Search for a muonphilic scalar X_0 or vector X_1 via $J/\psi \rightarrow \mu^+\mu^- + \text{invisible decays at BESIII}$

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A light scalar X_0 or vector X_1 particles have been introduced as a possible explanation for the $(g-2)_{\mu}$ anomaly and dark matter phenomena. Using $(8.998 \pm 0.039) \times 10^9 J/\psi$ events collected by the BESIII detector, we search for a light muon philic scalar X_0 or vector X_1 in the processes $J/\psi \to \mu^+\mu^- X_{0,1}$ with $X_{0,1}$ invisible decays. No obvious signal is found, and the upper limits on the coupling $g'_{0,1}$ between the muon and the $X_{0,1}$ particles are set to be between 1.1×10^{-3} and 1.0×10^{-2} for the $X_{0,1}$ mass in the range of $1 < M(X_{0.1}) < 1000 \text{ MeV}/c^2$ at 90% credibility level.

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The Standard Model (SM) of particle physics has achieved remarkable successes as a highly predictive theory of fundamental particles and their interactions. Nonetheless, the SM is generally considered incomplete since it is unable to explain several important questions, anomalies, and phenomena [1–3]. One of the possible experimental evidences of physics beyond the SM is the persistent discrepancy of more than 3σ between the experimental observation and the SM prediction of the muon anomalous magnetic moment $(g-2)_{\mu}$ [4–6].

Extra U(1) groups have been added as minimal extensions to the SM to study new physics [7,8]. One of the notable extensions of the SM gauge group is the anomalyfree gauged $U(1)_{Lu-L\tau}$ model [9–11]. This model introduces a new massive vector boson X_1 , which only couples to the second and third generations of leptons $(\mu, \nu_{\mu}, \tau, \nu_{\tau})$ with the

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coupling strength g_1 . The X_1 can contribute to the muon anomalous magnetic moment and explain the $(g-2)_{\mu}$ anomaly [12]. Henceforth, we refer to the $U(1)_{Lu-L\tau}$ model, where X_1 only couples to the SM particles, as the "vanilla" $U(1)_{Lu-L\tau}$ model. The existence of dark matter (DM) and its observed abundance is one of the greatest mysteries in physics. Recent studies have revealed that an extended $U(1)_{Lu-L\tau}$ model, which introduces a dark matter particle with mass $M(\chi)$ and coupling to MeV-scale X_1 with the coupling strength g'_D , can also explain DM phenomena and the relic abundance of DM [13–17]. For $M(\chi) < M(X_1)/2$ and coupling ratios $g'_D/g'_1 \gg 1$, the dominant decay mode of the X_1 is invisible, $X_1 \to \chi \bar{\chi}$. We henceforth refer to the model with $\mathcal{B}(X_1 \to \chi \bar{\chi}) \approx 1$ as the "invisible" $U(1)_{Lu-L\tau}$ model. In addition to a vector boson scenario, an extra U(1)group involving a new light scalar boson X_0 , coupling to muons with coupling strength g'_0 , has been recently addressed [18-20]. This model can also serve as one possible explanation for the $(g-2)_{\mu}$ discrepancy within a specific $X_0 - g'_0$ parameter space. In the following, this model is denoted as the "scalar" U(1) model.

Stringent constraints on the visible decay of $X_1 \rightarrow \mu^+ \mu^$ have been obtained in the BABAR [21], CMS [22] and Belle [23] experiments. The parameter space with $10^{-3} < g_1' < 1$ in the mass range from the $\mu^+\mu^-$ threshold to 68 GeV/c^2 has been excluded. Moreover, since the "vanilla" $U(1)_{L\mu-L\tau}$ model modifies the neutrino interactions, there are also strong constraints on the g_1 coupling from neutrino trident $\nu N \rightarrow \nu N \mu^+ \mu^-$ scattering experiments [24–27]. Therefore, X_1 could weakly couple to the SM particles and predominantly decay to invisible final states, especially when the mass of $X_{0,1}$ is below $2m_{\mu}$. Recently, the invisible decays of X_1 have been investigated in the NA64-e [28] and Belle II [29,30] experiments. There is no direct result on the scalar boson X_0 , but it could be estimated based on the vector scheme [19]. BESIII offers significant advantages in searching for the low-mass $X_{0.1}$ particles via the $J/\psi \to \mu^+ \mu^- X_{0,1}$ decay, where the $X_{0,1}$ is radiated from one of the muons and then decays invisibly. First, BESIII has collected a large J/ψ data sample at the e^+e^- center-of-mass energy $\sqrt{s} = 3.097$ GeV [31].

