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# Itinerant magnetism, electronic properties and half-metallicity of $\text{Co}_2\text{ZrSn}$ and $\text{Co}_2\text{HfSn}$ Heusler alloys

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Half-metallic ferromagnetic alloys are attracting considerable interest for their potential applications in spintronic devices. Co-based Heusler alloys are considered to be promising half-metallic compounds as they combine suitable magnetic, electronic and transport properties with compositional versatility and high thermal stability. In this work,  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  Heusler alloys were studied by combining experimental and ab-initio investigations in order to accurately estimate their electronic density of states in proximity of the Fermi level and to determine their magnetic and electronic properties. Magnetization measurements, performed between 2 K and 550 K, suggest for both alloys a gradual transition from localized ferromagnetism to weak itinerant ferromagnetism with increasing temperature, well described by a simple mean field model up to the Curie temperature (454 K in  $\text{Co}_2\text{ZrSn}$  and 432 K in  $\text{Co}_2\text{HfSn}$ ) and beyond. Ab-initio calculations were performed using two exchange-correlational functionals, PBE and PBE optimized for solids (PBEsol), in order to assess the reproducibility of theoretical results. Overall, band structures and density of states (DOS) diagrams indicated, for both compounds, the presence of a half-metallic band gap in the minority spin sub-band. The dependence of magnetic moments and band gap width on cell parameters is discussed in detail. Calculated magnetic moments and cell parameters satisfactorily match the experimental results obtained in this work and previously reported in the literature.

## 1. Introduction

The interest for spintronics has rapidly grown in recent years [1,2], and generation and transport of spin-polarized currents has become a decisive topic for developing suitable devices [1–4], actively stimulating research on compounds which show half-metallic properties. Among several materials [5–7], Heusler alloys, defined as ternary intermetallic compounds of  $\text{X}_2\text{YZ}$  (X, Y are transition metals, Y is a p-group element) composition and  $\text{L}_{21}$  space group, proved to be good candidates for spintronic applications, as they show high Curie temperature ( $T_C$ ) and high spin-polarization, related to a remarkable half-metallicity [8–10]. In half-metallic Heusler alloys, the magnetization ( $M$ ) is predicted to follow the Slater-Pauling rule, namely the total magnetic moment per formula unit scales with the number of valence electrons ( $Z$ ) as  $M_{tot} = Z - 24$ . Deviations from this behavior are expected for non-perfect half-metallicity [11]. Notably, Co-based Heusler alloys were found to be suitable for spin-injection processes [12] and progressively became the focus for prospective spintronic devices operating close to room temperature. Half-metallicity was indeed reported for compounds like  $\text{Co}_2\text{FeAl}_{0.5}\text{Si}_{0.5}$  [13],  $\text{Co}_2\text{Cr}_{0.6}\text{Fe}_{0.4}\text{Al}$  [14],  $\text{Co}_2\text{MnSi}$  [15],  $\text{Co}_2\text{CrAl}$  [16],  $\text{Co}_2\text{FeSi}$  [17],  $\text{Co}_2\text{V}(\text{Al},\text{Ga})$  [18,19], and  $\text{Co}_2(\text{Ti},\text{Hf})(\text{Si},\text{Ge},\text{Sn})$  [20,21]. Since the development of spin-voltage generators is regarded as crucial in spintronics [22,23], thermoelectric properties are also of high interest for these applications, having been proved spin-Seebeck effect to be an effective way to generate and carry spin-polarized current over relatively long distances [24]. Therefore, half-metallic alloys which show a constant, relatively large Seebeck coefficient (when compared with other thermoelectric materials [25]) and a high Curie

temperature  $T_C$  (possibly above room temperature) are greatly looked after [26]. Co-based Heusler compounds like  $\text{Co}_2\text{Ti}(\text{Si},\text{Ge},\text{Sn})$  and  $\text{Co}_2(\text{Zr},\text{Hf})\text{Sn}$  have been reported to satisfy these requirements quite well [20,27]. A distinctive feature of  $\text{Co}_2(\text{Zr},\text{Hf})\text{Sn}$  alloys is the fact that both compounds crystallize directly from the melt in the  $L2_1$  structure [27], whereas the formation process of many other previously mentioned Co-based Heusler alloys, such as  $\text{Co}_2\text{FeAl}$ ,  $\text{Co}_2\text{FeSi}$ ,  $\text{Co}_2\text{FeGa}$ ,  $\text{Co}_2\text{MnAl}$ ,  $\text{Co}_2\text{VAl}$  [28] and  $\text{Co}_2\text{CrAl}$  [29], is subjected to a phase transition from a partially disordered B2 structure to the fully-ordered  $L2_1$  at various temperatures. Thus, the congruent melting of the  $L2_1$  structure allows an easier synthesis of the  $\text{Co}_2(\text{Zr},\text{Hf})\text{Sn}$  alloys with respect to other Heusler, representing a potential advantage in view of potential applications.

In-depth knowledge of the nature of ferromagnetism (as determined by the electronic structure) and of the robustness of the half-metallic behaviour are crucial issues for the prospective implementation of these alloys in real devices. Information on the occurrence of band gaps at 0 K in one of the two spin sub-bands can be obtained by ab-initio calculations. On the other hand, independent information about the shape of the density of states around the Fermi level can be obtained by magnetic measurements and by the analysis of the behaviour of magnetization as a function of temperature and applied field [30–33].

In a previous work [27], we investigated structural, mechanical, and electronic transport properties of  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  Heusler compounds, reporting uncommon trends of Seebeck coefficient (S), electrical conductivity and power factor (P.F.). In particular, for both alloys, the profile of S and P.F. as a function of temperature (T) was reported to be peculiar, presenting a linear growth below  $T_C$ , followed by a flat plateau above  $T_C$ . The aim of this study is to investigate the half-metallic behaviour of  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  alloys, by combining experimental measurements and ab-initio calculations. The magnetic properties are discussed in terms of the Edwards-Wohlfarth model [34,35] of weak itinerant ferromagnetism using Arrott-plots [36] and checking the functional dependence of the magnetization around  $T_C$ . Experimental indications of half-metallicity are found by analyzing the magnetization dependence on temperature in both alloys. A shift from a high-temperature  $M \sim T^2$  regime (Stoner law) to a low-temperature  $M \sim T^{3/2}$  regime (Bloch law) was observed, and it has been attributed to a variation of the spin-flip mechanism (Stoner excitations in the first case, and transverse spin waves in the second one), suggesting the potential presence of the half-metallic band gap, as found in other Heusler alloys [30–32]. Ab-initio calculations showed the presence of a half-metallic band gap in the minority spin sub-band for both alloys. The magnitude of such band gaps and the position of Fermi energies relative to the edge of conduction bands are discussed in detail, as well as the variation of magnetic moment as a function of the lattice parameter and, as a consequence, of the choice of two different exchange-correlation functionals.

## 2. Experimental

Samples of  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  alloys, obtained by arc-melting followed by annealing at 1073 K for 6 days, are the same used and reported in Ref. [27], where a detailed analysis of their structure and composition has already been provided.  $L2_1$  Heusler was found as main phase. Small quantities of  $\text{Co}_2\text{Zr}$  and  $\text{Co}_2\text{Hf}$  C15-Laves phase were also found in  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  samples, in which Sn partially substitutes Zr and Hf atoms, respectively.

Static magnetic properties were measured by means of a SQUID magnetometer (QD MPMS3) in the field interval  $0 \pm 70$  kOe, between 2 K and 400 K, and by a furnace-equipped VSM magnetometer (Lakeshore) in the field interval  $0 \pm 17$  kOe, between 300 K and 550 K, under constant Ar gas flux. Low and high temperature measurements were observed to match on the temperature interval 300-400 K, common to the two magnetometers. Small regular prism-shaped samples were used for magnetic measurements.

Ab-initio calculations were performed using Vienna Ab-initio Simulation Package (VASP) [37] with projector augmented plane (PAW) method [38]. In particular, Co, Hf\_pv, Sn\_d, Zr\_sv potentials were adopted [39]. Perdew-Burke-Ernzerhof (PBE) [40] and Perdew-Burke-Ernzerhof optimized for solids (PBEsol) [41] functionals were selected in order to investigate the effect of computational parameters change on results. A Monkhorst-pack [42]  $15 \times 15 \times 15$  k-points mesh and Gaussian-type smearing were used for ionic relaxation

cycles, while a 24x24x24 mesh and tetrahedron-type smearing were used for single-point energy calculations. Energy cutoff of 500 eV was used in all calculations.

### 3. Results and Discussion

#### 3.1) Magnetic Properties

Figure 1 shows the hysteresis loops,  $M(H)$ , obtained by SQUID measurements at selected temperatures between 2 K and 400 K for  $\text{Co}_2\text{HfSn}$  (panel a) and  $\text{Co}_2\text{ZrSn}$  (panel b) alloys. Both samples clearly show a non-saturating high-field behaviour, which becomes increasingly apparent at high temperatures.

