Reaction between propargyl radical and 1,3-butadiene to form five to seven membered rings. Theoretical study

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REATION BETWEEN PROPARGYL RADICAL AND 1,3-BUTADIENE TO FORM FIVE TO SEVEN MEMBERED RINGS. THEORETICAL STUDY.

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Abstract.

Propargyl radical addition to 1,3-butadiene seems to be a promising channel to form 5-, 6-, and 7-membered rings. These are important steps in the growth of polycyclic aromatic hydrocarbons and soot platelets. The reaction mechanism, involving 97 intermediates and 115 transition structures, was studied by CBS-QB3 method (reported here) and density functional theory. All these structures were included in the subsequent RRKM study at different combustion pressures (P=30-0.01 atm) and temperatures (T=1200-2100 K). At P=30 atm, open-chain products dominate in the whole range of temperatures. The importance of 5- and 6-membered rings rises with T, reaching a maximum in the T range 1500-1800 K. A more modest yield in 7-rings is present at T= 1500 K. At P=1 atm, in the range 1200-1500 K, the yield in 5- and 6-rings dominate. 5- and 6-rings yields are about 41% at 1200 K (CBS-QB3 data). At P=0.1 atm, 6-rings become the main products a 1000 K (35%), then they decrease to 12% (2100 K) and 5-rings rise up to 44% (1200 K), then decrease to 14% (2100 K). Open-chains are the main products at T<1000 K and T > 1500 K. Then, at P=0.01 atm, open-chain products are important below 900 K and above 1500 K,6-rings are main contributors between 900 K and 1500 K. 6-Rings reach a maximum yield of 47% (1200 K) and 5-rings 44% (1200 K) and 7-rings 17% (900 K). The main products form through to H losses.

Keywords: 1) PAH formation; 2) first C-ring; 3) propargyl; 4) 1,3-butadiene; 5) RRKM; 6) CBS-QB3; 7) Density Functional Theory

Running Title: Ring closures in propargyl + 1,3-butadiene

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1. Introduction

Particulate is a major contribution to the overall mass of atmospheric aerosol, and PAHs exhibit an ubiquitous presence. The impact of carbonaceous particulate[1,2] and polycyclic aromatic hydrocarbons (PAHs) on the environment is significant.[3,4] PAHs and amorphous carbon have been also identified in planetary atmospheres,[5,6] in the envelopes of carbon-rich stars,[6–9] and in the interstellar medium.[10] Graphene sheets and graphene nanoribbons are also interesting from a technological point of view.[11–15] PAHs are considered as soot precursors,[16,17] by sharing the same origin.[18–22] We have studied theoretically the growth of an aromatic system adsorbed on a model soot platelet[23] and the feasibility of van der Waals associations and σ bond formation between PAH-like molecules as a function of temperature.[24,25] Formation of aromatics, in particular the first ring, and soot particles, have been reviewed and discussed by Richter and Howard in 2000,[26] and by Frenklach in 2002.[27] The first ring formation has been studied both experimentally and computationally. Investigations have involved cyclopentene flame,[28] 1,3-butadiene + C₂[29] and C₂H[30] reactions. Bittner and Howard have suggested benzene formation via the butadienyl plus ethyne reaction.[31] Similar mechanisms (vinyl addition to ethyne, or to but-1-ene-3-yne) has also been proposed by the same groups.[32–35] Jones et al. proposed barrierless reactions of ethynyl radicals with substituted 1,3-butadiene molecule to form benzene in the interstellar medium.[36] We have previously studied[37] the first growth steps of aromatic systems through radical-breeding mechanism proposed by Krestinin,[38–40] and by radical addition of propargyl to But-1-ene-3-yne.[41]

The propargyl has been considered a species capable of generating aromatics through self-addition: recombination of two propargyl radicals can be the dominant pathway to benzene and phenyl formation.[35,42–47] It plays also an important role in the hydrocarbon growth process: for instance, the kinetics of the reaction between the propargyl radical and ethyne[48,49] and butadiyne[50,51] has been investigated both experimentally and theoretically. Similar reaction, the thermal decomposition of benzyl radical has been also computationally investigated.[52]