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The corresponding cross section of $J/\psi \to \mu^+\mu^- X_{0,1}$ is approximately 22 times greater than that of the continuum $e^+e^- \to \mu^+\mu^- X_{0,1}$ process, which was previously employed in the search for X_1 at Belle II [20]. Second, the lower e^+e^- collider energy at BESIII leads to a better detection resolution, enabling a finer binning scheme in search of low-mass $X_{0,1}$. Additionally, the very narrow width of J/ψ results in a lower background level from the initial state radiation process. Hence, $J/\psi \to \mu^+\mu^-$ offers an ideal opportunity to search for muonic new physics particles [20].

In this paper, we perform a search for a light muon philic scalar X_0 or vector X_1 in the processes $J/\psi \to \mu^+\mu^- X_{0,1}$ with $X_{0.1} \rightarrow$ invisible, in the mass range from 1 to $1000 \text{ MeV}/c^2$, based on the data sample of 9 billion J/ψ events collected by the BESIII detector in 2009, 2018, and 2019 [31]. The data collected in 2012 is not used because information from the muon counter detectors is unavailable. Three SM extension models, including the "vanilla" $U(1)_{L\mu-L\tau}$ model, the "invisible" $U(1)_{L\mu-L\tau}$ model and the "scalar" U(1) model, are considered. In the vanilla $U(1)_{L\mu-L\tau}$ model, X_1 decays to neutrinos with the branching fraction $\mathcal{B}(X_{0.1} \to \nu \bar{\nu})$ varying from 33% to 100% depending on the X_1 mass [32]. In the invisible $U(1)_{Lu-L\tau}$ model, X_1 predominantly decays into light DM particles with a branching fraction $\mathcal{B}(X_1 \to \chi \bar{\chi}) \simeq 1$. In the scalar U(1) model, X_0 is long-lived with displaced decay or decays predominantly to invisible particles. For all models, it is assumed that the total width $\Gamma_{X_{0,1}}$ of the $X_{0.1}$ is negligible compared to the experimental resolution and so is set to zero. Therefore, we look for events with two final state muon tracks with missing energy. In the presence of the $X_{0,1}$ signals, narrow peaks would be visible in the recoil mass distribution of the $\mu^+\mu^-$ system. The branching fractions of the $J/\psi \to \mu^+ \mu^- X_{0.1}$, $X_{0.1} \to \text{invisible decays}$ are calculated as

$$\mathcal{B}(J/\psi\to\mu^+\mu^-X_{0,1})\times\mathcal{B}(X_{0,1}\to\text{invisible}) = \frac{N_{X_{0,1}}}{N_{J/\psi}\epsilon_{X_{0,1}}},$$
(1)

where $N_{X_{0,1}}$ are the signal yields, $N_{J/\psi} = (8.998 \pm 0.039) \times 10^9$ is the total number of J/ψ events, and $\epsilon_{X_{0,1}}$ are the signal efficiencies for the X_0 and X_1 cases, respectively. The values of the coupling $g'_{0,1}$ can be obtained by converting the results for the branching fractions [20].

The BESIII detector is described in detail elsewhere [33–35]. Simulated Monte Carlo (MC) samples produced with a Geant4-based [36] package are used to determine detection efficiencies and to estimate backgrounds. The signal events for the $J/\psi \to \mu^+\mu^-X_{0,1}$ with $X_{0,1} \to$ invisible decays are generated based on the theoretical

amplitude in Ref. [20] with EvtGen [37]. We generate signal MC samples at 58 different $X_{0,1}$ mass values with negligible width $\Gamma_{X_{0,1}}$, corresponding to mass hypotheses ranging from 1 to 1000 MeV/ c^2 in steps of 10 to 20 MeV/ c^2 depending on the resolution. Possible backgrounds are investigated using an inclusive MC sample including the production of the J/ψ resonance and the continuum processes. All particle decays are modeled with EvtGen using branching fractions either taken from the Particle Data Group [38], when available, or otherwise estimated with LUNDCHARM [39]. The background from $e^+e^- \rightarrow \mu^+\mu^-$ events is modeled with BABAYAGA [40]. Final state radiation is simulated with the Photos package [41].

