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1 **Agricultural operations planning in fields with multiple obstacle areas**

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7 **Highlights**

- 8 • Generation of feasible area coverage plan in fields with multiple obstacle areas.
- 9 • The optimization of the block sequence connection is formulated as a TSP problem.
- 10 • The developed model requires low computation time to compute the optimal block sequence.
- 11 • The error between the simulated and actual total travelled distance was 0.15% - 0.21%.

12 **Abstract**

13 When planning an agricultural field operation there are certain conditions where human planning can lead to
14 low field efficiency, e.g. in the case of irregular field shapes and the presence of obstacles within the field
15 area. The objective of this paper was to develop and implement a planning method for agricultural vehicles
16 operating in fields inhabiting multiple obstacles. The developed approach consists of three stages. The first
17 two stages regard the generation of the field geometrical representation where the field is split into sub-fields
18 (blocks) and each sub-field is covered by parallel tracks, while the third stage regards the optimization of the
19 block sequence aiming at minimizing the blocks connection travelled distance. The optimization problem
20 was formulated as a TSP problem and it was solved implementing the ant colony algorithmic approach. To
21 validate the developed model, two application experiments were designed. The results showed that the model
22 could adequately predict the motion pattern of machinery operating in field with multiple obstacles. Errors of
23 total distance travelled were 0.21% and 0.15% for the two experimental setups. Regarding the computation

24 time, the model required low computation times from 2.92 s in field with one obstacle to 11.51 s in field with
25 two obstacles.

26 **Keywords:** route planning, agricultural vehicles, ant colony algorithm, traveling salesman problem.

27 **1 Introduction**

28 When planning an agricultural field operation there are certain field conditions where experience-based
29 planning can lead to low machinery efficiency, for example the case of irregular field shapes and case of the
30 presence of obstacles within the field area (Oksanen and Visala, 2007). So far, a significant amount of
31 research has been carried out to solve the route planning problem in field operations. These advances include
32 a number of methods for the geometrical field representation (de Bruin et al., 2009; Oksanen and Visala,
33 2009; Hofstee et al., 2009; Hameed et al., 2010) and a number of methods for route planning within a given
34 field geometrical representation (Bochtis and Vougioukas, 2008; Bochtis and Sørensen, 2009; de Bruin et al.,
35 2009; Bochtis et al., 2013, Scheuren et al., 2013).

36 In the case of fields with inhabited obstacles, in all developed methods the field is always decomposed into
37 sub-fields (referred to as blocks). Due to the specific nature of field operations decomposition methods of the
38 working space from the industrial robotics discipline area (Choset, 2001; Galeran and Carreras, 2013) cannot
39 be directly applied. Oksanen and Visala (2007) developed a field decomposition method based on the
40 trapezoidal decomposition for agricultural machines to cover the field. After decomposition, the trapezoids
41 are merged into blocks under the requirements that the blocks have exactly match edges and the angles of
42 ending edges is not too steep. Hofstee et al., (2009) developed a tool for splitting the field into single convex
43 fields. Stoll (2003) introduced a method to divide the field into blocks based on the longest side of the field.
44 Palmer (2003) presented a method of generating pre-determined tracks in fields with obstacles. Jin and Tang
45 (2009) developed an exhaustive search algorithm for finding the optimal field decomposition and path
46 directions for each subfield. However, in all of the above mentioned methods the optimum order to traverse
47 the decomposed block was not derived. A first theoretical approach that provided the traversal sequence of
48 the resulted blocks was presented in Hameed et al., (2013). The approach was based on the implementation

49 of genetic algorithms for the optimization of the visiting sequence of the different sub-field areas resulted by
50 the presence of the obstacles. However, the computational requirements of the approach were exponential to
51 the problem size (e.g. the number of obstacles in the field area) and the feasibility of the approach has not
52 been tested in terms of their implementation on the real farming conditions.

53 The objective of this paper was to develop a planning method that generates a feasible plan for
54 non-capacitated agricultural machines executing area coverage operations in fields inhabiting multiple
55 obstacle areas. The method consists of three stages. The first two stages regard the generation of the
56 field-work tracks and the division of the field into blocks, respectively, and the third stage regards the
57 optimization of the sequence that the blocks are worked under the criterion of the minimization of the blocks
58 connection distance. The problem of finding the optimal block traversal sequence was formulated as a
59 travelling salesman problem (TSP) and it was solved by implementing the ant colony algorithmic approach

60 **2 Methodology**

61 **2.1 Overview**

62 The headland pattern is one of the most common field coverage patterns for agricultural machines, in which
63 the field is divided into two parts, the headland area and field body area. The field body is the primary
64 cropping area and it is covered with a sequence of straight or curved field-work tracks. The distance between
65 two adjacent tracks is equal to the effective operating width of the agricultural machine. The headland area is
66 laid out along the field border with the main purpose to enable the machines to turn between two sequential
67 planned tracks. The order in which the agricultural machines operate in the two types of areas depends on the
68 type of the operation; for example, the headland area is harvested before the field body, while the field body
69 is seeded before the headland area. When a field has obstacles headlands are also laid out around the
70 obstacles. The field body is split into a number of sub-fields (or blocks) around the obstacles, such that all
71 blocks are free of obstacles.

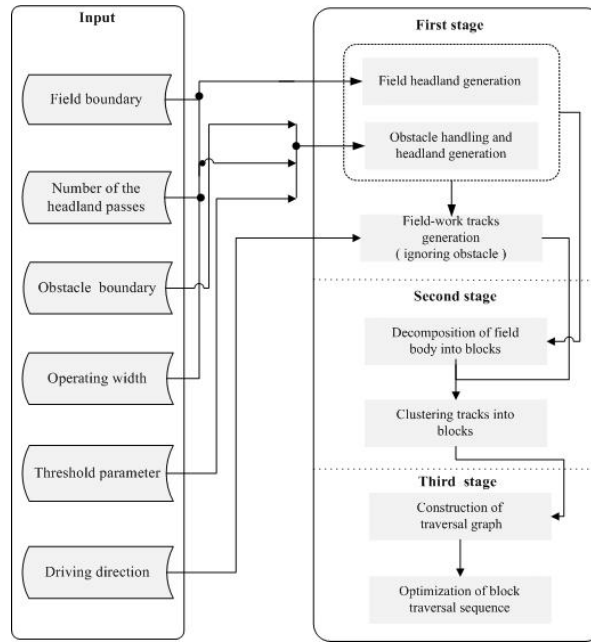
72 The planning method involves the following three stages:

- 73 a) In the first stage, the field area and the in-field obstacle(s) are represented as a geometrical graph,
74 This process includes the headland generation, the obstacle handling, and an initial generation of
75 field-work tracks (ignoring the in-field obstacles until stage 2) (section 2.3).
- 76 b) In the second stage, the field body is decomposed into block areas and the previous generated
77 field-work tracks are divided and clustered into these block areas (section 2.4).
- 78 c) In the third stage, the problem of the optimal traversal sequence of the blocks (in terms of area
79 coverage planning) is derived (section 2.5).