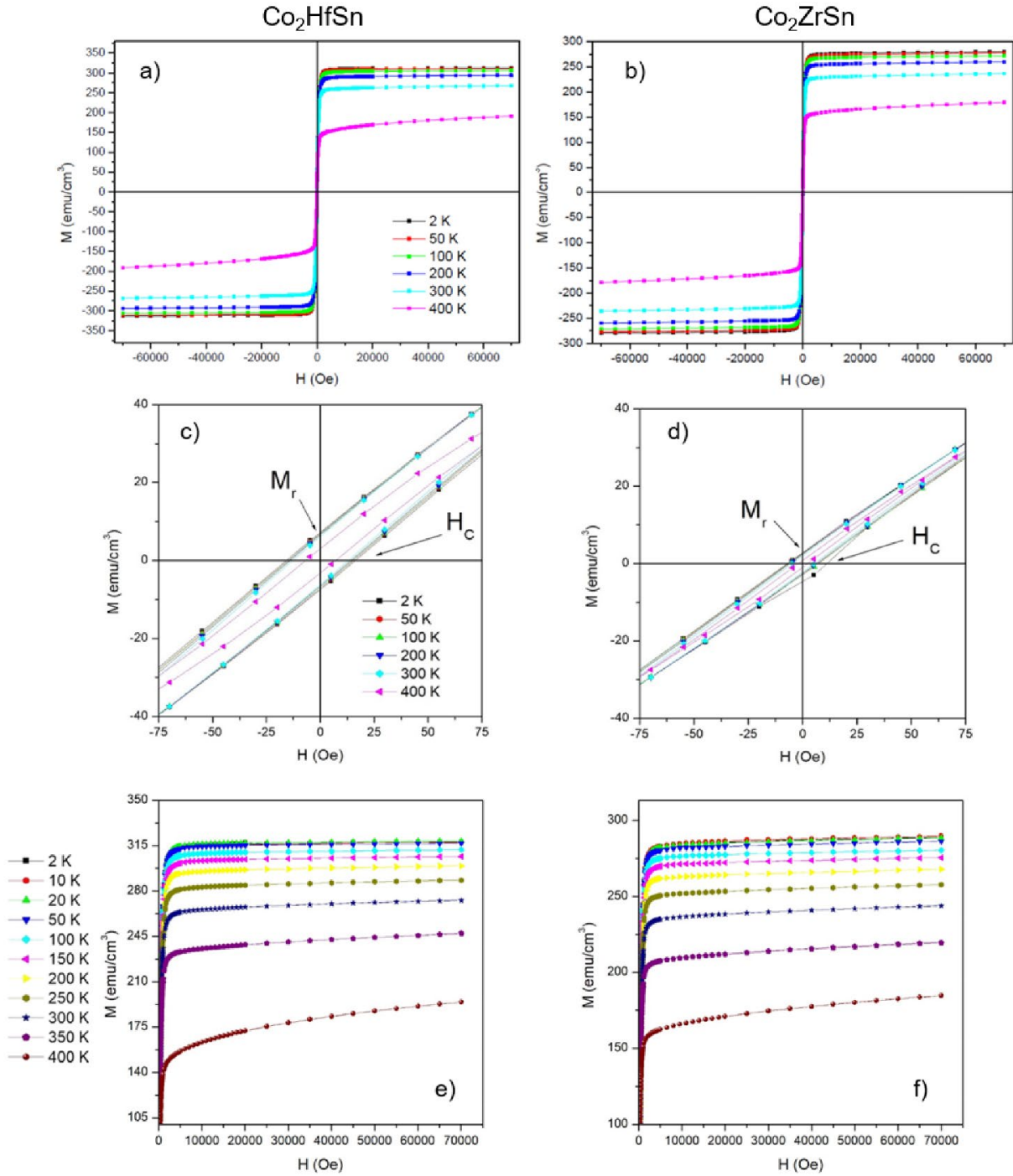


Figure 1: SQUID magnetization results. a-b) Hysteresis loops of  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$ , c-d) Low-field details  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$ , e-f) High-field details  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  at different temperatures.

The low-field region of the hysteresis loops for  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  alloys is highlighted in more detail in Figure 1c and 1d, respectively. A symmetric hysteresis loop is observed in both samples, with coercive field values at  $T = 2$  K of 16 Oe for  $\text{Co}_2\text{HfSn}$  and 7 Oe for  $\text{Co}_2\text{ZrSn}$ , which gradually decreases with increasing temperature down to about 7 Oe and 2 Oe, respectively, at  $T = 400$  K. The non-saturating high-field trend of the  $M(H)$  curves is highlighted in Figure 1e and Figure 1f for  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  alloys, respectively.

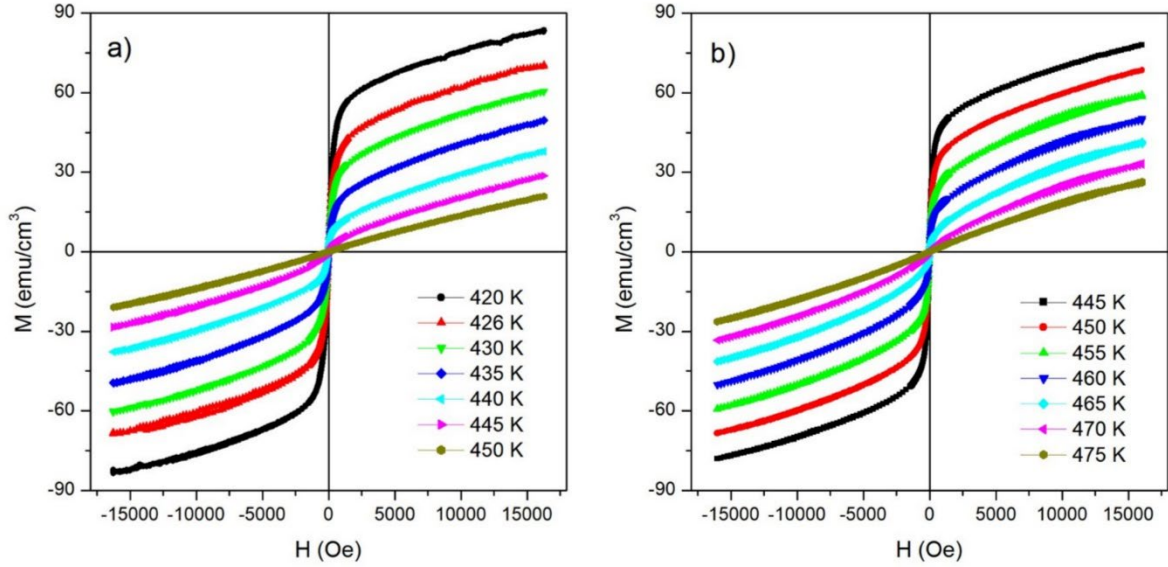


Figure 2: VSM measurements of magnetization in proximity of the Curie temperature in  $\text{Co}_2\text{HfSn}$  (a) and  $\text{Co}_2\text{ZrSn}$  (b).

High temperature magnetic properties obtained by the VSM are shown in Figure 2 in the range around  $T_C$ . Combining SQUID and VSM measurements, it was possible to obtain the complete magnetization curve as a function of temperature under constant field ( $H = 5$  kOe), as shown in Figure 3 for both alloys. The magnetization curves obtained by SQUID and VSM measurements match satisfactorily.

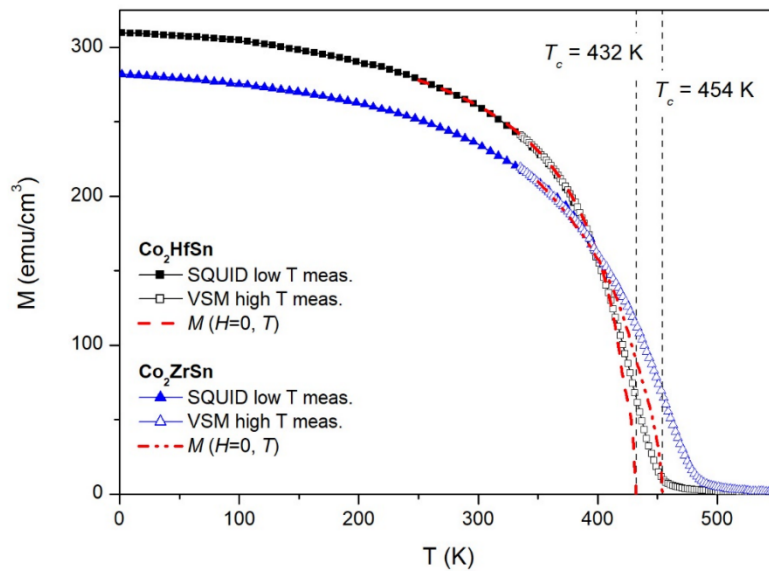


Figure 3: Temperature dependence of magnetization of  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  samples under a constant field of 5 kOe. Full and open symbols refer to SQUID and VSM measurements, respectively. Red dashed lines are the corresponding  $M(H=0, T)$  curves derived from theory (see Section 3.2). The Curie Temperatures ( $T_C$ ) are highlighted by the vertical grey dashed lines.

### 3.2) Weak itinerant ferromagnetism

In weak itinerant ferromagnets, the electrons responsible for ferromagnetism participate in the electrical conduction and the unbalance between spin-up and spin-down carriers is small. In Wohlfarth's simple model of weak itinerant ferromagnetism, the following relationship is obtained under equilibrium conditions for free magnetic energy [34,35]:

$$\frac{H}{M} = \alpha(T) + \beta(T)M^2 + O\{M^4\} \quad (1)$$

where  $M(H, T)$  is the magnetization,  $\alpha$ ,  $\beta$  are temperature dependent coefficients.