Butadiene has also been considered important in combustion and astrochemistry and C₂H + 1,3-butadiene reaction has also been recently investigated both theoretically and experimentally.[30]

Both the propargyl radical and 1,3-butadiene have been measured in molar fractions x, in the ranges x = 2–3 x10⁻³ and 8 x10⁻⁵– 6 x10⁻³, respectively.[53] They have been detected in premixed ethyne,[54] benzene,[55] toluene,[56] or gasoline[57] flames. Propargyl radical has also been detected in molar fraction up to x = 1 x 10⁻³ or 2.4 x 10⁻⁴ in low-pressure flames.[58,59]
In this paper we explore the possible formation of 4-, 5-, 6-, or 7-membered ring intermediates, which could be involved in subsequent PAH growth processes under combustion conditions. We simulate also the effect of four pressure values (30, 1, 0.1, and 0.01 atm): the highest pressure value could be related to internal combustion engine,[60,61] while the low pressure data could be pertinent to low-pressure flames.[59,62–68] The reacting system examined is defined by the radical addition of propargyl to 1,3-butadiene (Chart 1).

![Chart 1](image)

**2. Theoretical Method**

The high-level composite method CBS-QB3[69,70] was used to study the energy hypersurface. All stationary points were determined by gradient procedures[71–75]. The nature of the minima and first order saddle points was confirmed by vibrational frequency analysis. The CBS-QB3 energies including zero point vibrational energies (ΔE_{ZPE}) are reported throughout in the text.

For comparison purpose, all the critical points were also optimized at the DFT[76] level, by using the M06-2X functional.[77–80] The cc-pVTZ basis set[81] was used in these optimizations. The optimizations were followed by cc-pVQZ[82] single-point energy calculations, to finally obtain M06-2X/CBS (complete basis set) energy estimates through the extrapolation formula put forward by Halkier et al.[83]. A validation of the computational level adopted in this study was done in a previous study.[41] The DFT energies are reported in the Supplementary Material.

Geometry optimizations and thermochemistry calculations were carried out by using the Gaussian 09 system of programs.[84]

The Rice Ramsperger Kassel Marcus (RRKM) theory,[85,86] was then used to obtain the distribution of the reaction products. In order to obtain these distributions as functions of time, RRKM and Master Equation calculations (RRKM-ME) were carried out by using the MultiWell program suite.[53,87–89] It allows to calculate sum and densities of states, then assesses micro-canonical rate constants according to RRKM theory, and finally solves the master equation. Corrections for quantum tunneling were included for all hydrogen transfer reactions (not H dissociations) by incorporating the contributions for one-dimensional
unsymmetrical Eckart barriers. [90] MultiWell stores densities and sums of states in double arrays: the lower part of the array consisted of 600 array elements, which range in energy from 0 to 2995 cm\(^{-1}\). The higher energy part of the double array consisted of 600 elements ranging in energy from 0 to 150000 cm\(^{-1}\) with an energy spacing of 250.4 cm\(^{-1}\). The Lennard-Jones parameters necessary for the collision frequency calculations were assumed to be the same for all the structures, and were: \(\sigma = 5.9\ \text{Å}\), and \(\varepsilon/k_B = 410\ \text{K}\). Energy transfer was treated by assuming the exponential-down model for collision step-size distributions: \(E_{\text{down}} = 2000\ \text{cm}^{-1}\), independent from the temperature. [52,91] This value was found to accurately reproduce the experimental falloff behavior for decomposition of benzyl radical with a good agreement between calculations and experimental data across the temperature range 300-3000K. [52]

Low-frequency modes were treated as harmonic oscillators. Rate constants were calculated in the range 1200-2100 K. In the present work, the number of stochastic trials was set to \(10^7\) for 300 collisions. Simulations were carried out for combustion temperatures, at different pressures (of \(N_2\) buffer gas), namely at \(P = 0.01, 0.1, 1,\) and 30 atm, to simulate combustions under low, normal, and high pressure conditions. Low-pressure flames are oftentimes preferred because of their nearly one dimensional structure and extended reaction zone. [59,62–68]