80 The input parameters of the planning method include:

- 81 • The boundary of the field area and the boundaries of the in-field obstacles. All boundaries are
82 expressed as a clock-wise ordered set of vertices.
- 83 • The number of the headland passes (h) for the main field and around each obstacle.
- 84 • The driving direction (θ). It determines the direction of the parallel fieldwork tracks that cover the
85 field area.
- 86 • The operating width (w). This is the effective operating width of the implement and also represents
87 the width of the field-work tracks.
- 88 • The threshold parameter (r), for the classification of the obstacle type (explained in section 2.2.2).

89 A graphical description of the proposed planning method is presented in the diagram in Fig. 1.



90

91

Fig. 1. The architecture of the proposed planning method.

92 **2.2 First stage**

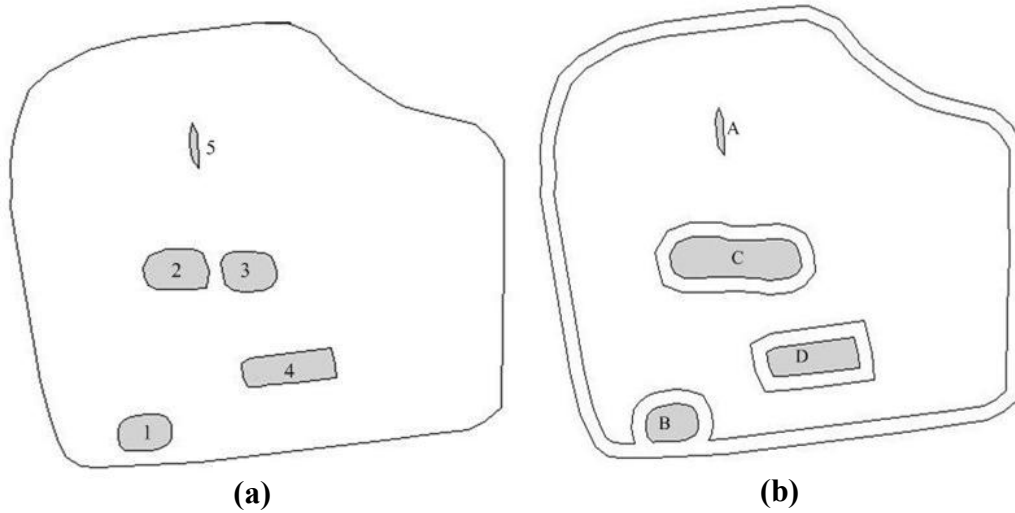
93 **2.2.1 Generation of field headland**

94 The field headland area is obtained by offsetting the boundary inwardly by a width equal to the
 95 multiplication of the operating width, w times the number of headland passes, h . The distance from the
 96 field boundaries to the first headland pass is half of the operating width, $w/2$ while the distance between
 97 subsequent headland passes equals to the operating width, w . An inner boundary is created at distance $w/2$
 98 from the last headland pass.

99 **2.2.2 Categorizing of obstacles and generation of obstacles headlands**

100 There are different types of obstacles in terms of their effect on the execution of a field operation. For
 101 example, certain physical obstacles due to their relatively small dimensions do not constitute an operational
 102 obstacle resulting in the generation of sub-fields (e.g. in Fig. 2a: Obstacle 5 is potentially such an obstacle).
 103 Other obstacles might exist that are close to the field boundary and the generation of sub-fields is not

104 required (e.g. obstacle 1 in Fig. 2). Finally, there are obstacles in close proximity that from the operational
105 point of view should be considered as one obstacle (e.g. obstacles 2 and 3 in Fig. 2).
106



107

108 **Fig. 2. Different obstacles configurations within a field area (a) and their classification (b).**

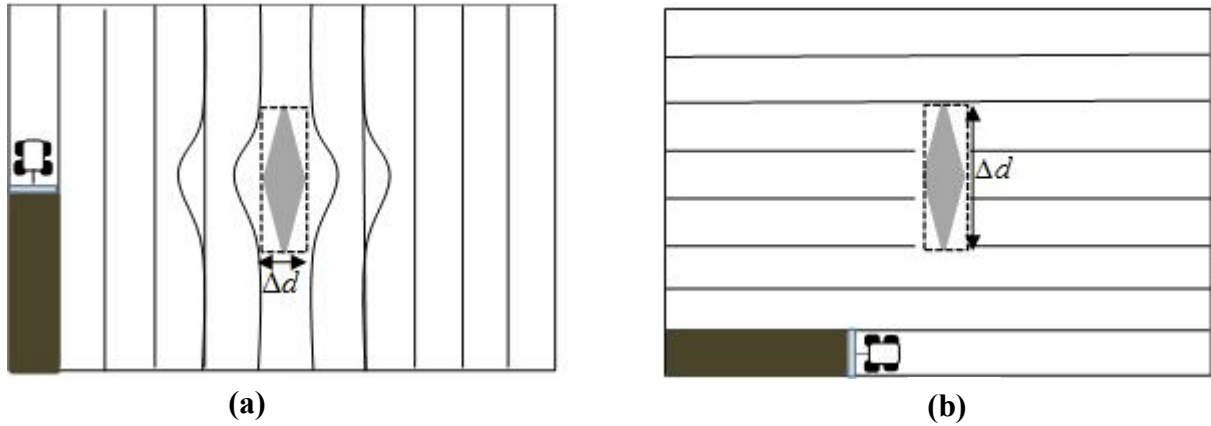
109 Four types of obstacles are defined:

110 Type A. An obstacle that due to size and configuration in relation to the driving direction does not affect the
111 coverage plan generation. In order to classify an obstacle as type A, the minimum boundary box of the
112 obstacle polygon is generated with one of its edges parallel to the driving direction. If the dimension, Δd of
113 the minimum bounding box that is perpendicular to the driving direction is less than the threshold parameter
114 r , this obstacle is considered as type A obstacle. Fig. 3a and Fig. 3b present how the driving direction θ
115 determines the classification of an obstacle as type A or not.

116 Type B. This type includes obstacles where their boundary intersects with the inner boundary of the field.
117 Type B obstacles are incorporated into the inner boundary of the field and the field headland is extended
118 around this obstacle.

119 Type C. This type includes obstacles where the minimum distance between another obstacles is less than the
120 operating width, w . In this case both obstacles are classified as of type C and a subroutine is used to find the
121 minimal bounding polygon to enclose these obstacles. For instance, assuming that the minimum distance

122 between the obstacle 2 and 3 in the Fig 2.a is less than the operating width, w , then the minimal bounding
 123 polygon (MBP) is gained by the sub-routine to represent the boundaries of these two obstacles as shown in
 124 Fig 2.b