This expression is valid when the following two conditions are simultaneously satisfied: a)  $M(H, T) \ll Nn\mu_B$ , where,  $N$  is the number of atoms concurring to provide electrons to the conduction band,  $n$  the number of electrons per atom in the conduction band,  $\mu_B$  is the Bohr magneton; b)  $T \ll T_F$ , where  $T_F$  is the Fermi temperature of the electron gas. In our case, the maximum magnetization is  $M_{max} \cong 0.1nN\mu_B$ , and  $T$  is always well below  $T_F$  for both alloys. In the present case, the terms in higher even powers of magnetization ( $M^{2j}$ , where  $j = 2, 3, 4, \dots$ ) may be considered negligible, because the leading factor in the coefficient of these terms is of the type  $\rho_F'^{2j} / \rho_F^{4j+1}$ , where  $\rho_F$  and  $\rho_F'$  are, respectively, the density of states and its derivative at the Fermi energy [34]; these coefficients are estimated to be very small for  $j \geq 2$ , when the DOS  $\rho(E)$  does not show a highly structured behaviour around the Fermi energy (as discussed in Section 3.3).

This model implies that the ferromagnetic order of  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  compounds can be basically described by two temperature-dependent parameters,  $\alpha$  and  $\beta$  (see Equation 1). These quantities can be derived from the Arrott plots, as shown in Figure 4. In weak itinerant ferromagnetism, Arrott plots directly derive from Equation 1, when  $O\{M^4\}$  terms are neglected, so that a linear relationship between  $M^2$  and  $H/M$  should be observed at all temperatures, both well below and above  $T_C$  (Figure 4). As usual [36,43,44], the low-field regions are excluded by the plot, because the Wohlfarth theory applies to an infinitely extended, ideal single crystal, containing no magnetic domain walls, whereas the low-field regions of the measured  $M(H)$  curves are dominated, in real samples, by the presence of multiple magnetic domains arising by effect of surfaces, grain boundaries, defects, magnetic anisotropies, and responsible for the observed magnetic hysteresis. Data shown in Figure 4 are taken for  $H \geq 7$  kOe, i.e., well above the closure field of the hysteresis loops, where the sample can be assumed to be in a single-domain state. The observed linearity between  $M^2$  and  $H/M$  at all temperatures (Figure 4a,b) strongly suggests that both compounds are indeed weak itinerant ferromagnets. It should be remarked that in all ferromagnetic materials the linearity between  $M^2$  and  $H/M$  can usually be observed near to the Curie temperature, being derived from the general Landau's theory of magnetic phase transitions [34,36], but it is hardly found elsewhere.

The trend of the parameter  $-\alpha(T)$  as a function of temperature is shown in Figure 4c. It should be noted that information about  $T_C$  can be obtained either from the graphs in panels a), b) of Figure 4 (the linear extrapolation of the high-field data is expected to pass through the origin at  $T = T_C$ ) or from the change of sign of the parameter  $-\alpha(T)$  observed in Figure 4c. The latter method allows a more accurate estimate of the transition temperature, resulting in  $T_C = 432$  K and  $T_C = 454$  K for  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$ , respectively. The theoretical zero-field magnetization for  $T \leq T_C$  is  $(H = 0, T) = \sqrt{-\alpha(T)/\beta(T)}$ . This curve is shown in Figure 3 (red dashed line). The effect of applying a constant magnetic field ( $H = 5$  kOe) during measurements is negligible at low temperatures (i.e.,  $(H = 5 \text{ kOe}, T) \cong M(H = 0, T)$ ) whereas it becomes increasingly apparent when  $T$  approaches to  $T_C$  and obviously for  $T > T_C$ . As a matter of fact, the magnetization curve at 5 kOe obtained using the SQUID magnetometer (i.e. up to 400 K) can be safely taken as representative of the behaviour of the ideal spontaneous magnetization.

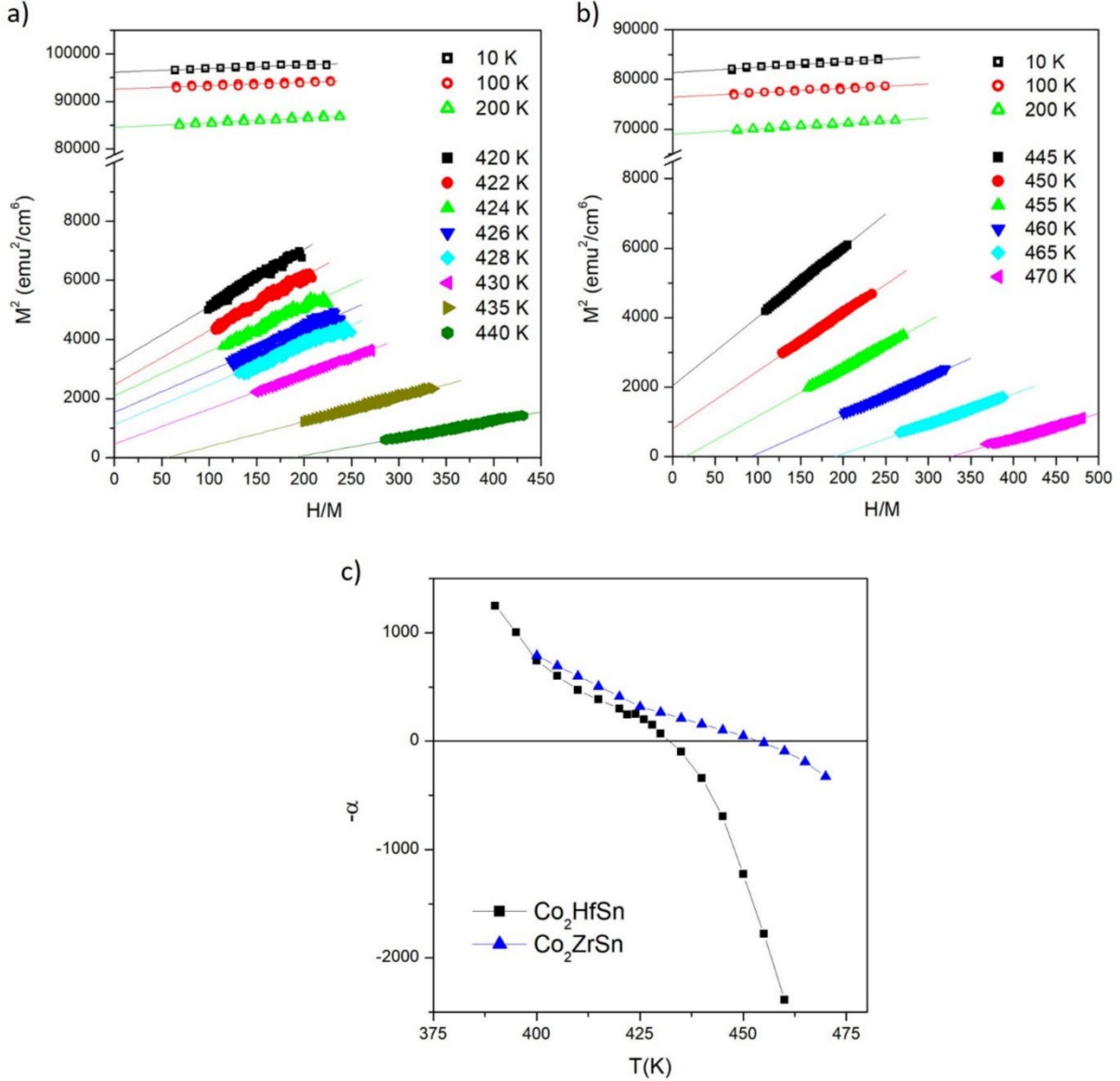


Figure 4: Arrott plot of a)  $\text{Co}_2\text{HfSn}$ , b)  $\text{Co}_2\text{ZrSn}$  alloys, and c)  $-\alpha$  parameter as a function of temperature around  $T_C$ .

The data reported in Arrott plots are well described (even in proximity of the ferromagnetic-paramagnetic transition) by using the mean-field values for the exponents of  $H/M$  and  $M$ , as appearing in Equation 1 (i.e., 1 and 2, respectively) [21,35]. Slightly different values of the critical exponents (1.02-1.03 and 2.10-2.12, respectively) were recently found in  $\text{Co}_2\text{HfSn}$  by exploiting accurate magnetization measurements performed using a SQUID magnetometer around  $T_C$  [21].

A further method to prove that the mean field model is able to describe the magnetic properties of  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  samples at high temperatures, is to verify the functional dependence of  $M$  on  $H$  near  $T_C$ . According to Equation 1, at  $T_C$  the behavior of  $M$  with  $H$  is predicted to be:

$$M(H) = \frac{1}{\beta^{1/3}(T_C)} H^{1/3} \quad (2)$$

The  $M(H^{1/3})$  curves are reported in Figure 5 for temperatures around  $T_C$ . All curves are basically linear and almost parallel to each other, as indicated by the theory, the coefficient  $\beta$  being almost constant there.