### 3. Results and discussion

#### 3.1 Potential energy surface

Four entrance channels are conceivable: they are due to the addition of each of the external carbons (1 and 3) of the delocalized propargyl radical (a) to the positions 1 and 2 of 1,3-butadiene (b) (Chart 1). The propargyl additions to the external carbons of 1,3-butadiene have lower energy barriers compared to the additions to the internal carbons (Table 1), and their adducts are more stable because the possibility of delocalization of the unpaired electron. Making reference to the reagents, the adducts are located at -22.1 (1), -6.1 (2), -23.1 (3), -7.2 (4) kcal mol\(^{-1}\), respectively.

<table>
<thead>
<tr>
<th>Channel</th>
<th>barrier</th>
<th>adduct</th>
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<tr>
<td>1</td>
<td>5.7</td>
<td>-22.1</td>
</tr>
<tr>
<td>2</td>
<td>11.1</td>
<td>-6.1</td>
</tr>
<tr>
<td>3</td>
<td>7.8</td>
<td>-23.1</td>
</tr>
<tr>
<td>4</td>
<td>13.6</td>
<td>-7.2</td>
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Table 1. Entrance channels: $\Delta E_{ZPE}$ (kcal mol$^{-1}$)

barriers and adduct for the initial radical additions.

The reaction pathways that start from 1-4 are shown in Schemes 1-3. Because of the complexity of the system, the reaction mechanism (entailing 97 intermediates and 115 transition structures) has been necessarily split in three schemes, and red numbers in each scheme indicate connections to another scheme. Due to the complexity of the reaction mechanism, the numeric labels will be often mentioned not sequentially. The bold lines in Scheme 1-3 show the favorable routes leading to the most abundant products: the complete list of all the products and their yields is reported in Section 2 of the Supplementary Material. Other connections between the intermediates could be conceivable, but we arbitrarily chose to neglect transition structures with energies above 20 kcal mol$^{-1}$ with respect to reactants.

The four initial adducts 1-4 are interconnected: 1 (Scheme 1) and 4 (Scheme 3) are connected through the intermediate 37. Initial adducts 2 and 3 through structure 39 (Scheme 2). All the above-mentioned steps involve fairly moderate energies (up to 12 kcal mol$^{-1}$ above the reactants). On the other hand, connection between 1-3 or 2-4 is much more indirect (1-12-38-50-3 and 2-39-3-40-4, respectively).

In Scheme 1 the most stable intermediate is the 7-ring 8 at -60.6 kcal mol$^{-1}$ with respect to the reactants. It is formed starting from 1, by cyclization (5), then ring opening (6) followed by another cyclization (7). However, the H migration 7-8 involves a high barrier (21.0 kcal mol$^{-1}$) and in case the system was thermalized, this barrier could be demanding enough to make the formation of the 8 (and 9) difficult (see section 3.2).

Other important structures are the 5-rings due to H losses 18, 30 and 31. These H losses have high barriers but they are irreversible and they possibly “pump away” from the C$_7$H$_8$ system.

In Scheme 2 the most relevant structures are the 5-ring 70, and the 6-rings 44, 47 and 55, formed by H losses. All the products are formed from 2 or 3, by passing through several intermediates which, in some case, involve moderate barrier heights.

From 4 (Scheme 3), after ring closure and H loss, the most promising products are the 6-rings 47 and 87, and the 5-rings 78 and 84: the barrier could be fairly high (e.g. 32.6 kcal mol$^{-1}$ for the step 46-47, and 32.0 kcal mol$^{-1}$ for 77-78), but the relative energies are well below the limit of the reactants (e.g. -11.8 kcal mol$^{-1}$ for the step 46-47, and -7.4 kcal mol$^{-1}$ for 77-78).

