-32.3	-32.4	-32.8	-0.3	0.63	0.18	0.85
	PAW ^b	-23.8	-18.8	-23.5	-29.2	-5.4	0.86	-0.48	0.85

^a Fddd structure; ^b P-4 structure

Conclusions

The use of Quantum-ESPRESSO with a new set of PAW PP, generated by the *atompaw code*, has revealed to achieve good results for the calculation of crystal structures and SSNMR chemical shifts in selected hydrogen storage materials. Results of crystal geometries for low symmetry borohydrides (LiBH₄ and Ca(BH₄)₂) revealed to be in accordance with similar DFT based computational studies. Calculated SSNMR parameters (chemical shifts , quadrupolar coupling constants, and CSA) showed good correlation with

experimental values. A maximum deviation of 1 ppm for PAW PP with respect to the experimental ¹H SSNMR chemical shifts was found. This value is comparable with the error obtained employing standard Ceresoli's PP. In summary, we were able to validate a new set of PAW PP, showing that the predicted SSNMR ¹H, ²³Na and ⁶Li chemical shift values obtained by using PAW PP, are analogous to those derived by employing the standard QE PP. In addition to this, a substantial improvement of the ¹¹B chemical shifts estimation were obtained adopting PAW PP.

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Graphic for Table of Contents



Coupling Solid-State NMR with GIPAW ab-initio Calculations in Metal Hydrides and Borohydrides

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Table SI1 – Computed Shielding tensors for all compounds under investigation.

	Nucleus	δ _{xx} (ppm)	δ _{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ ext{iso}}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	Na	34.0498	34.0500	34.0503	34.1	0.0003	0.75000
	Н	4.5364	4.5364	4.5364	4.5	0.0000	0.00000
QE	Na	33.9062	33.9061	33.9060	33.9	-0.0001	1.00000
	Н	3.3403	3.3402	3.3401	3.3	-0.0001	1.00000

NaH

NaBH₄

	Nucleus	δ_{xx} (ppm)	δ_{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ ext{iso}}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	Na	0.0003	0.0003	0.0001	0.0	-0.0001	0.00000
	В	-42.0043	-42.0043	-42.0044	-42.0	-0.0001	0.00000
	Н	0.7300	0.7300	-2.6627	-0.4	-2.2618	0.00000
QE	Na	0.0000	0.0000	0.0001	0.0	0.0001	0.00000
	В	-41.9972	-41.9972	-41.9971	-42.0	0.0001	0.00000
	Н	1.0976	1.0976	-3.3911	-0.4	-2.9925	0.00000

LiH

	Nucleus	δ_{xx} (ppm)	δ _{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ ext{iso}}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	Li	0.0042	0.0042	0.0043	0.0	0.0001	0.00000
	Н	3.0195	3.0195	3.0196	3.0	0.0001	0.00000
QE	Li	0.0008	0.0008	0.0008	0.0	0.0000	0.00000
	Н	3.3205	3.3205	3.3206	3.3	0.0001	0.00000

MgH₂

	Nucleus	δ_{xx} (ppm)	$\delta_{ m yy}$ (ppm)	δ_{zz} (ppm)	$\delta_{ ext{iso}}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	Н	2.2110	3.5396	5.6467	3.8	1.8476	0.71910
QE	Н	3.9945	3.9736	3.7445	3.9	-0.1597	0.13087

CaH₂

	Nucleus	δ _{xx} (ppm)	δ _{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ m iso}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	H1	5.0692	4.9308	4.1700	4.7	-0.5533	0.25012
	H2	4.3427	4.3695	5.2175	4.6	0.5743	0.04667
QE	H1	4.8558	4.6949	3.9462	4.5	-0.5528	0.29108
	H2	3.9913	4.0349	4.9170	4.3	0.6026	0.07235