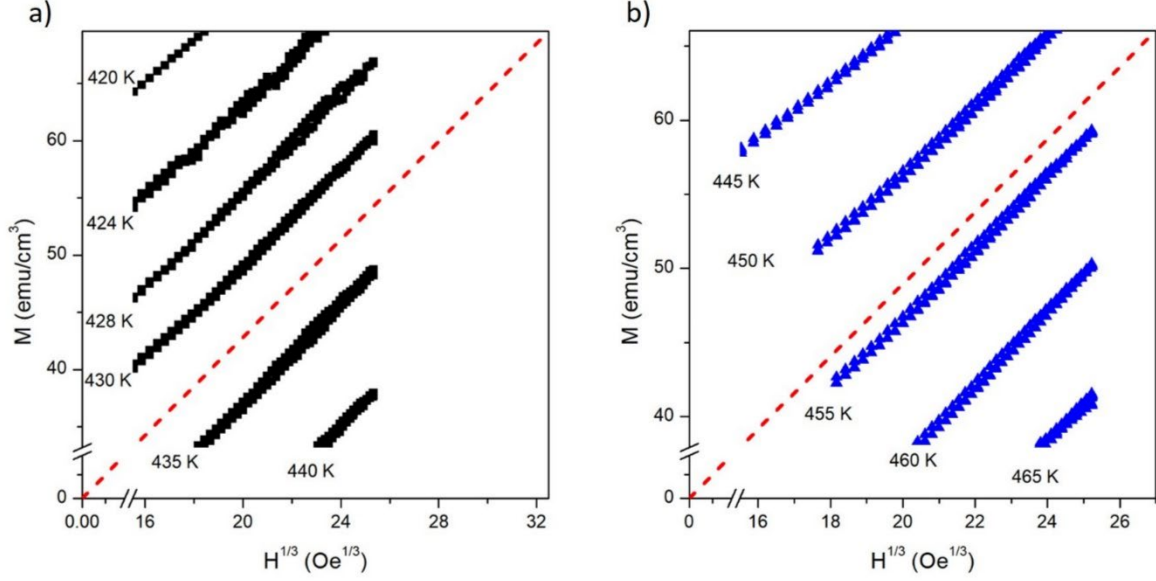


Figure 5: Symbols: experimental magnetization dependence on  $H^{1/3}$  around  $T_C$  of  $\text{Co}_2\text{HfSn}$  (a) and  $\text{Co}_2\text{ZrSn}$  (b). Dashed straight lines: behavior of  $M(H^{1/3})$  predicted at  $T = T_C$ .

The inverse initial susceptibility  $\chi_0^{-1} = (\lim_{H \rightarrow 0} \frac{dM}{dH})^{-1}$  is reported as a function of  $T > T_C$  in Figure 6a,b (full symbols). In the mean field model of weak itinerant ferromagnetism,  $\chi_0^{-1}(T) \equiv \alpha(T)$ , as directly derived from Equation 1. The quantity  $\alpha(T)$  obtained from the Arrott plots is also shown in Figure 6a,b (open symbols). Experimental and predicted results are in rather good agreement well above  $T_C$ , while close to the Curie temperature the inverse magnetic susceptibility is substantially lower than the theoretical prediction, indicating that the  $M(H)$  curves are steeper than predicted by the model. This can be checked by directly looking at experimental and calculated  $M(H)$  isotherms (Figure 6c,d). The theoretical curves are easily obtained in analytical form by solving Equation 1, as reported in the Supplementary Material.

The curves drawn using the  $\alpha(T)$  and  $\beta(T)$  values derived from the Arrott plots, with no adjustable parameters, are shown in Figure 6c,d. For both compounds, all theoretical curves appear to be superimposed to the corresponding experimental results at high magnetic fields. This confirms that terms in high powers of magnetization ( $M^{2j}$ , where  $j = 2, 3, 4, \dots$ ) in Equation 1 are not required in order to describe the present experimental results. As it will be discussed later, this is related to the shape of the electronic density of states around the Fermi level.

Below  $T_C$ , the agreement between theory and experiment is to be expected only at high fields, when the sample is in a single-domain state (see Section 3.2). In particular, the theory predicts the existence of a finite value of the spontaneous magnetization  $M(H, T)$  for  $H \rightarrow 0$ , whereas the presence of magnetic domains in a real sample leads to a much lower remanence value, which is very close to zero in the temperature range considered in Figure 6c,d. This explains the observed deviation between theory and experiment below about 7 kOe.

Well above  $T_C$  the agreement between theory and experiment is very good. In this case, both experimental and theoretical curves appear to be perfectly superimposed over the entire magnetic field range, including the low field region. A deviation is observed in both compounds for temperatures slightly higher than  $T_C$ ; in particular, the experimental curves turn out to be steeper than predicted by the model. This behavior reflects the discrepancy of  $\chi_0^{-1}$  and  $\alpha$  values around  $T_C$  put in evidence by Figure 6a,b. One possible origin of this behavior is the presence of slight fluctuations in the composition of samples, which could entail a non-uniform transition temperature  $T_C$  in different regions of the material. In this case, the higher slope of the experimental curves for temperatures just above  $T_C$  could derive from a residual ferromagnetic contribution of regions where the magnetic transition has not yet occurred. In this regard, it should be mentioned that as far as the composition



of Heusler phases are concerned, SEM-EDS analysis of samples indicated deviations from the ideal stoichiometry, of the order of a few percent, as reported elsewhere [27].

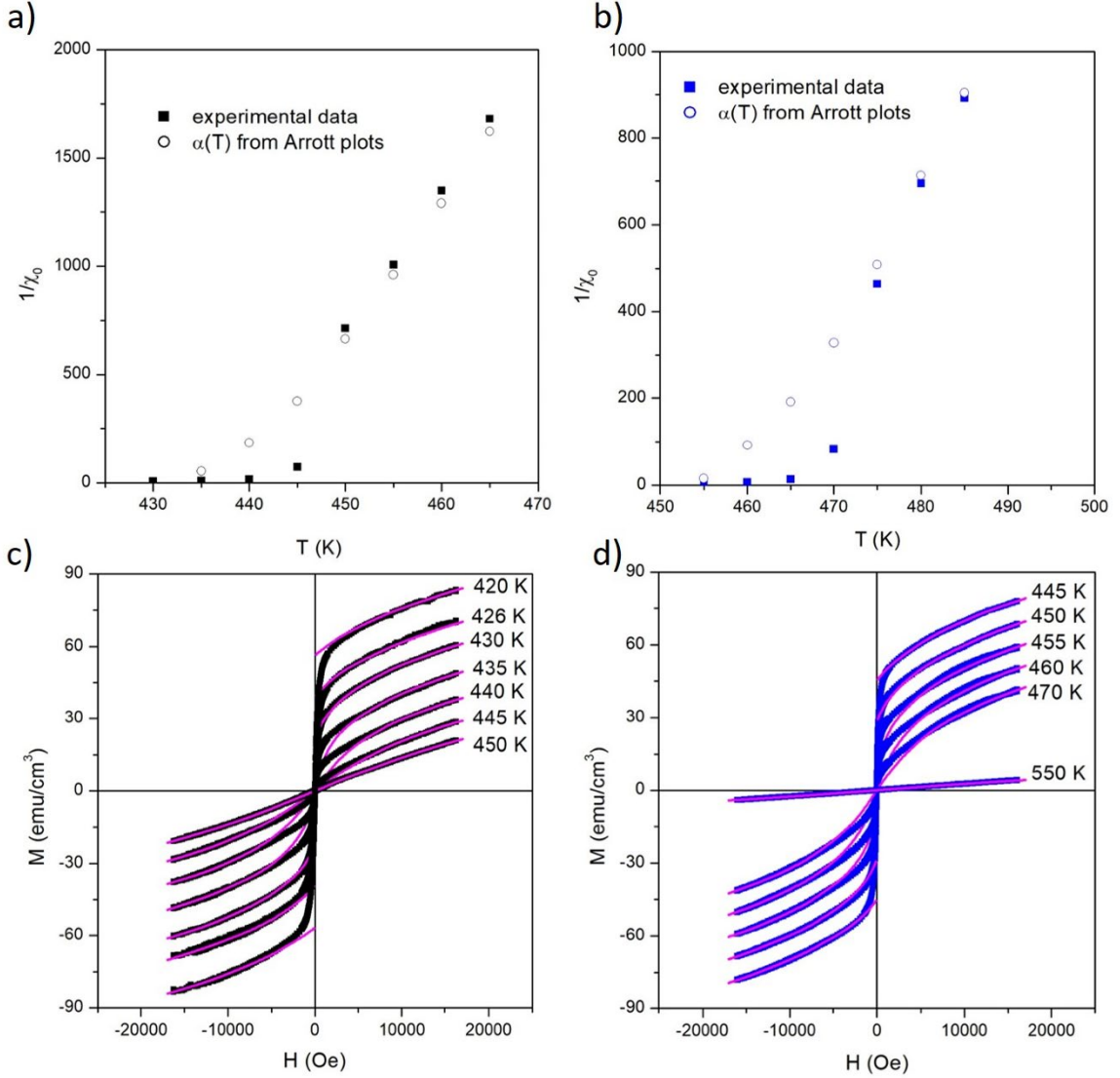


Figure 6: Upper row: inverse of the zero-field magnetic susceptibility ( $\chi_0^{-1}$ ) as a function of temperature in  $\text{Co}_2\text{HfSn}$  (a) and  $\text{Co}_2\text{ZrSn}$  (b). Full symbols: experiment, open symbols: theory. Lower row: comparison between experimental and calculated  $M(H)$  isothermal magnetization curves of  $\text{Co}_2\text{HfSn}$  (c) and  $\text{Co}_2\text{ZrSn}$  (d). Full symbols: experiment, lines: theoretical  $M(H)$  curves (see Section 3.2).