H losses from the initial adducts lead to open-chain stable structures (93-96), characterized by high energy barriers (18-26 kcal mol$^{-1}$ with respect to the reactants) and high exothermicity (16-24 kcal mol$^{-1}$), but they are favorable in terms of entropy.

The energy profile leading to the most important products, according to the RRKM (see session 3.2), are shown in Figures 1 (a-e).
Scheme 1. Pathways toward 4-rings, 5-rings, 6-rings, and 7-rings intermediate structures that appear more promising on the basis of $\Delta E_{ZPE}$ values. The bold figures are the labels of the structures, whereas the other values are $\Delta E_{ZPE}$ energies expressed in kcal mol$^{-1}$. Box highlights the initial adduct 1. The red labels are relative to structures connecting Scheme 1 to Schemes 2 and 3. The blue structures are the most abundant products, according to RRKM simulations. The bold lines show the favorable routes. The arrows do no indicate how the equilibrium is shifted, but only connections among intermediates.
Scheme 2. Pathways toward 4-rings, 5-rings, 6-rings, and 7-rings intermediate structures that appear more promising on the basis of $\Delta E_{ZPE}$ values. The bold figures are the labels of the structures, whereas the other values are $\Delta E_{ZPE}$ energies expressed in kcal mol$^{-1}$. Box highlights the initial adducts 2 and 3. The red labels are relative to structures connecting Scheme 2 to Schemes 1 and 3. The blue structures are the most abundant products, according to RRKM simulations. The bold lines show the favorable routes. The arrows do no indicate how the equilibrium is shifted, but only connections among intermediates.
Scheme 3. Pathways toward 4-rings, 5-rings, 6-rings, and 7-rings intermediate structures that appear more promising on the basis of $\Delta E_{ZPE}$ values. The bold figures are the labels of the structures, whereas the other values are $\Delta E_{ZPE}$ energies expressed in kcal mol$^{-1}$. Box highlights the initial adduct 4. The red labels are relative to structures connecting Scheme 3 to Schemes 1 and 2. The blue structures are the most abundant products, according to RRKM simulations. The bold lines show the favorable routes. The arrows do not indicate how the equilibrium is shifted, but only connections among intermediates.
Ring closures in propargyl +1,3-butadiene

Δ$E_{zpe}$ / kcal mol$^{-1}$

(a)  

(b)  

(c)
Figure 1. Pathways toward the main products. $\Delta E_{ZPE}$ values referred to the reactants (propargyl radical + 1,3-butadiene).

3.2 Master equation simulations.

The yields calculated for each of the four entrance channels (in 4 separate simulations) were scaled by the branching ratio (Section 1 of the Supplementary Material). Only for the four initial transition structures the symmetrical hindered rotation approximation was used to have a better estimate of the branching ratio. Then the total yields were calculated by summing up the four weight-averaged channels. RRKM-ME simulations show that the back-reaction to the original reactants could be significant. It more easily occurs at high temperature and low pressure. Since this effect is not observable in the experiments,
the computational results reported in this paper have been corrected for it and the net product reaction yields reported in Figure 2 exclude the re-dissociation to the initial compounds. However, for sake of clarity, the back dissociation fractions are also reported in the Figure 2, where they are referred to the same ordinate axis, but stand alone (have not to be summed up with the rest). We have estimated the net product reaction yields at four pressure values: P = 30, 1, 0.1, and 0.01 atm.

At P = 30 atm (Figure 2a), up to 1500 K, the main products are the open-chain intermediates in all the range of temperatures. Until 1500 K the most abundant is 1, followed by 3. Above 1500 K the main products are 93, followed by 95. The reason of this trend is a dual contribution: at low temperature the products due to the thermalization prevail; at high temperature the H losses from the initial adducts become more and more important. Plots with these two separate contributions to the open-chain yields are reported in the Section 2 of the Supplementary Material.

