A structure-based approach for ontology partitioning


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Abstract. In this paper, we present a novel structure-based partitioning algorithm opportunely designed to break a large ontology into different modules related to specific topics for the domain of interest. The main idea behind our work is to exploit topological properties of the ontology graph and several techniques derived from Network Analysis to produce an effective partitioning without considering any information about semantics of ontology relationships. Several preliminary experiments conducted to validate the effectiveness of our approach are also reported.

Keywords: Ontology Partitioning, Network Analysis

1 Introduction

With the advent of Semantic Web, an increasing number of ontologies is widely available to formally represent and efficiently use the knowledge related to specific domains. As more and more applications use ontology to represent semantic information, how to support an effective ontology usage is becoming more and more important.

Indeed, the growing size and monolithic nature of these ontologies originate new and previously unexplored problems, such as the difficulty of designing adequate quality control procedures, or scalability, maintenance, reusability and reasoning complexity issues [2].

Since the origins of such problems seem to be reducible to the fact that domain-comprehensive ontologies are just too large to be handled effectively, recent works [3] have suggested to dissemble the overall models into a subset of smaller modules, each focused around a specific sub-topic of interest. Interestingly, while maintaining knowledge of its connection with the other sub-parts of the ontology, each module can easily be used independently from the others, thus providing obvious benefits to the information processing and ontology maintenance burden.
Here we present a method, recently published by the authors in [1], for structure-based partitioning of a large ontology into a set of topic-centered sub-modules. Intuitively a well-built module will contain information about a sub-topic that can stand coherently by itself: the concepts within a module to have strong semantic connections to each other while lacking strong dependencies with information outside the module.

The basic idea behind our work is to convert an ontology into a weighted graph, where certain elements (e.g. subjects, verbs and objects) are nodes, and links between these nodes are derived from the definitions and axioms existing in the ontology. More in details, our method is an attempt to make the partitioning more generic and completely automated, without the need of pre-assigning weights to the relationships typical of each ontology. Working on the ontology graph, we leverage techniques derived from network analysis to identify important concepts in the ontology, evaluate the degree of dependency between these concepts, and therefore find sets of both related and unrelated concepts and finally identify the modules of the original ontology.

The paper is organized as in the following. Section 2 describes the related work on the ontology partitioning problem. Section 3 presents the proposed approach and illustrates the developed partitioning tool. Sections 4 and 5 report the preliminary experimental results and some conclusions and future work, respectively.

2 Related Work

Due to their extensive use in different domains, ontologies have grown into large, complex collections of thousands of concepts [4, 5]. In order to support their maintenance and reusability, it has been recently proposed that the structure of a large ontology should be based on the combination of self-contained, independent and reusable knowledge components (modules). To this goal, modularization techniques to identify significant modules from existing ontologies are becoming essential not just to ontologies’ management, but also to their exploration [6]. In addition, a distributed computing environment could leverage the obtained modules to perform parallelized search or reasoning tasks on the ontology [7].

In this section, we describe recent works related to ontology modularization. Although existing approaches can be divided into several categories [8–10], here we focus on module extraction and ontology partitioning techniques.

The first kind of approach is based on the idea of reducing an ontology (i.e., segmentation or traversal view extraction) to the sub-part that covers a particular sub-vocabulary, related to a specific topic. Following this idea, the authors in [11] use a set of classes of the input ontology and extract related elements on the base of specific properties and restrictions. Noy et al. [12] present Traversal Views as a way of defining an ontology view: a user specifies a subset of an ontology to include in the view by defining the starter concepts, the links to follow from those concepts, and how deep into the ontology the search should go on.
Similarly to [11] and [12], the authors in [13] define a method for the dynamic selection of relevant modules from on-line ontologies. Here, the input sub-vocabulary can contain either classes, properties, or individuals. The mechanism is fully automatized and designed to work with different kinds of ontologies (from simple taxonomies to rich and complex OWL ontologies), and relies on inferences during the modularization process. Finally, in [10], users can extract a module from the original ontology according to a semantic query.

In the second kind of approach, partitioning an ontology corresponds to the process of splitting up the set of axioms into a set of modules \( \{M_1, ..., M_k\} \) such that each \( M_i \) is an ontology and the union of all modules is semantically equivalent to the original ontology \( O \).

In [2] the partitioning is accomplished through the ontology graph structure enriched by assigning different weights to the different relationships. The weighting is performed according to the priority and meaning of the relationships and the random walk algorithm is then adopted to obtain final partitions. Stuckenschmidt and Klein [14] use the previous assumption that dependencies between concepts can be derived from the structure of the ontology. In their approach, an ontology graph is built through the extraction of dependencies resulting from the subclass hierarchy and some additional domain restrictions; then, they exploit connections among nodes to assign the weights. Finally, in order to obtain the final partitioning, they define a modularization algorithm called island based on the minimum cut principle that was implemented in PATO [2].