### 3.3) Ab-initio calculations

In order to better understand the nature of half-metallicity in  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$ , ab-initio calculations have been performed. Two exchange-correlation functionals, Perdew-Burke-Ernzerhof (PBE) and Perdew-Burke-Ernzerhof optimized for solids (PBEsol), were used with the purpose to check whether the obtained results are consistent as the simulation parameters are changed.

The total energy of the calculated cubic unit cell as a function of the lattice parameter is reported in Figure 7 for both compounds. Minimum energy values are reached for lattice parameters of 6.2498 Å and 6.1641 Å for  $\text{Co}_2\text{HfSn}$  with PBE and PBEsol, respectively, while 6.2843 Å and 6.2029 Å are obtained for  $\text{Co}_2\text{ZrSn}$  with PBE and PBEsol, respectively. Reported experimental lattice parameters [27] of 6.2157 Å for  $\text{Co}_2\text{HfSn}$  compound and 6.2458 Å for  $\text{Co}_2\text{ZrSn}$  compound, obtained at room temperature and from the same samples used in this work, are inside the calculated values. Formation energies ( $\Delta E_{\text{form}}$ ) per formula unit starting from the constituent elements ( $\alpha\text{-Co}$ ,  $\alpha\text{-Hf}$ ,  $\alpha\text{-Zr}$ ,  $\beta\text{-Sn}$ ) of -1.60 eV/f.u. and -1.61 eV/f.u. were obtained using PBE

functional for  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$ , while, for PBEsol,  $\Delta E_{\text{form}}$  values turned out equal to  $-1.76$  eV/f.u. and  $-1.74$  eV/f.u., respectively.

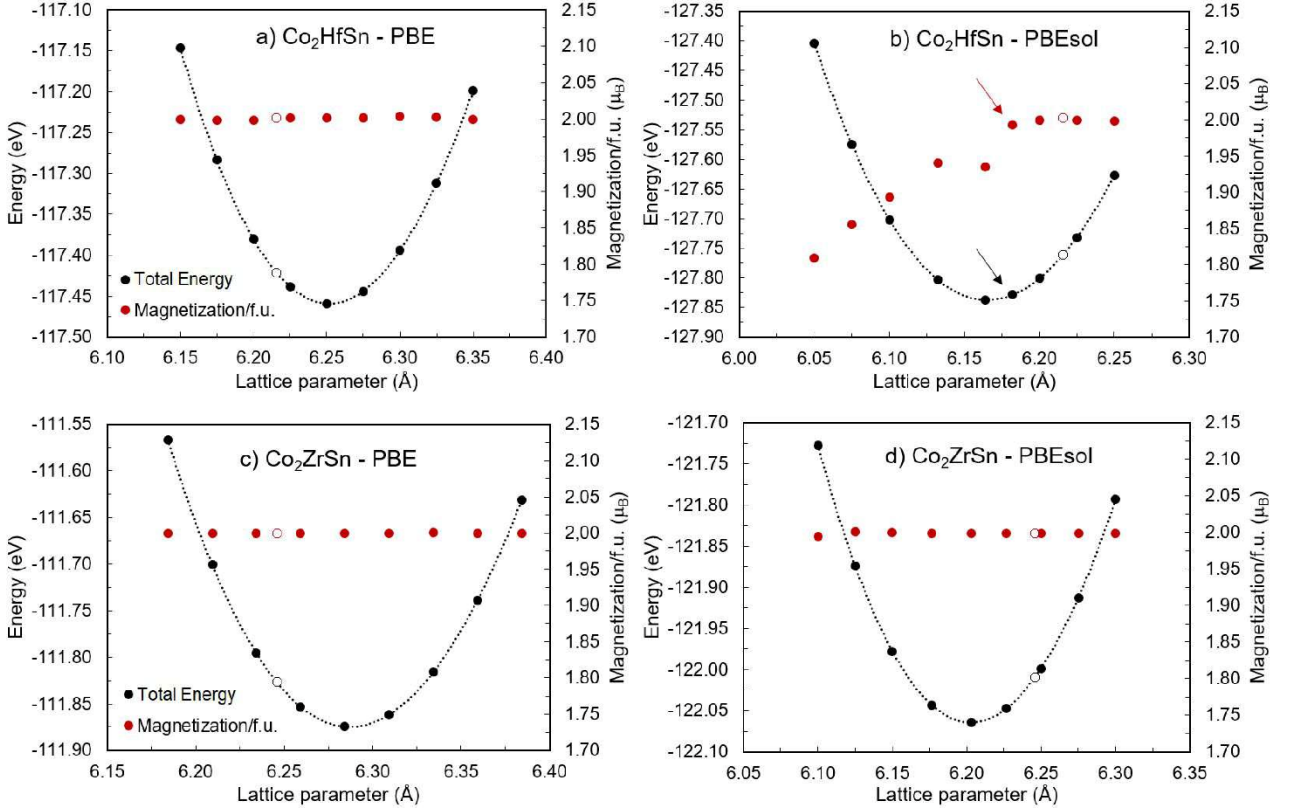


Figure 7: Total energy (black dots) and magnetization per formula unit (red dots) as a function of lattice parameter  $a$  (each point corresponds to results of a DFT calculation with fixed lattice parameter). a), b)  $\text{Co}_2\text{HfSn}$  computed with PBE and PBEsol, respectively. c), d)  $\text{Co}_2\text{ZrSn}$  computed with PBE and PBEsol, respectively. Empty circles are used for calculations performed imposing experimental lattice parameter values [27]. Near-equilibrium cell in  $\text{Co}_2\text{HfSn}$ -PBEsol is highlighted by arrows.

The magnetization per formula unit were also calculated as a function of the lattice parameter and results are also reported in Figure 7. For both alloys and functionals, the magnetization is generally not very sensitive to variations of  $a$ . An exception is  $\text{Co}_2\text{HfSn}$  when computed with PBEsol (Figure 7b) in which fluctuations up to  $0.20 \mu_B$  are observed within a range of  $0.2 \text{ \AA}$ . In particular, it is notable how magnetization suddenly increases from  $1.93 \mu_B$  in the equilibrium cell (which lies at the minimum of the curve) to  $2.00 \mu_B$  in a near-equilibrium cell (highlighted by arrows), that has a lattice parameter of  $6.1821 \text{ \AA}$ . Total energies and magnetic moments were also calculated imposing the above mentioned experimental lattice parameters and are indicated with empty circles in Figure 7. It can be noted that all magnetization per formula unit values are close to  $2 \mu_B$ .

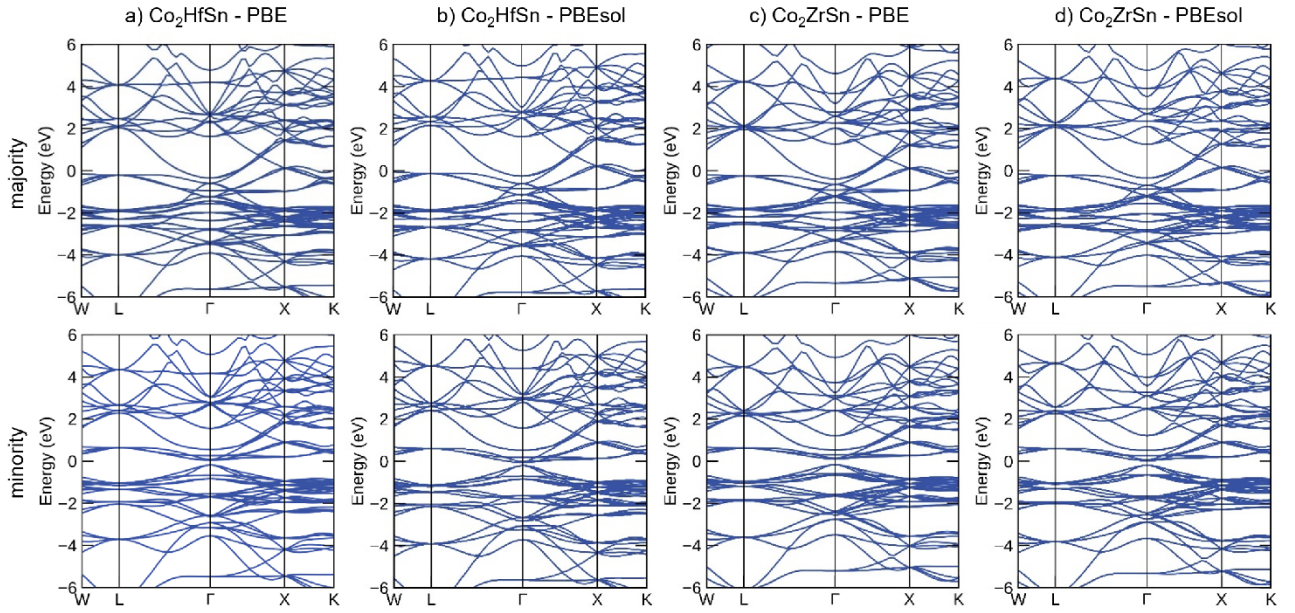


Figure 8: Band structure diagrams of  $\text{Co}_2\text{HfSn}$  alloy calculated with a) PBE, b) PBEsol functionals and  $\text{Co}_2\text{ZrSn}$  alloy with c) PBE, d) PBEsol functionals.