LiBH₄

	Nucleus	δ _{xx} (ppm)	δ_{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ ext{iso}}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	Li	-0.5566	-1.0993	-3.1972	-1.6	-1.5795	0.34359
	В	-41.9350	-40.1831	-36.2946	-39.5	3.1763	0.55155
	H1	-1.8448	-1.3012	-0.4408	-1.2	0.7548	0.72019
	H2	-0.3886	-1.1660	-3.1100	-1.6	-1.5551	0.49989
	H3	0.2941	-0.7710	-2.7454	-1.1	-1.6713	0.63729
QE	Li	0.0591	-0.5262	-2.5863	-1.0	-1.5685	0.37316
	В	-39.7839	-37.9781	-33.6075	-37.1	3.5157	0.51364
	H1	0.2248	-0.4921	-1.2487	-0.5	-0.7434	0.96440
	H2	0.1806	-0.5758	-2.3189	-0.9	-1.4142	0.53486
	H3	0.8629	-0.1872	-1.9261	-0.4	-1.5093	0.69575

α-Ca	(BH₄)₂	Fddd
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	Nucleus	δ_{xx} (ppm)	δ_{yy} (ppm)	δ_{zz} (ppm)	δ_{iso} (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	В	-16.3295	-20.6651	-28.6903	-21.9 -6.7953		0.63803
	H1	-1.0618	-0.6751	0.5985	-0.4	0.9780	0.39541
	H2	1.4853	0.0399	-1.4570	0.0	-1.4797	0.97680
QE	В	-14.2737	-18.6149	-26.5024	-19.8 -6.7054		0.64742
	H1	-1.0114	-0.6521	0.6975	-0.3	1.0195	0.35243
	H2	-1.3186	0.0839	1.4906	0.1	1.4053	0.99801

α-Ca(BH₄)₂ *F2dd*

	Nucleus	δ _{xx} (ppm)	δ _{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ ext{iso}}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	В	-16.2979	-20.6464	-28.6557	-21.9	-6.7890	0.64052
	H1	-1.0545	-0.6578	0.5992	-0.4	0.9702	0.40887
	H2	-1.0536	-0.6599	0.5981	-0.4	0.9699	0.40592
	H3	1.4949	0.0500	-1.4475	0.0	-1.4800	0.97631
	H4	1.4981	0.0548	-1.4435	0.0	-1.4800	0.97522
QE	В	-14.2327	-18.5897	-26.4554	-19.8	-6.6961	0.65067
	H1	-0.9928	-0.6277	0.7076	-0.3	1.0119	0.36081
	H2	-0.9915	-0.6299	0.7062	-0.3	1.0113	0.35757
	H3	-1.2980	0.1021	1.5095	0.1	1.4050	0.99654
	H4	-1.2938	0.1068	1.5125	0.1	1.4040	0.99758

β-Ca	(BH₄)	2	P-4
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	Nucleus	δ_{xx} (ppm)	δ_{yy} (ppm)	δ_{zz} (ppm)	δ_{iso} (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	В	-18.8292	-23.4528	-29.2164	-23.8	-5.3836	0.85883
	H1	0.3514	-0.0310	-1.6315	-0.4	-1.1945	0.32014
	H2	-0.5890	-0.4871	0.9580	0.0	0.9974	0.10217
	H3	0.1834	-0.2029	-0.9103	-0.3	-0.6004	0.64344
	H4	-0.5925	-0.4863	0.9555	0.0	0.9966	0.10656
QE	В	-16.5647	-21.3195	-26.8205	-21.6	-5.2523	0.90529
	H1	0.5671	0.1164	-1.2126	-0.2	-1.0362	0.43494
	H2	-0.4438	-0.1109	1.1235	0.2	0.9339	0.35646
	H3	0.3043	0.0068	-0.4799	-0.1	-0.4236	0.70226
	H4	-0.4462	-0.1118	1.1210	0.2	0.9333	0.35829