At intermediate temperatures (1200-1500 K) the importance of 6- and 5-rings grows up to about 28 and 21% respectively, then it decreases to about 12-14% at 2100 K. The 5-rings formed are mainly 78, but also 30, 31, and 18 in different ratio, depending on the temperature, whereas the 6-rings are 47, 87, and 5. 4- and 7-rings formation is non-negligible only in the range 1200-1800 K: the maximum yield is \( \approx 7\% \) and 4% respectively at 1200 and 1500 K. 7-Rings are entirely constituted by the 7 intermediate. Rate constants are reported in the Section 3 of the Supplementary Material.

At P=1 atm (Figure 2b), open-chain structures are the most important contribution below T=1100 K and above 1500 K. In the intermediate range of temperatures (1100-1500 K) the yields in 5- and 6-rings dominate. The yield in 6-rings (mainly 47 and 87, and in minor extent 5, 45, 88) rises to 41% at 1200, and then decreases to 12% at 2100 K. The yield in 5-rings (30, 31, and 78) increases from 2% at 900 K to 41% at 1200 K, and then it decreases similarly to 6-rings. 7-Ring formation (7) is relevant only above 900 K and below 1500 K (maximum 5% at 1200 K).
Ring closures in propargyl +1,3-butadiene

![Graph a](image-a)

![Graph b](image-b)
Figure 2. Net product reaction yields, at \( P = 30 \text{ atm} \) (a), \( 1 \text{ atm} \) (b), \( 0.1 \text{ atm} \) (c), and \( 0.01 \text{ atm} \) (d). The grey dashed lines (which stand alone) indicate the back dissociations to the reactants.

At \( P=0.1 \text{ atm} \) (Figure 2c), open-chain products are important below 1100 K (1 and 2) and above 1500 K (93 and 95). The 5- and 6-rings become the main products at 1200 K: 5-ring yield reaches 44\% (30, 31, 78, and 18), and 6-ring 47\% (47, 87, and 45). At higher temperatures their yields decrease to 14 and 12\%, respectively (2100 K). The 4- and 7-rings contribution is below 8\% over all range of T.
Then, at P=0.01 atm (Figure 2d), the behavior is similar to Figure 2c, with the exception of 7-ring (7), 6- and 5-rings yields which are higher at 900 K. 6-Rings become the most abundant products between 800 and 1500 K, reaching a maximum (47%) at T= 1200K. At higher T, their contribution remains important, and similar to the 5-rings contribution. The maximum 5-rings yield is 44% at T=1200 K. 7-Rings are relevant only when T is around 900 K (17%)

All the 5 and 6-rings formed during the reaction are almost exclusively products due to H loss. 7 is the only contributor to 7-rings, and 56 is the 4-ring product.

Pressure increase affects the products distribution: at lower pressure and lower temperatures the amount of open-chain products drops in favor of 5-, 6- and 7-rings formation (Figure 2). At higher temperatures they always prevail. 4-Rings yield remains below 9% in all range of temperatures and pressures.

3.3 Comparison with the DFT computations.

The 4 initial transition structures (the additions of propargyl radical to 1,3-butadiene) are 1.5-2 kcal mol\(^{-1}\) higher at M06-2X (7.2, 12.6, 9.8, 15.4 kcal mol\(^{-1}\) for 1, 2, 3, and 4 formation, respectively) than at CBS-QB3 level, and the resulting rate constants are lower by a factor of 5 (600 K) to 1.2 (2100 K). Several 6-rings (53, 54, 55, 59, 60) and some other intermediates (40, 90, 91) are 4-9 kcal mol\(^{-1}\) more stable when calculated by the M06-2X functional. However, in general, the DFT and CBS-QB3 energies are similar: the mean-squared deviation is -0.62 kcal mol\(^{-1}\); mean-unsigned deviation 1.82; root mean square deviation 2.32.