Calculated band structure diagrams are shown in Figure 8. It can be noted that band gaps in the minority sub-bands are direct and centred on the  $\Gamma$  point, while majority spin bands crossing the Fermi level are partially filled. This can be observed even more clearly from density of states diagrams, reported in Figure 9. Comparable profiles were obtained with the two functionals, both for valence and conduction levels, in majority and minority spin sub-bands. As expected for weak itinerant ferromagnets [45], majority and minority sub-bands are approximately specular and slightly shifted relative to each other.

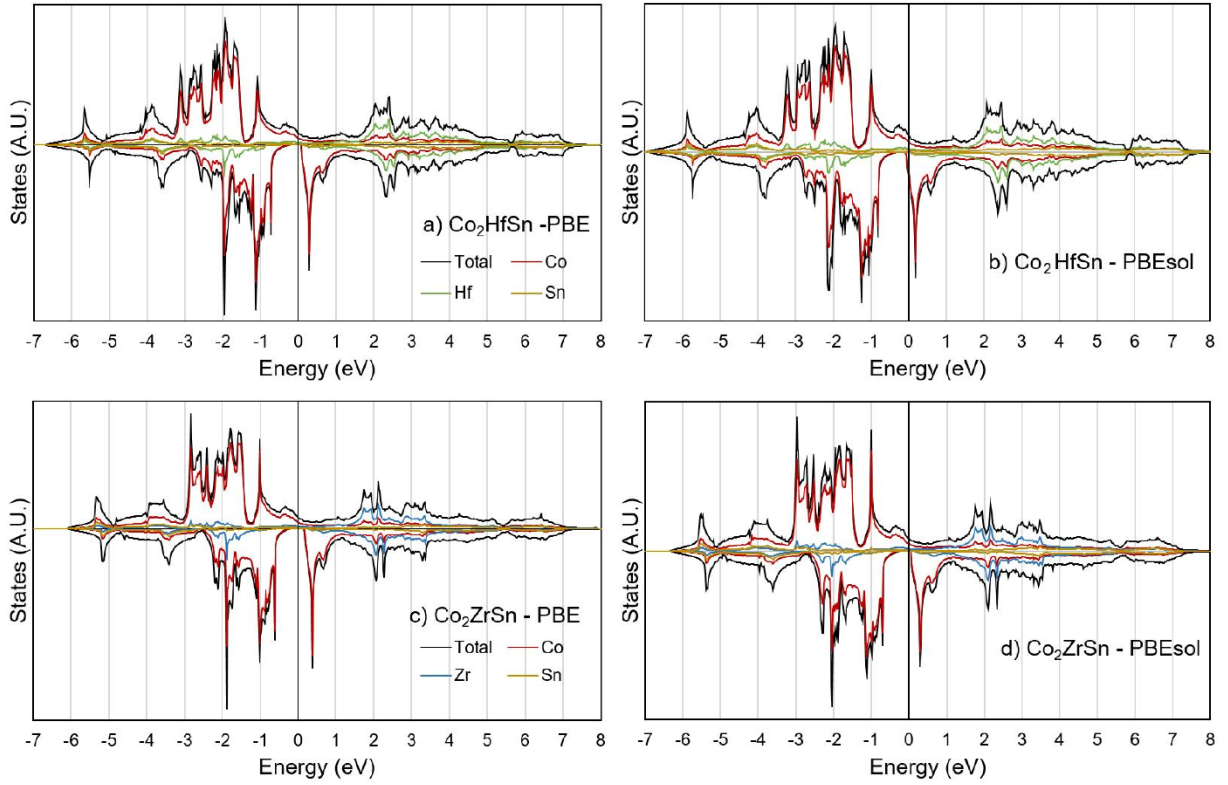


Figure 9: Total and projected density of states diagrams for the fully relaxed structures of  $\text{Co}_2\text{HfSn}$  alloy calculated with a) PBE, b) PBEsol functional and of  $\text{Co}_2\text{ZrSn}$  alloy calculated with c) PBE, d) PBEsol.

Band gaps in the minority spin sub-bands of 0.34 eV and 0.30 eV are observed for  $\text{Co}_2\text{ZrSn}$  when PBE and PBEsol are used, respectively, and the Fermi energy ( $E_F$ ) is observed inside the gap. In  $\text{Co}_2\text{HfSn}$ , a band gap of 0.30 eV is obtained for PBE calculations and  $E_F$  is also observed inside the minority gap; however, when PBEsol functional is used, the Fermi energy is observed slightly outside the band gap for the minority spin sub-band. This implies that at 0 K a few electrons with minority spins have enough energy to be in the conduction band, with consequences on the calculated magnetic properties. The steep slope of the minority DOS near the Fermi energy is also particularly important as minor variations in the position of  $E_F$  can significantly change the balance between majority and minority electrons at 0 K. Values of approximately  $2 \mu_B$  (see Figure 7) for the calculated magnetization were found in all cases, apart from  $\text{Co}_2\text{HfSn}$  computed with PBEsol, in which a  $1.93 \mu_B$  value was obtained for the fully relaxed cell. Thus, except for this latter case, the alloys are observed to follow the Slater-Pauling rule. Comparing Figure 9a with Figure 9b, and Figure 9c with Figure 9d, it can be noted that the PBEsol functional systematically locates Fermi energy of alloys closer to the conduction band. In  $\text{Co}_2\text{HfSn}$ , the position of the  $E_F$  is slightly inside the minority conduction band, causing the above-mentioned deviation from Slater-Pauling rule. The same shift of Fermi level towards the conduction band can be observed in the  $\text{Co}_2\text{ZrSn}$  DOS (Figure 9c and Figure 9d) when comparing PBE and PBEsol results; however, in this case,  $E_F$  is always inside the band gap and the resulting magnetization does not change from  $2.00 \mu_B$ .

Furthermore, as it can be noted from Figure 7b, the magnetic moment in the case of  $\text{Co}_2\text{HfSn}$ -PBEsol is also highly sensitive to small lattice parameter variations. In fact, it is noticeable how it rapidly increases up to  $2.00 \mu_B$  when increasing  $a$ . Increasing the fixed lattice parameter in the calculation also corresponds to a shift of the Fermi energy towards lower energies, i.e. from the conduction band to the gap in the minority sub-band. Hence, the PBEsol results for  $\text{Co}_2\text{HfSn}$  are underestimating the lattice parameter and the magnetic moment, while the position of the Fermi level is overestimated with respect to the minority band gap. This becomes evident considering the DOS diagrams shown in Figure 10 calculated using the previously mentioned experimental

lattice parameters [27] (empty circles in Figure 7). In all cases, the calculated DOS does not significantly differ from those reported in Figure 9 as well as calculated magnetic moment values, with the exception of  $\text{Co}_2\text{HfSn}$ -PBEsol (Figure 10b). In this case, Fermi energy is inside the half-metallic band gap in the minority spin sub-band and, accordingly, magnetic moment value here is  $2 \mu_B$  as in the other cases. Band-gap values for  $\text{Co}_2\text{HfSn}$  are here of 0.32 eV and 0.27 eV when calculated with PBE and PBEsol, respectively, while for  $\text{Co}_2\text{ZrSn}$  they are 0.36 eV and 0.30 eV, respectively, with PBE and PBEsol.