125

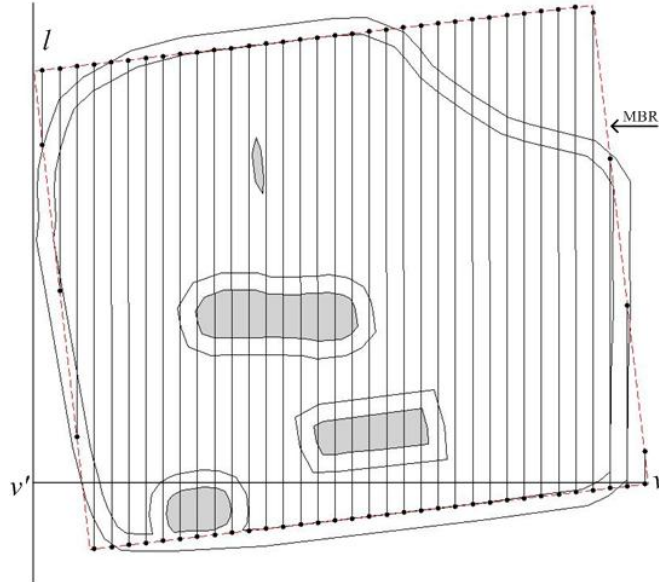
126 **Fig. 3. The same obstacle can be classified as of type A (a) and as of type D (b) depending on the**
 127 **orientation of the obstacle as compared to the driving direction where $r = w$.**

128 Type D. All remaining obstacles are considered as the Type D. Also the resulted new obstacles derived by
 129 the connection of two or more obstacles of type C are also classified as type D obstacles. Headland areas are
 130 generated only for the obstacles of type D. The method of generating obstacle headland is analogous to the
 131 method of field headland generation; however, the offset direction of the boundary is outward.

132 2.2.3 Generation of field-work tracks

133 Track generation concerns the process of generating parallel tracks to cover the field body. The
 134 minimum-perimeter bounding rectangle (MBR) of the inner field boundary is generated using the method of
 135 rotating calipers (Godfried, 1983). In the first step, depicted in the Fig. 4, the MBR is generated around the
 136 inner field boundary, and a reference line l parallel to θ is created intersecting one vertex on the MBR
 137 while let all other vertices of MBR located on the same half-plane determined by the line l . Let v be the
 138 vertex of the MBR with the longest perpendicular distance from l , and let v' be the projection of v on l .
 139 Then the number of the field-work tracks for a complete covering of the filed polygon area is given by
 140 $n = \lceil |vv'|/w \rceil$ (where $\lceil \cdot \rceil$ is the ceil function). The line segments to cover the entire MBR are generated

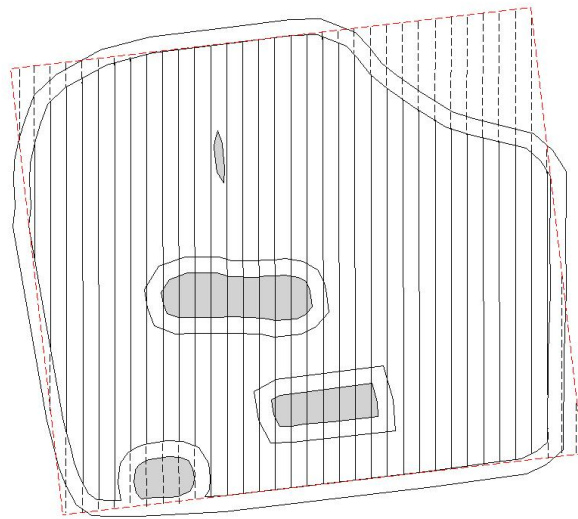
141 sequentially from the reference line l . The distance from l to the first line segment along the $\nu\nu'$ equals to
 142 $w/2$, while the distance between the subsequent line segments along the $\nu\nu'$ equals to w .



143

144 **Fig. 4. The MBR of the field is covered by a set of straight lines that are parallel to the reference line l .**

145 Let $T_0 = \{1,2,3\dots n\}$ denote the set of indices of these line segments, each of which intersects with the MBR in
 146 the form of two ending points on the MBR border. For each line segment $i \in T_0$, if it has n_i intersections
 147 with the inner field boundary it is subdivided into $n_i + 1$ new line segments. Each new line segment is
 148 checked if it is inside or outside the field body (disregarding the obstacles). If it is inside (the solid line
 149 segment in Fig. 5), the line segment is saved as a field-work track, otherwise it is discarded (the dash line
 150 segment in Fig. 5). In order to give each field-work track an index value, one of the two outmost tracks is
 151 arbitrary selected as the first track associating it with the index of value 1. Let $T = \{1,2,3\dots n'\}$ be the ordered
 152 set of the tracks.



153

154

Fig. 5. Field body is covered by the field-work tracks (the solid lines)

155

2.3 Second stage

156

2.3.1 Decomposition of field body into blocks

157

In this step, the field body is decomposed into blocks, following the boustrophedon cellular decomposition method (Choset,1997). Specifically, a line, termed as a *slice*, parallel to the driving direction θ , sweeps

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159

through the inner field boundary from left to the right. Whenever the slice either meets a new obstacle (*in*

160

event) or leaves an obstacle (*out* event) one or more preliminary blocks are formed behind the slice with

161

block boundaries along the slice (See Fig. 6). When the decomposition is completed, an adjacency

162

non-complete graph is built where each node of the graph represents a preliminary block and two nodes of

163

the graph are connected only if there are common sections between the edges of the corresponding

164

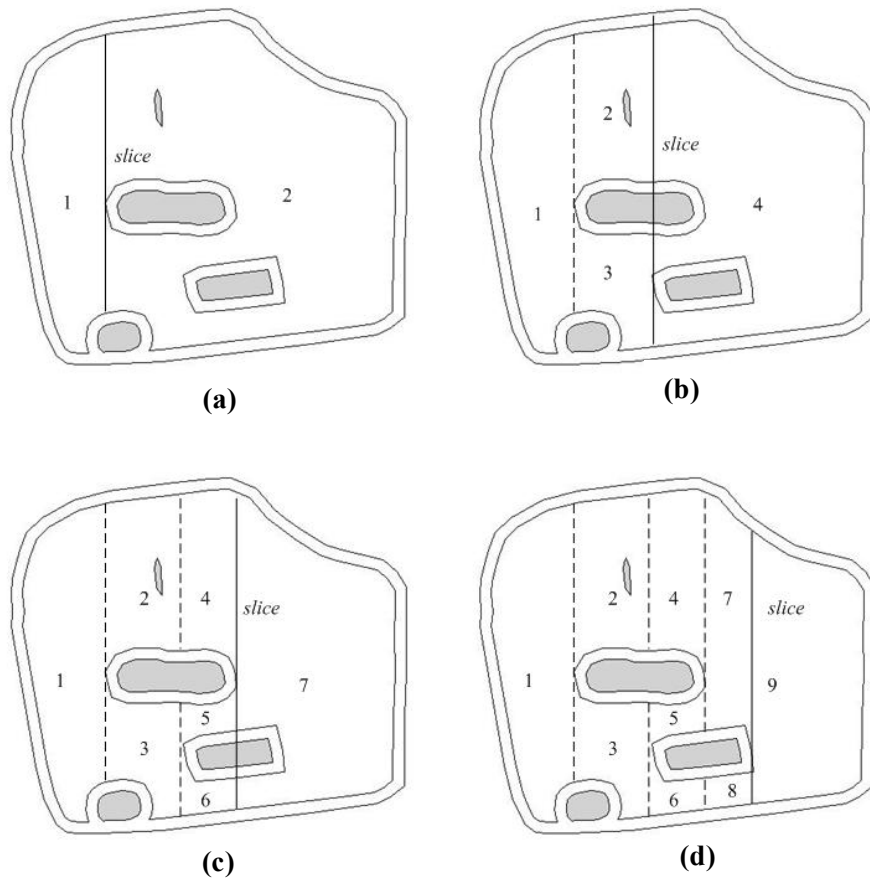
preliminary blocks (Fig. 7). The next step is to merge the generated preliminary block areas according to the

165

adjacency graph. The merging requirement is that two connected blocks in the graph have a common edge.