3 The proposed Ontology Partitioning approach

The aim of this work is to develop a new partitioning technique based on the ontology graph representation. Although there exist several possible representations for an ontology graph, we chose to treat an ontology as a network, where each element of an RDF triple represents a separate node in the graph. Links between nodes are then weighted by computing the related frequency in the graph. We can identify two consecutive steps in our method: ontology graph building (with the edges’ weight computation) and graph partitioning.

3.1 Ontology Graph Building

Let us consider an RDF description of a generic ontology. We suppose that a weighted and directed graph \( G = (V, E, \omega) \) can be extracted from the ontology, where:

- \( V \) is the finite set of the graph vertices - each vertex \( v \) represents an element of the ontology;
- \( E \subseteq V \times V \) is the set of directed edges - two vertices are connected by an edge if the corresponding elements are related within one or more triples in the ontology;
- \( \omega : E \to \mathbb{N}^+ \) is a function assigning a weight \( w_{ij} \) to each edge \( e_{ij} = \langle v_i, v_j \rangle \).
Intuitively, the weight of a connection between two nodes \( v_i \) and \( v_j \) describes the importance of the link from one node to other. Thus, the weight \( w_{ij} \) for the edge connecting two nodes \( v_i, v_j \) is computed as the number of direct relationships \( c \) between the two related ontology elements divided by the maximum number of global relationships shared by each of the two nodes with every other node in the ontology:

\[
\omega_{ij} = \frac{c_{ij} + c_{ji}}{\max\left(\sum_k c_{i,k} + c_{k,i}, \sum_k c_{j,k} + c_{k,j}\right)}.
\]

Thus, we computed the degree of relations between concepts focusing just on the structure of the graph. Note that, according to the previous equation, we need no prior knowledge of the semantics of the relationships between nodes, nor of the strength of the dependencies between concepts in the specific ontology we are partitioning. We can also observe that if in the original ontology there is more than one directed link between two nodes, then these links are combined into a single weighted edge of the graph.

Figure 1 shows how a part of an ontology graph can be generated using the set of triples (in the turtle format) related to the **Kennedy’s Family Ontology**.

![Fig. 1: Example of a graph ontology.](image)

### 3.2 Graph Partitioning

At this point, we want to exploit the weighted graph in order to detect sets of strongly related concepts. To this goal, we use a multilevel \( k \)-way partitioning schema to compute \( k \) partitions through edge-cut minimization - meaning that we search for a partitioning such that the number of edges (or, in case of a weighted graph, the sum of their weights) crossing different partitions is minimized. The \( k \)-way partitioning is well suited for our needs, determining sets of concepts that present strong internal connections and weak external ones.

For the implementation, we leverage the **METIS** libraries. However, while METIS expects the number of modules the graph has to be partitioned into to

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1 The Kennedys Ontology is available at http://topbraid.org/examples/kennedys

2 http://glaros.dtc.umn.edu/gkhome/metis/metis/overview
be known, we want to obtain such number based on ontology features. Thus, we implemented a recursive procedure using METIS partitioning method to iteratively increase the number of modules (starting from an initial value \(k\) which depends from the number of the ontology’s concepts).

The partitioning procedure aims at minimizing both the bulkiness of each module \(M_i\) and its related connectedness as suggested in [16] using a proper heuristics.

Exploiting these optimization criteria, we define the bulkiness value for each module \(M_i\) as: \(\text{bulk}_i = \frac{1}{2} - \frac{1}{2} \cos(\pi \cdot \frac{n_i}{n})\), \(n\) being the number of nodes and \(n_i\) the number of nodes of a module \(M_i\).

Similarly, we define the connectedness of a module \(M_i\) as the number of edges connecting \(M_i\) to other modules divided by the total number of edges in that module: \(\text{conn}_i = \frac{\#\{(v, v') \in M_i | M(v) \neq M(v')\}}{\#\{(v, v') \in M_i\}}\), where \((v, v')\) is an edge of the graph connecting nodes \(v\) and \(v'\), and \(M(v)\) returns the module which the vertex \(v\) is assigned to.

The number of actual elements in each module can be deduced by the number of the corresponding vertices. Eventually, a label can be associated to a module considering the label of the vertex having the highest betweenness: \(\text{betw}(v) = \sum_{s,t,v \in V, s \neq v \neq t} \frac{e^*_st(v)}{e^*_st}\), where \(s, t, v \in V, s \neq v \neq t\) and \(e^*_st\) is the number of shortest paths between \(s\) and \(t\), passing through \(v\).

### 3.3 The Partitioning Tool

The partitioning procedure described in the previous section was implemented through JAVA. Figure 2 shows an outline of the overall system architecture and of the related workflow.