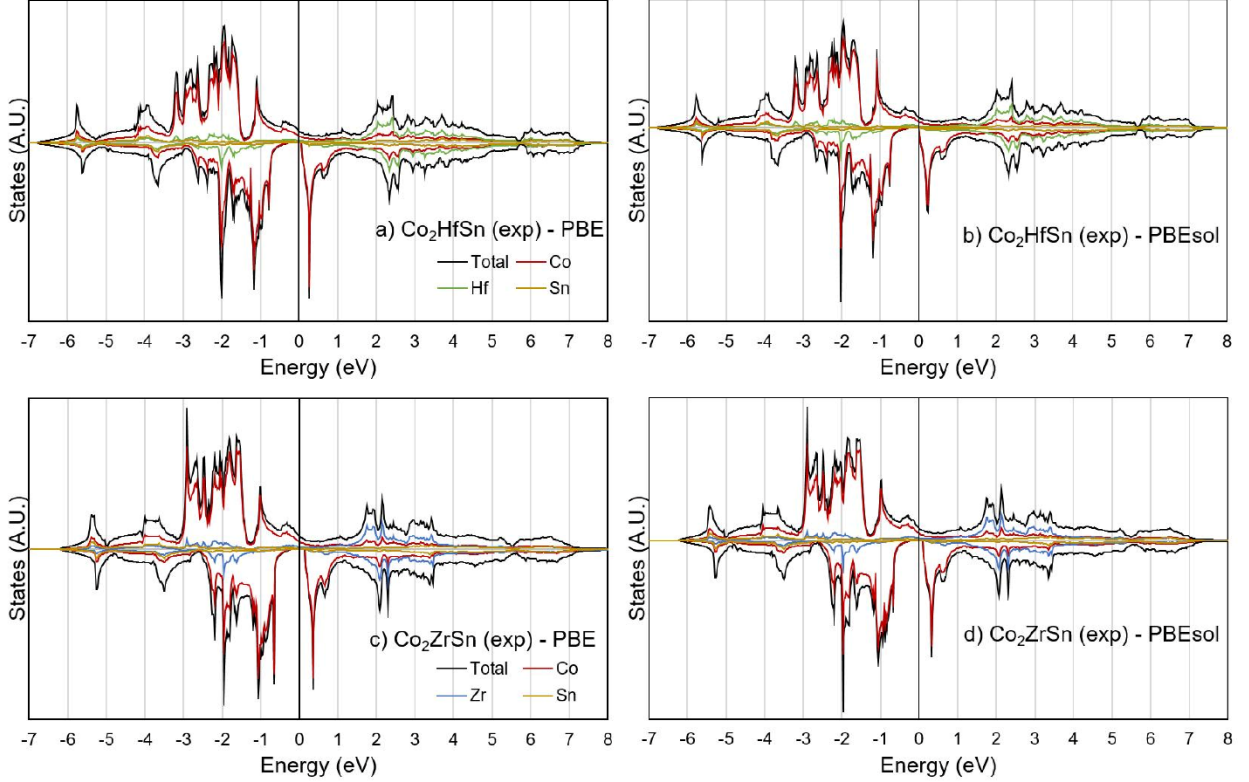


Figure 10: Total and projected density of states diagrams calculated imposing experimentally obtained lattice parameters [27] of  $\text{Co}_2\text{HfSn}$  alloy with a) PBE, b) PBEsol functional and  $\text{Co}_2\text{ZrSn}$  alloy calculated with c) PBE, d) PBEsol.

Spin-flip energy ( $E_{\text{flip}}$ ), defined as the energy of the limit of minority-spin conduction band subtracted to  $E_F$ , is another important parameter that can be used in order to evaluate half-metallicity. For the equilibrium cells in  $\text{Co}_2\text{ZrSn}$ ,  $E_{\text{flip}}$  are equal to 0.18 eV and 0.08 eV for calculations with PBE and PBEsol functionals, respectively. In  $\text{Co}_2\text{HfSn}$ ,  $E_{\text{flip}}$  is 0.10 eV for PBE, while, for PBEsol,  $E_F$  intersects the conduction band 0.08 eV above the highest limit of the band gap. Using experimental lattice parameters, spin-flip energies are for  $\text{Co}_2\text{HfSn}$  respectively of 0.06 eV and 0.01 eV with PBE and PBEsol, while for  $\text{Co}_2\text{ZrSn}$  they are 0.16 eV and 0.12 eV with PBE and PBEsol, respectively. In all cases,  $\text{Co}_2\text{ZrSn}$  compound shows the largest  $E_{\text{flip}}$ .

As noticeable from projected DOS diagrams (Figure 9 and Figure 10), in all cases, densities of states near Fermi level are dominated by Co contribution. Also, magnetization values are due almost exclusively to Co atoms, as expected. This information suggests that tuning of half-metallic and conductive properties can be effectively achieved acting almost exclusively on Co sites.

### 3.4) Magnetization at low temperature

The temperature dependence of the magnetization measured under a magnetic field of 5 kOe (basically coincident with the spontaneous magnetization, as remarked before) is shown in Figure 11. In both compounds, the magnetization is accurately fitted by a law of the type  $M_s = M_s(0)(1-AT^2)$  up to  $T \approx 230$  K (left panels). However, at low temperatures, the  $M(T^2)$  curve deviates upwards from a straight line, as shown in the two

insets of Figure 11; in  $\text{Co}_2\text{ZrSn}$  the deviation is stronger and takes place below about 70 K, whilst in  $\text{Co}_2\text{HfSn}$  it is observed below about 30 K. At low temperatures, the magnetization can be instead fitted by the Bloch law,  $M_s(T) = M_s(0) (1 - BT^{3/2})$ , as shown in Figure 11 (right panels). These results are in good agreement with the calculated DOS (see Section 3.3) and with the possible half-metallic character of these Heusler alloys. In itinerant ferromagnets, the linear dependence of magnetization on the square of temperature arises by effect of spin flipping excitations of electrons (Stoner excitations); however, in half metals, spin-flip processes are inhibited at low temperatures by the spin-flip energy  $E_{\text{flip}}$ , so that transverse spin wave excitation, resulting in the Bloch law, becomes the dominant mechanism of magnetization reduction [30]. This effect can be pictured as the prevalence of localized (Heisenberg-type) ferromagnetism at very low temperature (as expected for half metals when spin-flip processes are inhibited) followed by a gradual transition to standard itinerant ferromagnetism, when Stoner excitations begin to play an important role.

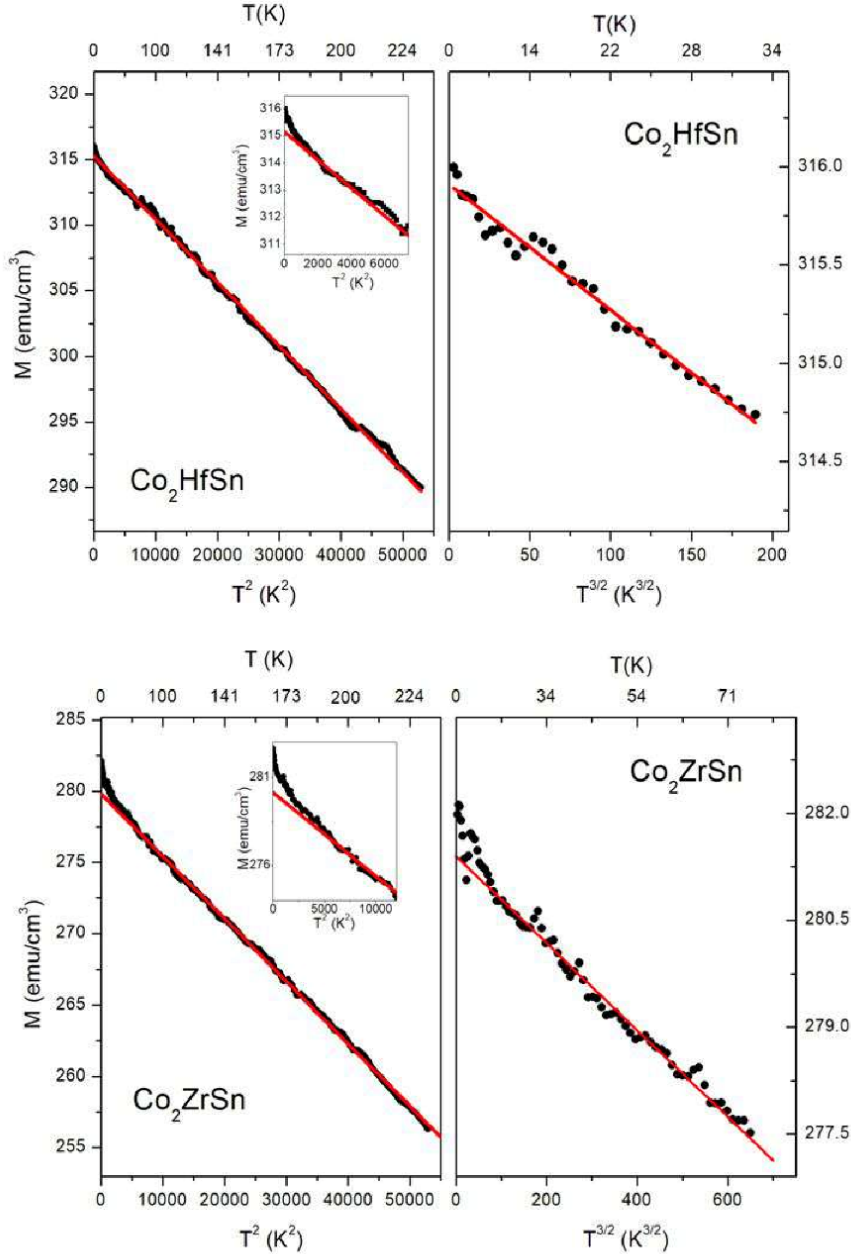


Figure 11: Left panels: Plot of spontaneous magnetization  $M_s$  as a function of  $T^2$  in  $\text{Co}_2\text{HfSn}$  (up) and  $\text{Co}_2\text{ZrSn}$  (down). Insets show the deviation from the  $T^2$ -law. Right panels: plot of  $M_s$  as a function of  $T^{3/2}$  at low temperatures in  $\text{Co}_2\text{HfSn}$  (up) and  $\text{Co}_2\text{ZrSn}$  (down).