166

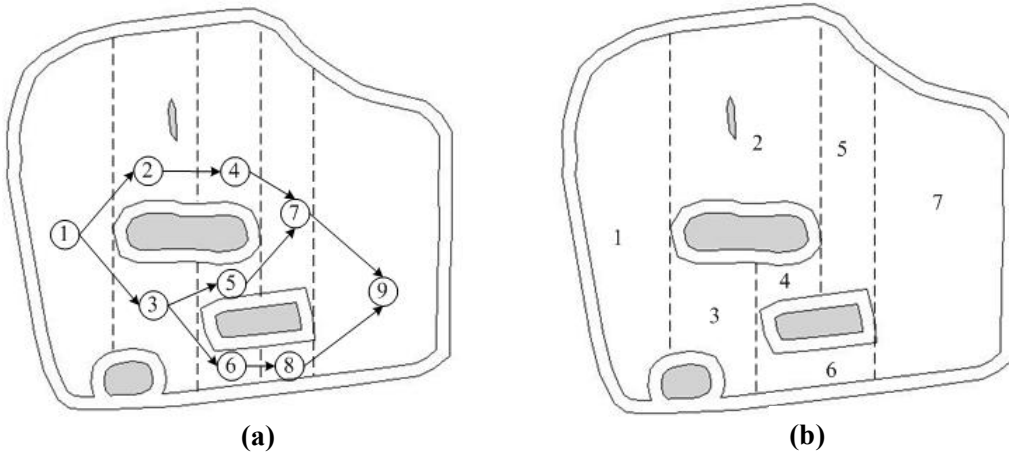
After the merging process, the generated block areas are indexed.



167

168

Fig. 6. The sequential stages of the generation of the preliminary blocks.



169

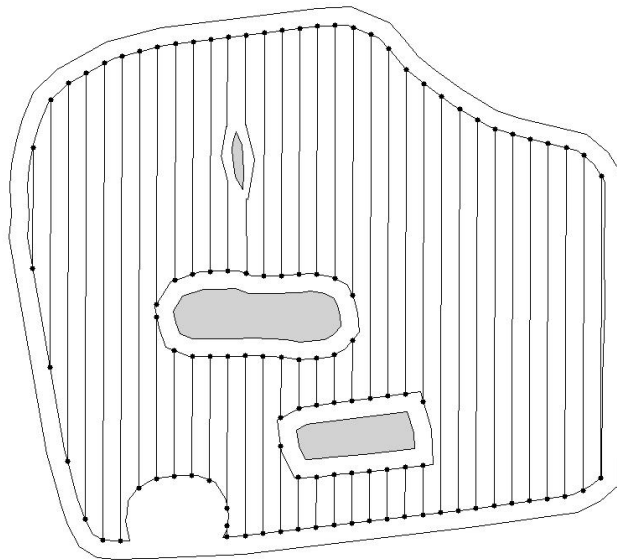
170

Fig. 7. The adjacency graph of the preliminary blocks (a) and the final generated blocks.

171 **2.3.2 Clustering tracks into blocks**

172 In the following, a method of dividing the generated tracks into segments and clustering the divided tracks
173 into blocks areas is introduced.

174 Let $B = \{1, 2, \dots, k\}$ be the generated block areas as described in section 2.3.1. The whole processing of
175 clustering includes $\|T\|$ iterations. In each iteration, if a track $i \in T$ intersects with the boundary of a block
176 area $j \in B$, it is subdivided into segments. The resulted segments are checked if they are located or not inside
177 the area of block j . The segments located inside the block area are given the same index value with the
178 index of the block. The set of the tracks in block $i \in B$ is denoted as $T_i, i \in B$.



179

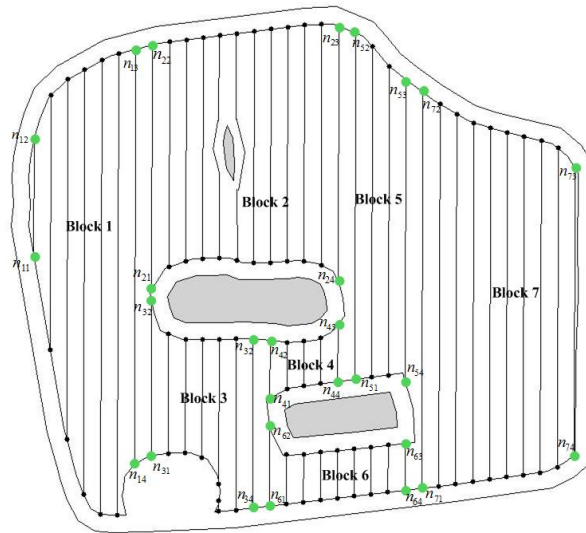
180 **Fig. 8. Division and clustering of the initial tracks into the generated block areas.**

181 **2.4 Third stage**

182 **2.4.1 Construction of traversal graph**

183 After the second stage the field has been divided into blocks and field-work tracks have been assigned to
184 each block. Each block is a sub-field without obstacles, so the coverage of the corresponding area could be
185 planned either using an optimized track sequence (e.g. *B-pattern*), or a conventional way of the continuous

186 track sequence can be used. On the presented work the latter case has been adopted and also the assumption
 187 that the work inside a block is always commenced in one of its two outmost tracks (the first or the last track
 188 of the block) has been considered. By making this assumption, each block can be represented by 4 entry/exit
 189 points: $N = \{n_{ij}, i \in B, j \in \{1,2,3,4\}\}$, where the nodes n_{i1} and n_{i2} are end points of the first track and n_{i3} , n_{i4} are
 190 end points of the last track of block j . For a given block the exit point is determined by the entry point and
 191 the parity of the number of the tracks of the block. For example, considering block 1 in Fig. 9 which has an
 192 even number of tracks, for the case of the continuous pattern if the operation commences at the end of the
 193 track corresponding to node n_{12} , then the operation will be completed at the end of the last track
 194 corresponding to node n_{14} .