β-Ca(BH₄)₂ P4₂/m

	Nucleus	δ _{xx} (ppm)	δ _{yy} (ppm)	δ_{zz} (ppm)	$\delta_{ m iso}$ (ppm)	δ_{CSA} (ppm)	η _{csa}
PAW	В	-18.7948	-23.4389	-29.1659	-23.8	-5.3660	0.86546
	H1	-0.5557	-0.4522	0.9907	0.0	0.9964	0.10387
	H2	0.2172	-0.1684	-0.8776	-0.3	-0.6013	0.64124
	H3	0.3898	0.0052	-1.6038	-0.4	-1.2009	0.32027
QE	В	-16.5704	-21.3429	-26.8098	-21.6	-5.2354	0.91158
	H1	-0.4479	-0.1156	1.1169	0.2	0.9324	0.35638
	H2	0.5667	0.1144	-1.2244	-0.2	-1.0433	0.43353
	H3	0.3000	0.0013	-0.4857	-0.1	-0.4242	0.70409

Table SI2 – Computed EFG tensors for all compounds under investigation.

	Isotope	Spin	Quadrupole	Sample	V _{xx}	V _{yy}	V _{zz}	C _Q (MHz)	η_Q
			Moment (Q) (10 ⁻³⁰ m ²)						
PAW	²³ Na	3/2	10.4	NaBH ₄	0.0000	0.0000	0.0000	0.0000	0.00000
				NaH	0.0000	0.0000	0.0000	0.0000	0.00000
	¹¹ B	3/2	4.059	NaBH ₄	0.0000	0.0000	0.0000	0.0000	0.00000
				LiBH ₄	-0.0026	-0.0116	0.0141	0.1348	0.63560
				Fddd α -Ca(BH ₄) ₂	0.0030	0.0513	-0.0542	-0.5170	0.89094
				F2dd α -Ca(BH ₄) ₂	0.0030	0.0513	-0.0543	-0.5177	0.89120
				<i>Р-4 β-Са(ВН₄)₂</i>	0.0039	0.0468	-0.0507	-0.4839	0.84605
				<i>P4₂/m β</i> -Ca(BH ₄) ₂	0.0039	0.0469	-0.0507	-0.4837	0.84806
	⁶ Li	1	-0.0808	LiH	0.0000	0.0000	0.0000	0.0000	0.0000
				LiBH ₄	0.0015	0.0053	-0.0069	0.0013	0.55849
	⁷ Li	3/2	-4.01	LiH	0.0000	0.0000	0.0000	0.0000	0.0000
				LiBH ₄	0.0015	0.0053	-0.0069	0.0646	0.55849
	²⁵ Mg	5/2	19.94	MgH ₂	-0.0342	-0.0602	0.0943	4.4195	0.27553
QE	²³ Na	3/2	10.4	NaBH ₄	0.0000	0.0000	0.0000	0.0000	0.00000
				NaH	0.0000	0.0000	0.0000	0.0000	0.00000
	¹¹ B	3/2	4.059	NaBH ₄	0.0000	0.0000	0.0000	0.0000	0.00000
				LiBH ₄	-0.0021	-0.0101	0.0123	0.1170	0.65390
				Fddd Ca(BH ₄) ₂	0.0018	0.0247	-0.0264	-0.2522	0.86426
				F2dd Ca(BH ₄) ₂	0.0018	0.0248	-0.0266	-0.2537	0.86107
				<i>Р-4 β-Са(ВН₄)₂</i>	-0.0013	-0.0180	0.0193	0.1842	0.86609
				<i>P4₂/m β</i> -Ca(BH ₄) ₂	-0.0014	-0.0180	0.0194	0.1849	0.85764
	⁶ Li	1	-0.0808	LiH	0.0000	0.0000	0.0000	0.0000	0.0000
				LiBH ₄	0.0017	0.0038	-0.0055	0.0010	0.38732
	⁷ Li	3/2	-4.01	LiH	0.0000	0.0000	0.0000	0.0000	0.0000
				LiBH ₄	0.0017	0.0038	-0.0055	0.0521	0.38732
	²⁵ Mg	5/2	19.94	MgH ₂	-0.0087	-0.0597	0.0683	3.2010	0.74635



Figure SI1- Experimental ¹H, ¹¹B and ²³Na SSNMR spectra of all the studied samples .