The observed crossover between Bloch and Stoner laws for  $M(T)$  is in agreement with the theoretical prediction that the Fermi energy is in the gap of the minority electron sub-band. In  $\text{Co}_2\text{ZrSn}$ , the crossover temperature

is higher than in  $\text{Co}_2\text{HfSn}$ , suggesting a higher spin-flip energy, as actually predicted by calculations (Figure 9). In  $\text{Co}_2\text{HfSn}$ , the much weaker deviation of  $M(T)$  away from the  $T^2$  law is compatible with a Fermi energy still located in the minority electron gap, but very close to its upper edge, so that spin-flip processes begin to take place at very low temperatures. The picture emerging from the present analysis for  $\text{Co}_2\text{HfSn}$  agrees with the results of simulations performed using the PBE and PBEsol functionals (see Figure 9 and Figure 10) where the Fermi level was found to be remarkably close to the edge of the conduction band. It should be remarked that in the region where spin-flip effects dominate, the quantity  $\Delta M/M = [M_s(0) - M_s(T^2)]/M_s(0) = A T^2 / M_s(0)$  turns out to have basically the same slope ( $A/M_s(0) \approx 1.70 \times 10^{-6} \text{ K}^{-2}$ ) in both alloys, indicating that the densities of electronic states around the Fermi level are similar in the two compounds [46], in qualitative agreement with the calculated DOS.

As far as the magnetic moments per formula unit are concerned, based on the Slater-Pauling rule for half-metallic Heusler alloys as well as ab-initio calculations (Section 3.3), values of  $\mu = 2.00 \mu_B$  are expected for these compounds. Magnetic moments of  $\mu = 2.01 \mu_B/\text{f.u.}$  for  $\text{Co}_2\text{HfSn}$  and  $1.80 \mu_B/\text{f.u.}$  for  $\text{Co}_2\text{ZrSn}$  result from extrapolation to  $T = 0 \text{ K}$  of the overall experimental data. These values are in agreement with the experimental values of  $\mu$  reported in different papers, ranging from  $1.50$  to  $2.00 \mu_B/\text{f.u.}$  in  $\text{Co}_2\text{HfSn}$  [21,47–51] and from  $1.34$  to  $2.00 \mu_B/\text{f.u.}$  in  $\text{Co}_2\text{ZrSn}$  [47,48,50–55]. However, the effect of the relative amount of impurities present in the samples used in this work (see Section 2) should also be taken into account. The intermetallic compounds  $\text{Co}_2\text{Hf}$  and  $\text{Co}_2\text{Zr}$  are known to be standard Pauli paramagnets, characterized by very low susceptibility values [55–57]. A calculation done using these susceptibility values shows that the contribution of the magnetic impurities is completely negligible at all temperatures, resulting in a magnetization at  $70 \text{ kOe}$  which is lower than the measured value by about three orders of magnitude. Considering the presence of the impurity phases, the values per formula unit would become:  $\mu = 2.15 \mu_B/\text{f.u.}$  for  $\text{Co}_2\text{HfSn}$  and  $2.05 \mu_B/\text{f.u.}$  for  $\text{Co}_2\text{ZrSn}$ . Deviations from stoichiometry and secondary phases are rarely taken into consideration in the literature on the considered alloys. However, the type and fraction of spurious non-Heusler compounds can strongly affect the experimental value of magnetic moment per unit formula, and can be deemed responsible for the very scattered experimental values of  $\mu$  found in the literature as shown above. The occurrence of secondary phases in  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  samples has already been reported in literature also by Yin et al., who extensively investigated formation enthalpies and other thermodynamic properties of a large number of Co-based Heusler compounds [28].

### 3.5) Comparison between experimental and calculated data

Combining experimental and ab-initio calculated data it is possible to obtain crucial information on half-metallicity of  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  alloys. A collection of relevant data reported in this work, together with a selection of previously reported results in literature is presented in Table 1.

As it can be noticed, calculated data are generally in agreement with experimental values. In all cases, the half-metallic character of the investigated compounds has been confirmed by the present calculations, with the exception of  $\text{Co}_2\text{HfSn}$  when computed with PBEsol functional. The reason for this failure has already been discussed and is essentially related to the underestimation of the equilibrium lattice parameter of the unit cell when using this exchange-correlation functional for this system. This is also confirmed by the experimental lattice parameters in Table 1.

Although the results of present calculations are in good agreement with the experimental data, discrepancies between calculated and experimental data still occur (Table 1). The origin of these differences can be attributed to two main factors. First, computational details are known to have great influence on calculated properties [58]. The choice of the most suitable DFT exchange-correlation functional is usually regarded as the main issue in determining band gaps [59], Fermi energies [60] and magnetic moments [61]. Second, it has to be reminded that ab-initio calculations are usually performed in perfect crystals, thus the effect of intrinsic and extrinsic defects, off-stoichiometry, surfaces, secondary phases etc. is not normally taken into account. As an example, off-stoichiometric compositions and anti-site point defects were found to have great influence on the electronic properties of  $\text{Co}_2\text{VAl}$  [18] and  $\text{Co}_2\text{MnSi}$ ,  $\text{Co}_2\text{MnGe}$ ,  $\text{Co}_2\text{CrAl}$  half-metallic Heusler compounds [62,63]. Finally, it is also worth noting that the experimental magnetic characterizations reported in Figure 5 and Figure 6 suggest that a rather smooth profile of density of states is expected at the Fermi level for both alloys and this is confirmed by the calculated results.

Table 1: Band gap ( $E_g$ ) of the relaxed structures, formation energy ( $\Delta E_{\text{form}}$ ) per formula unit, magnetic moment in number of Bohr magnetons per formula unit ( $\mu$ ), Curie temperature ( $T_C$ ) and cell parameter ( $a$ ) for  $\text{Co}_2\text{HfSn}$  and  $\text{Co}_2\text{ZrSn}$  alloys. Band gap of  $\text{Co}_2\text{HfSn}$  with PBEsol is indicated in brackets because the Fermi energy is not inside the minority band gap.  $\mu$  values are reported both in the limit of neglected presence of secondary phases, and as they are considered Pauli paramagnets. \* Ref. [21,47–51]; § Ref. [47,48,50–55]. Values without reference are from this work.

<b><math>\text{Co}_2\text{HfSn}</math></b>					
	$E_g$ (eV)	$\Delta E_{\text{form}}/\text{f.u.}$ (eV)	$\mu/\text{f.u.}$ ( $\mu_B$ )	$T_C$ (K)	$a$ (Å)
PBE	0.30	-1.60	2.00	-	6.2498
PBEsol	(0.22)	-1.76	1.93	-	6.1641
Exp.	-	-	2.01-2.15 1.50-2.00*	432 430 [21]	6.2157 [27] 6.218 [48]
<b><math>\text{Co}_2\text{ZrSn}</math></b>					
	$E_g$ (eV)	$\Delta E_{\text{form}}/\text{f.u.}$ (eV)	$\mu/\text{f.u.}$ ( $\mu_B$ )	$T_C$ (K)	$a$ (Å)
PBE	0.34	-1.61	2.00	-	6.2843
PBEsol	0.30	-1.74	2.00	-	6.2029
Exp.	-	-	1.80-2.05 1.34-2.00§	454 448 [54]	6.2458 [27] 6.249 [48]

## 4. Conclusions

The magnetic and electronic properties of  $\text{Co}_2\text{ZrSn}$  and  $\text{Co}_2\text{HfSn}$  alloys were studied combining experimental investigations and ab-initio calculations. Theoretical data on the alloys were obtained by means of a plane-wave DFT approach, using two different exchange-correlation functionals (PBE and PBEsol), suitable for solid compounds. Calculated magnetic moments and densities of states suggest a half-metallic behaviour for both alloys. Overall, the calculated data were observed to be consistent when using different functionals, with the single exception of the PBEsol results for  $\text{Co}_2\text{HfSn}$ , whose Fermi level, and hence its magnetic moment, was found to be highly dependent on the variation of lattice parameter around the equilibrium value. The results of calculations were observed to be in good agreement with experimental data, both from this work and from literature. The origin of minor differences between experimental and theoretical results was analyzed and attributed to both computational and sample-dependent contributions, such as the underestimation of the calculated lattice parameter with the PBEsol functional or deviations from the ideal composition in the experimental samples. Besides, ab-initio calculations suggest that the magnetic behaviour of electrons near the Fermi level is due almost exclusively to Co atoms, suggesting that a fine tuning of the magnetic properties could be achieved by properly varying the Co content inside the alloys.

In conclusion, both alloys can be considered as weak itinerant ferromagnets over most of the investigated temperature intervals and are well described by the Edwards-Wohlfarth model, neglecting high-power terms of magnetization. This simple mean-field approach is able to explain the magnetic behaviour of both compounds over a wide range of temperatures and applied magnetic fields. The agreement between the experimental  $M(H)$  curves and the ones predicted by the model without making use of terms in higher powers of magnetization indicates that basically smooth profiles of the density of states are expected in proximity of the Fermi level for both compounds. The temperature dependence of spontaneous magnetization at low temperatures confirms the existence of a crossover from localized ferromagnetism to standard itinerant ferromagnetism. This can be related to a change in spin-flip mechanism possibly due to the presence of a half-metallic band gap at low temperatures as already observed for other Heusler compounds [30].



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