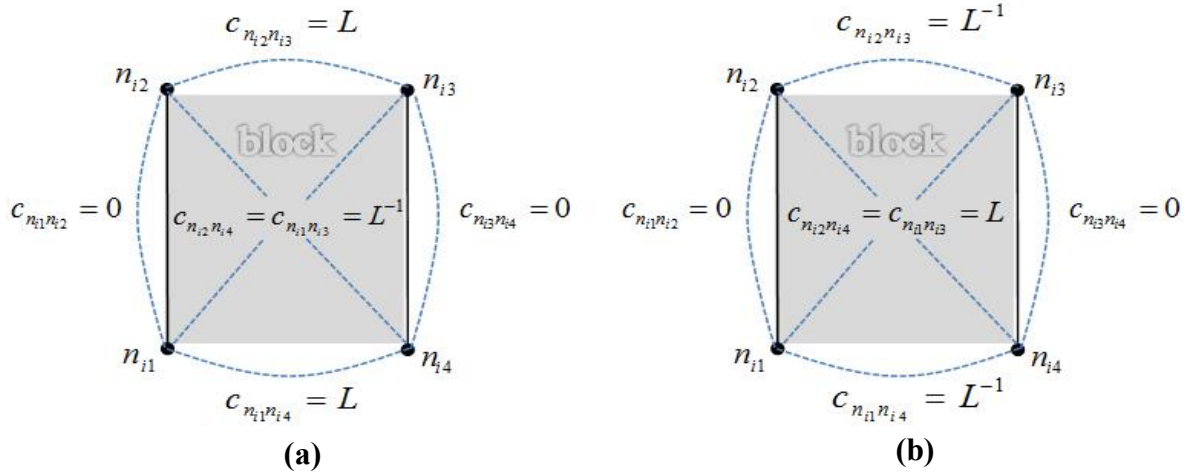


195

196 **Fig. 9. An example of a simple devised field with an obstacle, resulting in 4 blocks.**

197 The problem of the block sequencing is equivalent with the problem of traversing the undirected, weighted
 198 graph $G = \{N, E\}$, where N is the set of graph nodes as defined previously, and E is the set of edges,
 199 consisting of paths between any entry/exit points. Each edge $E_{n_{ix}, n_{jy}}, n_{ix} \neq n_{jy}$ is associated with a weight
 200 $C_{n_{ix}, n_{jy}}, n_{ix} \neq n_{jy}$ which corresponds to the transit cost from node n_{ix} to node n_{jy} . Although G can be considered
 201 as a complete graph, some potential connections between nodes within a block are not allowed while others

202 have to be enforced. For each block the function $e_i = (-1)^{\text{mod}(|T_i|,2)}$ is defined and its value (1 or -1) depends
 203 on the parity of the number of the tracks in the block. By using this function the cost for the connection
 204 between nodes belonging to the same block is given by: $c_{n_{i1}n_{i2}} = c_{n_{i3}n_{i4}} = 0$, $c_{n_{i2}n_{i3}} = c_{n_{i1}n_{i4}} = L^{-e_i}$, and
 205 $c_{n_{i2}n_{i4}} = c_{n_{i1}n_{i3}} = L^{e_i}$, where L is a (relatively) very large positive number.



206
 207 **Fig. 10. Internal cost assignment for blocks with odd (a) or even number of tracks (b)**

208 In order to avoid connections between blocks that in the physical operation will result to the situation where
 209 machine travels on a part of the field main area in order to move from one block to the other, both of the
 210 blocks must have nodes that are located either on the inner boundary of the field or in the outer boundary of
 211 the same obstacle in order to allow a connection between two blocks,.

212 For each pair of nodes of graph G a binary function $s(n_{ix}, n_{jy})$ is defined which returns the value 1 if n_{ix}
 213 and n_{jy} are both located either on the inner boundary of the field or on the outer boundary of an obstacle,
 214 and value 0 otherwise. If $s(n_{ix}, n_{jy}) = 1$ the cost for the connection of n_{ix} and n_{jy} is the actual shortest
 215 distance along the headland pass of the field or the obstacle. In contrast, a relatively large number, L , is
 216 assigned to the cost $C_{n_{ix}, n_{jy}}$ when $s(n_{ix}, n_{jy}) = 0$.

217 2.4.2 Optimization of block traversal sequence

218 Since the problem graph has been considered as a complete graph, the problem of finding the shortest path
219 for visiting all blocks is equivalent to finding the Hamiltonian path through the constructed graph G , which is
220 equivalent to the travelling salesman problem (TSP) (Hahsler, 2007). The TSP is a well-known
221 combinatorial optimization problem, which is non-deterministic Polynomial-time hard (NP-hard) problem
222 (Garey and Johnson, 1979) and various algorithmic approaches have been developed based on exact solution
223 approaches (e.g. branch-and-bound, and branch-and-cut, etc.) and approximate approaches (e.g. tabu search
224 genetic algorithm and ant colony algorithm, etc.) (Glover and Kochenberger, 2002). For the particular
225 problem presented here, any of the developed TSP solving methods can be implemented, in principle, since
226 the size of the computational problem is relatively small. This is due the fact that the number of obstacles in
227 an agricultural field is limited because of operational considerations.

228 Among the different solving methods the ant colony (ACO) algorithm has been selected. ACO is a
229 mathematical model based on ants behavior in finding the shortest route between ant colonies and food
230 sources. The principle is based on the fact that every ant deposits pheromone on the traveled path. For a
231 detailed description of the method refer to Dorigo (1996). In the presented problem, the cost of the
232 connection of two nodes, $c_{n_x n_y}, i, j \in B, x, y \in \{1, 2, 3, 4\}$, is connected with the so-called heuristic value for
233 moving between the two nodes in the ACO notion. Beyond the cost matrix, the parameters that have to be
234 quantified in the ACO are parameter ρ which represents the evaporation rate of the pheromone, and
235 parameters α , and β which are adjustable parameters to weight the importance of the pheromone.

236 3 Results and discussion

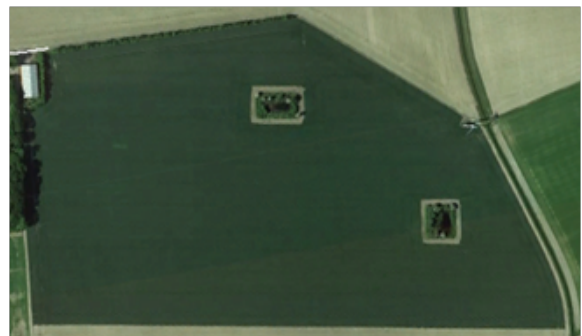
237 3.1 Feasibility of the method

238 To evaluate the feasibility of the plan generated by the method, the simulated output for two field operations
239 were compared with the actual planned and performed operations by the farmer in two fields. The first field

240 included one obstacle and has an area of 16.16 ha (Fig. 11a). The second field included two obstacles and
241 has an area of 24.25 ha (Fig. 11b). The specific operations involved potato seedbed forming and harrowing.
242 The trajectory of the tractor was recorded using an AgGPS 162 Smart Antenna DGPS receiver (Trimble,
243 GA, USA). Its accuracy is $\pm 20.3\text{-}30.5$ cm pass-to-pass. In order to provide the model with the accurate data
244 on field geometry, the vertices along the field edges were measured by tracking the field boundaries with the
245 same GPS receiver. The Douglas- Peucker line simplification algorithm (Douglas and Peucker, 1973) was
246 applied to process the GPS coordinates of the field geometry.