![Fig. 2: Partitioning Tool Architecture](image)

As shown in Figure 2, the first step is to generate a graph structure from an ontology input file. Such a structure can then be used as input for METIS.
To such a goal, we exploit the Jena\(^3\) to convert ontologies represented in the form of OWL, RDF or other RDF serialization formats in set of triples (stored in a RDBMS) and successively into the related ontology graph.

Then, the iterative approach we previously introduced is used to weight the graph generated by Jena and partition it into modules. Finally, to efficiently analyze the results of the partitioning, we need to visualize the original graph and modules into which it was divided. To this aim, we used both Jung API\(^4\) and Pajek\(^1\) visualization tool.

4 Preliminary Experimental Evaluation

In order to evaluate the quality of our partitioning method, we discuss in this section a preliminary experimental set-up conducted on the Kennedy’s Family ontology\(^5\) and presented by the authors in a previous work\(^1\).

Given the ontology and the modules derived from it through the partitioning procedure, we adopted both an empirical\(^6\) and a criteria-based\(^7\) evaluation to determine the quality of partitioning.

First of all, we collected a number of students and we made them analyze the Kennedy’s ontology in order to build what we will consider the optimal partitioning of the ontology\(^8\). Then, we defined three similarity measurements: precision, recall and F-Measure. These measures are based on the numbers of intra-pairs, which are pairs of concepts (subject-verb or verb-object) belonging to the same module.

More formally:

- **Precision**: is the ratio of intra-pairs in the generated partitioning that are also intra-pairs in the optimal partitioning.
- **Recall**: is the ratio of intra-pairs in the optimal partitioning that are also intra-pairs in the generated one.
- **F-Measure**: is a value used to point out the overall quality results.

In Table 1, we compared the obtained results with a partitioning performed by PATO\(^9\).

The problem of the empirical evaluation is to obtain a reliable optimal partitioning to be used as comparison when we face the analysis of large and complex

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\(^3\) http://jena.apache.org/
\(^4\) http://jung.sourceforge.net
\(^5\) The ontology consists of 619 triples, amounting to a total of 282 nodes and 748 edges.
\(^6\) A partitioning generated using our automatic tool is evaluated against a ground truth partitioning built by human experts, in terms of recall and precision.
\(^7\) The partitioning quality is evaluated according to some criteria which can be classified as logic-based, structural and application-dependent.
\(^8\) Humans identified three main sub-topics around which the analyzed ontology is focused: Professional Career, Vital Statistics and Degree if Kinship.
\(^9\) http://web.informatik.unimannheim.de/anne/Modularization/pato.html
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<table>
<thead>
<tr>
<th>Precision</th>
<th>Recall</th>
<th>F-Measure</th>
</tr>
</thead>
<tbody>
<tr>
<td>PATO</td>
<td>53.84%</td>
<td>50%</td>
</tr>
<tr>
<td>Proposed Approach</td>
<td>88.2%</td>
<td>91.4%</td>
</tr>
</tbody>
</table>

Table 1: Precision and Recall Comparison

ontologies. However, it is possible to rely on an alternative method exploiting criteria descriptive of the quality of the given partitioning. In our evaluation, we used the parameter of global connectedness again defined in [16]10.

Again, we compared the results with those obtained by PATO. The modules produced by PATO vary significantly in size, the connectedness values of the modules are heavily variable and the value of global connectedness is significantly higher than our method’s one as specified in the Table 2.

<table>
<thead>
<tr>
<th>Proposed Method</th>
<th>PATO</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of Modules</td>
<td>3</td>
</tr>
<tr>
<td>Number of Nodes</td>
<td>282</td>
</tr>
<tr>
<td>Smallest Module Size</td>
<td>16</td>
</tr>
<tr>
<td>Largest Module Size</td>
<td>65</td>
</tr>
<tr>
<td>Global Connectedness</td>
<td>1.01</td>
</tr>
</tbody>
</table>

Table 2: Structural Comparison

5 Conclusions and Future Work

In this paper we described a method for structure-based ontology partitioning. The main idea of our approach is to translate the structure of an ontology into a weighted graph and to break it into a set of modules which have strong internal connections and weak external ones.

A preliminary experimental evaluation was conducted on the Kennedy’s Family ontology. The results were validated by comparing them both with a ground truth generated by humans and with the results obtained by PATO partitioning tool. The obtained results were encouraging both in terms of precision and recall, and of internal coherence of the obtained modules. Future work will be devoted to improve the quality of the partitioning, for example employing other graph partitioning techniques, and to extend our experiments using larger ontologies.

References


10 The global connectedness is defined as the fraction of inter-modules edges compared to the total number of edges in the ontology graph.