The products distribution, estimated by kinetic simulations, shows similar trends with temperatures and pressures, but the yields are in some cases significantly different. This gap is especially evident at low pressures (0.01 and 0.1 atm) and low temperature (900 K): at 0.01 atm the 5-rings yield drops from 30% (CBS-QB3) to 10% (M06-2X/CBS) and, specularly, the open-chain products grow from 10% (CBS-QB3) to 27% (M06-2X/CBS). Similarly, at 0.1 atm, the 6-rings yield grows from 19% (CBS-QB3) to 38% (M06-2X/CBS), with a reduction of the open-chain products from 61% to 51%.

A sensitivity analysis has been carried out on the CBS-QB3 kinetic simulation, at 0.01 atm and 900 K, by increasing by 5% the barrier heights of first steps of the reaction (1-0, 1-5,1-12, 1-37, 5-42, 3-39, 3-56, 3-95, 3-40, 3-0), one by one. Changing the barrier of the step 1-0 (the back dissociation) by 1.4 A, entails a variation of -108%, -94%, -23% and +224% of the 5-, 6, 7-rings and open-chain yields, respectively. Also the barrier increase of the 1-5 step produces large changes of the yields: +73%, -21%, -23% for 5-, 6, open-chain, respectively. For 1-12 and 1-37, the variations are smaller, around 20%. On the other hand, the reactions from intermediate 3 do not show significant effect on the products distribution. The
discrepancies between CBS-QB3 and M06-2X kinetic simulations could be reasonably ascribed to the small differences of the energy barriers of the first reaction steps.

The M06-2X results are reported in Sections 5-8 of the Supplementary Material.

4. Conclusions

The propargyl radical and 1,3-butadiene have been detected in significant molar fractions in flames. The reaction pathways between the two molecules to form 4-, 5-, 6-, and 7-membered carbon rings under combustion conditions have been investigated first at the DFT level. These rings can be considered as precursors of larger polycyclic systems. Several pathways, leading to 4-, 5-, 6-, and 7-rings, result promising when $\Delta E_{ZPE}$ is considered.

However, a Master Equation/RRKM study, carried out at different temperatures and pressure, has shown which products are more likely formed.

The open-chain products dominate at the lower and higher temperatures. 1 and 3 are the most abundant open-chain products at low temperature, and 93 and 95 at high T. 5- and 6-membered rings show a similar behavior with T: they grow with T and prevail starting from 900-1000 K (at 0.01 atm) or 1100 K (at 1 atm) to 1500 K. 5-Rings (18, 30, 31, 78) and 6-rings (5, 45, 47, 87, 88) reach a maximum yield at 1200 K (0.01, 0.1 and 1 atm) or 1500 (30 atm) then they decrease but still remaining significant to the total observed products. Most of the prevailing products form through H losses. 7-Rings (7) show a trend with maximum yields depending on the pressure: at 30 atm is located at 1500 K whereas at 0.01 atm is at 900 K. These yields range from 4% (30 atm) to 17% (0.01 atm). 4-Rings (56, and 73) are minor products and their yields range from 5% (0.01 atm) to 9% (1 atm).

In conclusion, the propargyl radical plus 1,3-butadiene reaction seems a promising way to form cyclic carbon systems of different extension.

Acknowledgments. This work was conducted in the frame of EC FP6 NoE ACCENT and ACCENT–PLUS projects (Atmospheric Composition Change, the European NeTwork of Excellence).

Supplementary Material includes geometries, energetics, vibrational frequencies, moments of inertia of all the structures; branching ratio; product distributions and rate constants; DFT energetics and product distributions.
Ring closures in propargyl +1,3- butadiene

References


Ring closures in propargyl +1,3-butadiene

References:


[53] Maximum mole fractions reported are: ref. 43: 8.2 x 10-5 (1,3-butadiene) and 2.1 x 10-3 (propargyl) ref. 44: 1.5 x 10-3 (1,3-butadiene) and 2.4 x 10-3 (propargyl) ref. 45: 4.2 x 10-4 (1,3-butadiene) and 2.8 x 10-3 (propargyl) ref. 46: 5.76 x 10-3 (1,3-but, (n.d.).


Ring closures in propargyl +1,3-butadiene