(a)



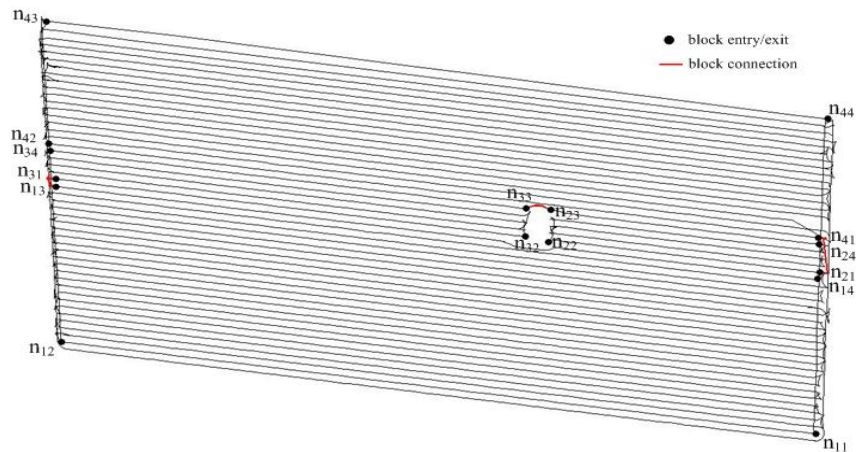
(b)

247
248 **Fig. 11. The selected experimental fields: field A (a) and field B (b).**

249 **3.1.1 Field A**

250 *3.1.1.1 Experimental operation*

251 For the operation in field A, an AB line was set and set for the navigation system by driving the tractor along
252 the longest edge of the field from one headland to the opposite headland. The operating width was 4.95 m
253 while the turning radius of the tractor was 6 m. The coverage of the field was performed following the
254 continuous fieldwork pattern. Based on the analysis of the GPS recordings (Fig. 12), the measured effective
255 working distance was 32,823 m, the measured non-working headland turn distance was 1,720.2 m and the
256 connection distance of blocks was 112.3 m. The average effective operating speed was 1.2 m/s, while the
257 average turning speed was 0.85 m/s.



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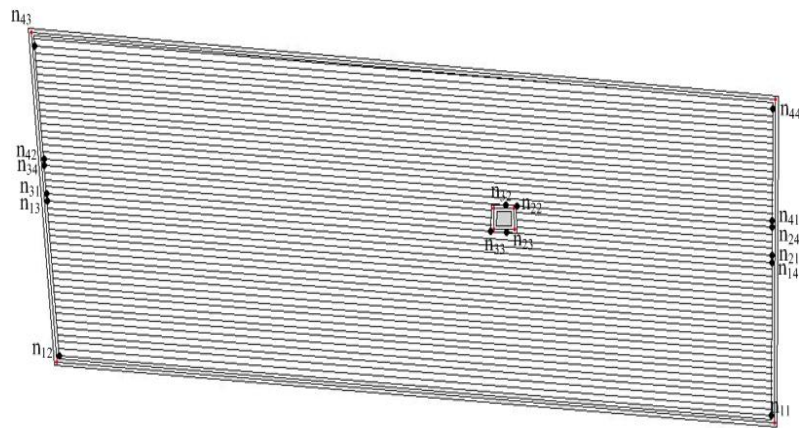
Fig. 12. The GPS recordings of operation in field A

260 *3.1.1.2 Simulated operation*

261 The operating width, the turning radius and the driving direction for the simulated operation were the same
 262 as in the experimental one (4.95 m and 6 m and 143.5° respectively), resulting in 49 tracks and 4 blocks. The
 263 headland passes number was also selected to be 2 as in the actual operation.

264 For finding the shortest connection distance of blocks, the total number of ants, m , was set to 16, while ρ ,
 265 α and β were set to 0.5, 1, and 5, respectively; these values were experimentally found to provide the best
 266 solutions by Colomi (1992). The number of iteration was 200. Ten runs were performed with an average
 267 computational time of 2.92 s.

268 The optimal sequence of the blocks and the corresponding entry and exit nodes was: $\{[n_{11} n_{12} n_{14} n_{13}] \rightarrow [$
 269 $n_{31} n_{32} n_{34} n_{33}] \rightarrow [n_{23} n_{24} n_{22} n_{21}] \rightarrow [n_{41} n_{42} n_{43} n_{44}]\}$. The estimated total effective distance, including the
 270 infield working distance and the working distance in the headlands, during the whole operation was 32,791
 271 m. The estimated non-working headland turn distance was 1,682.5 m. The connection distance of the blocks
 272 was 106.9 m.



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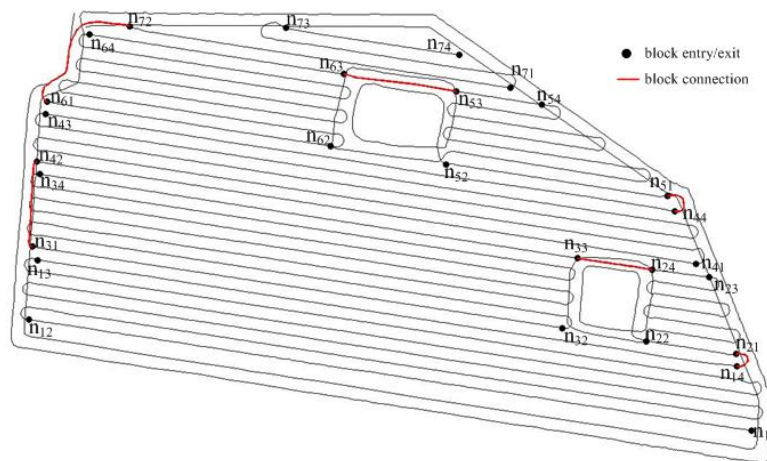
Fig. 13. The generated plan for field A

275 3.1.2 Field B

276 3.1.2.1 Experimental operation

277 In the operation in field B the operating width was 12 m and the turning radius of the tractor was 6.5 m.
 278 Based on the analysis of the GPS recording (Fig. 14), the measured effective working distance was 19,643
 279 m, the measured non-working headland turn distance was 1,370 m and the connection distance of blocks was
 280 450.4 m. The average effective operating speed was 1.5 m/s, while the average turning speed was 0.9 m/s.

281



282

283 Fig. 14. The GPS recordings of operation in field B

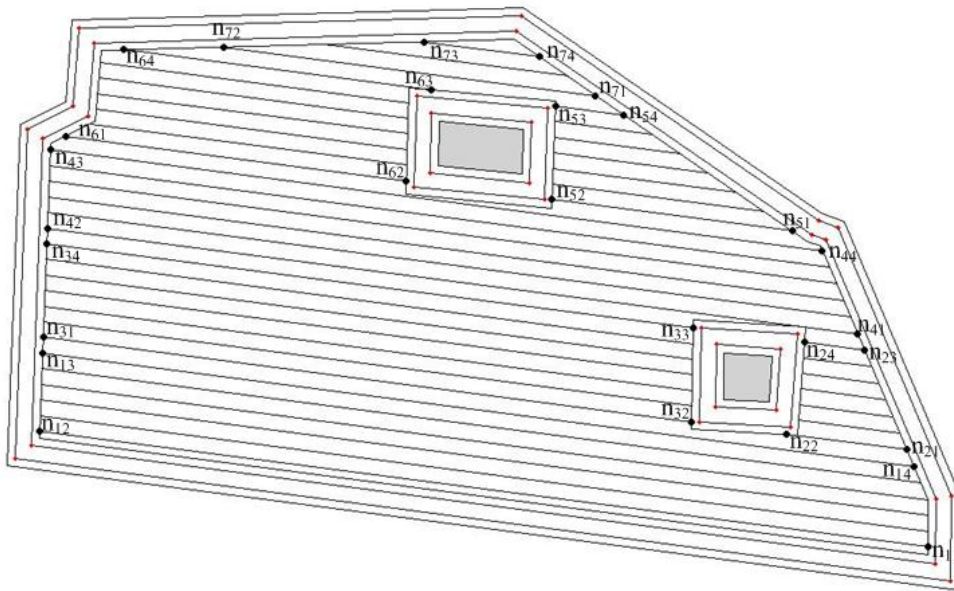
284 3.1.2.2 Simulated operation

285 The operating width, the turning radius and the driving direction for the operation were the same as in the
286 actual operation (12 m and 6.5 m and 172.5° respectively), resulting in 44 tracks and 7 blocks. The headland
287 passes number was set to 2 as in the actual operation.

288 For finding the shortest connection distance of blocks, parameters of the ACO algorithm were set as:
289 $\rho = 0.5, \alpha = 1$, and $\beta = 5$, and the number of iteration was 200. The number of the ants used was 28 which
290 equals to the number of the nodes presenting the entry and exit points of blocks. Ten runs were performed
291 with an average computational time of 11.51 s.

292 The optimal sequence of the blocks and the corresponding entry and exit nodes was:

293 $\{[n_{11} n_{12} n_{13} n_{14}] \rightarrow [n_{21} n_{22} n_{24} n_{23}] \rightarrow [n_{33} n_{34} n_{32} n_{31}] \rightarrow [n_{42} n_{41} n_{43} n_{44}] \rightarrow [n_{51} n_{52} n_{54} n_{53}] \rightarrow [n_{63} n_{64}$
294 $n_{62} n_{61}] \rightarrow [n_{72} n_{71} n_{73} n_{74}]\}$. The estimated total effective distance, including the infield working distance and
295 the working distance in the headlands, during the whole operation was 19,634 m. The estimated non-working
296 headland turnings distance was 1,350.5 m. The connection distance of the blocks was 445.3 m.



297

298 **Fig. 15. The generated plan for field B**

299 **3.2 Comparison between simulated and experimental results**

300 The comparison between the experimentally performed and planned operation and the simulated operation
 301 shows that the developed method can simulate the field operation with sufficient accuracy. As shown in
 302 Table 1, the prediction error in terms of total travelled distance was 0.21% for field operation A and 0.15%
 303 for field operation B. The relatively small errors between the measured and the predicted values of the
 304 operational time elements are mainly arisen from two reasons. First, due to the actual conditions of the field
 305 surface and the positioning error, the vehicle cannot exactly follow the planned parallel tracks. In addition,
 306 the GPS guidance system only navigate on the in-field parallel tracks while the turnings in the headland areas
 307 of the field and the obstacles were manually executed and was depended on the driver’s abilities.

308 **Table 1- Comparison between the data from the experimental and the simulated operations**

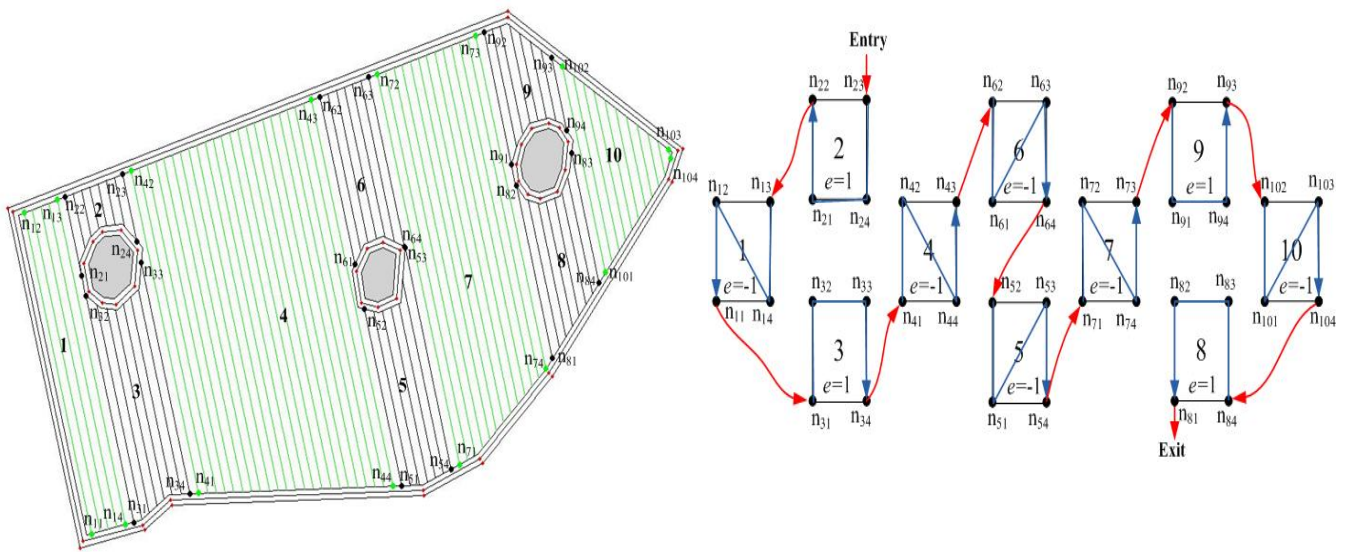
	Operation A			Operation B		
	Simulated (m)	Measured (m)	Error (%)	Simulated (m)	Measured (m)	Error (%)
Total effective distance	32,791	32,823	0.10	19,634	19,643	0.045
Non-working distance	1,682.5	1,720.2	2.23	1,350.5	1,370	1.4
Connection distance of blocks	106.9	112.3	5.05	445.3	450.4	1.14
Total travelled distance	34,580.4	34,655.5	0.21	21,429.8	21,463.4	0.15

309 To test the performance of the ACO algorithm for the solution of the optimization part of the method, an
 310 exhaustive algorithm was used to obtain the optimal block sequence examining all the combinations of the
 311 blocks connections in both cases of field A and field B. The exhaustive algorithm provided the same
 312 solutions as the ACO for both cases. For the field A, the exhaustive algorithm provided the optimal block
 313 sequence in 0.58 s while the ACO algorithm provided the same solution in 2.92 s. However, as the number
 314 of in-field obstacle increased to two in case of field B, the computational time of the exhaustive algorithm
 315 increased to 560.8 s while the computational time for the ACO algorithm was 9.98 s. This was expected

316 since the computational steps and consequently the computational time of the exhaustive enumeration
 317 algorithm increases exponentially with the size of the problem making it unfeasible for medium to large
 318 scale problems (e.g. up to 3-4 blocks).

319 3.3 Simulated test cases

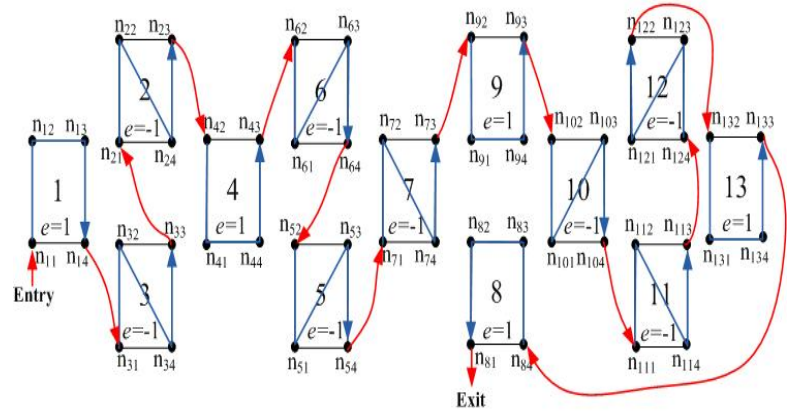
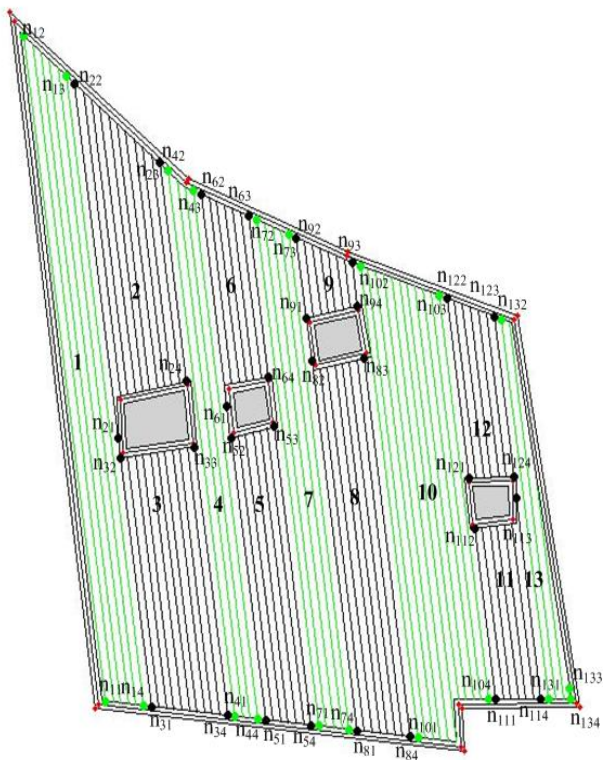
320 In order to demonstrate how the developed method can handle more complicated cases, three fields,
 321 including 3, 4, and 5 obstacles, respectively, were selected. The parameters regarding the input and output
 322 are shown in the Table 2 while the solutions are presented in Fig 16. As expected, the computational time
 323 was increased as the number of obstacles was increased. However, it has to be noted that, regarding the
 324 number of the iterations, as the number of the obstacle increases, more iterations are needed to guarantee
 325 than the best solution can be obtained.



326

327

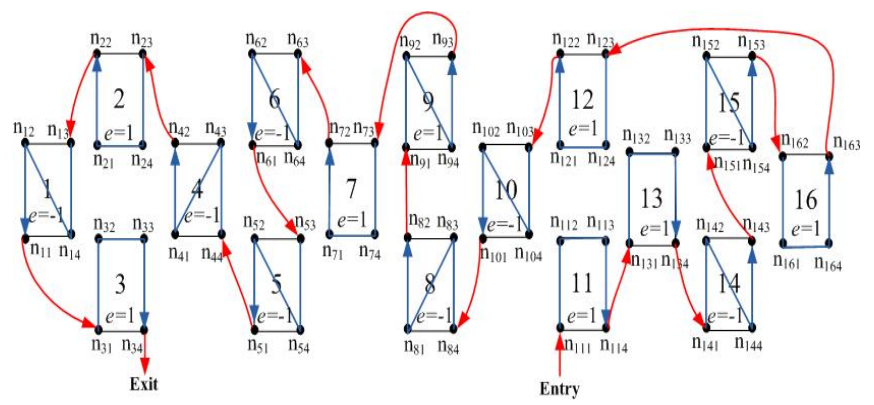
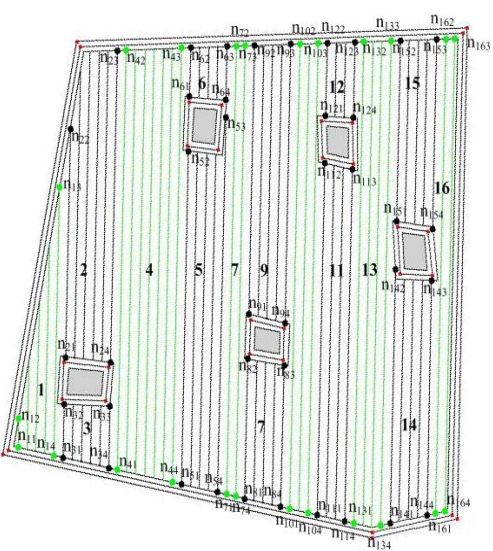
(a)



328

329

(b)



330

331

(c)

332 **Fig.15. The resulted solution of the method for the test cases regarding fields with (a) 3 obstacles, (b) 4**
 333 **obstacles, and (c) 5 obstacles**

Table 2. Parameters and results from the three simulated test cases

Field	(a)				(b)				(c)			
Area(ha)	20.21				56.54				4.81			
Number of obstacles	3				4				5			
Driving angle(°)	105				108.2				31.8			
Operating width (m)	9				12				15			
Minimum turning radius (m)	6				6				6			
Number of headland passes	1				1				1			
ρ	0.5				0.5				0.5			
α	1				1				1			
β	5				5				5			
Iterations	50	100	200	400	100	200	400	600	100	200	400	600
Average processing time (s)	15.2	27.5	55.1	109.3	69.4	118.3	233.7	400.4	123.3	235.5	465.8	697.7
Blocks connection distance (m)	371.5	371.5	371.5	371.5	765.1	765.1	765.1	765.1	856.4	856.4	856.4	856.4
Total effective working distance (m)	21,823				46,020				31,680			
Non-working distance (m)	2,973.9				1,790.7				1,573.2			

335

336 4 Conclusions

337 In this paper, a planning method for simulating field operations in fields with multiple obstacle areas was
 338 presented. The method implies that the field is divided into blocks when considering the in-field obstacle(s)
 339 and the optimal block traversal sequence was formulated as a TSP problem which is solved by applying the
 340 ACO algorithmic approach.

341 The validation of the method showed that it can simulate field operations with sufficient accuracy. Based on
 342 two experimental set-ups, the errors in the prediction of total travelled distance were 0.15% and 0.21%,

343 respectively. Furthermore, the optimization part of the method was validated by compared the ACO
344 algorithm solutions with an exhaustive enumeration algorithm for the small-sized problems included in the
345 two previously mentioned cases.

346 It was also demonstrated that the method can provide feasible solutions for more complicated field
347 operational environments in terms of the number of obstacles included in the field area. Even in the cases of
348 conditions seldom experienced in practice, e.g. involving 5 obstacles, the computational time of the method
349 was less than 700 s.

350 The developed method can be used as part of a decision support system providing feasible field operation
351 solutions in testing different driving directions, operating widths, machine turning radius etc. Furthermore,
352 the method can be incorporated in navigation-aiding systems for agricultural machinery since currently such
353 systems cannot provide a complete route for covering fields that include obstacles.

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