The signal candidates include $\mu^+\mu^-$ tracks and missing energy in the final states. Each charged track is required to be within a polar angle (θ) range of $|\cos \theta| < 0.93$ and the distance of closest approach to the interaction point must be less than 10 cm along the z-axis, and less than 1 cm in the transverse plane. To exclude the cosmic ray events, the momentum of each track is required to be less than 1.55 GeV/c, and the time difference in time-of-flight system (TOF) between two tracks is required to be within $|\Delta t_{\text{TOF}}| < 2$ ns. Events with additional charged tracks reconstructed in the main drift chamber (MDC) are rejected to exclude background from particles with displaced decays, such as K_S^0 and γ -conversion events. Moreover, to distinguish muons from electrons, pions, and kaons, a track is identified as a muon by the following requirements: (1) particle identification (PID) likelihoods, formed by combining the measurements of the energy deposited in the MDC and the flight time in the TOF, satisfy $\mathcal{L}(\mu) > \mathcal{L}(K)$ and $\mathcal{L}(\mu) > 0$, where $\mathcal{L}(\mu)$ and $\mathcal{L}(K)$ are likelihoods calculated based on the muon and kaon hypotheses, respectively; (2) the penetration depth of each track in the muon counters (MUC) is required to exceed $[-40.0 + 70 \times p/(\text{GeV}/c)]$ cm for $0.5 \le p \le 1.1 \text{ GeV}/c$, and to be greater than 40 cm for p > 1.1 GeV/c, where p is the momentum of each charged track; and (3) the deposited energy $E_{\rm EMC}(\mu)$ in the electromagnetic calorimeter (EMC) is required to be within (0.1, 0.3) GeV.

We split the events that pass the above selections into two groups, labeled the low mass region and the high mass region. The following selection criteria are optimized for the X_0 and X_1 searches in the low and high mass regions, respectively. In the low mass region, the signals are identified in the recoil mass squared $M^2_{\rm recoil}(\mu^+\mu^-) = (p_{J/\psi} - p_{\mu^+} - p_{\mu^-})^2$ distribution since $M^2_{\rm recoil}(\mu^+\mu^-)$ can be negative due to detector resolution, where the $p_{J/\psi}$ [31], p_{μ^+} , and p_{μ^-} are the four-momenta of J/ψ , μ^+ , and μ^- particles, respectively. This region is defined as $M^2_{\rm recoil}(\mu^+\mu^-) < 0.3~{\rm GeV}^2/c^4$, which is used to search for signals with mass $M(X_{0,1}) < 0.4~{\rm GeV}/c^2$. The dominant backgrounds in this region are composed of two final state muons from the $J/\psi \to \mu^+\mu^-(\gamma)$ and

 $e^+e^- o \mu^+\mu^-(\gamma)$ processes, where the photons are from initial and final state radiation. The high mass region is defined as $M_{\rm recoil}(\mu^+\mu^-) \in [0.25, 1.0]~{\rm GeV}/c^2$ and is used to search for the signal with mass $M(X_{0,1}) \in [0.4, 1.0]~{\rm GeV}/c^2$ in the recoil mass distribution. The region $M_{\rm recoil}(\mu^+\mu^-) > 1.0~{\rm GeV}/c^2$ is not studied in this work due to poor understanding of the background. In addition to the background from $J/\psi \to \mu^+\mu^-(\gamma)$ and $e^+e^- \to \mu^+\mu^-(\gamma)$ processes, a significant background comes from $J/\psi \to K_L^0\pi^+\pi^-$ decays, where the K_L^0 particle is undetected due to its long decay length.

The common selection criteria for all events are described below. We require the events with the polar angle of the momentum of $\mu^+\mu^-$ system $\cos(\theta_{\mu^+\mu^-})$ within the barrel EMC region $\cos(\theta_{\mu^+\mu^-})$ \in [-0.76, 0.76], to reject the inefficient region of photon detection. The events within $\cos(\theta_{u^+u^-}) \in [-0.03, 0.03]$, where photons easily escape due to the crystals being placed perpendicular to the beam direction, are further excluded. Additionally, the invariant mass of $\mu^+\mu^-$ pairs is required to be outside the mass windows of $M(\mu^{+}\mu^{-}) \in [0.429, 0.481] \text{ GeV}/c^{2}$ and $M(\mu^{+}\mu^{-}) \in [0.548, 0.780] \text{ GeV}/c^{2}$, to further suppress the backgrounds with $K_S^0 \to \pi^+\pi^-$ and $K^* \to K^{\pm}\pi^{\mp}$ decays, respectively. The signal processes have two final state muons; to suppress the background with additional final state photons, the total deposited energy E_{tot} (EMC) in the EMC from all showers in each event is required to be less than 43 MeV (50 MeV) for the low (high) mass region. For these showers, the difference between the EMC time and the event start time is required to be within [0, 700] ns to minimize the impact of electronic noise and showers unrelated to the event. In each event, we require the cosine of the opening angle in the J/ψ rest frame to satisfy $\cos(\alpha_{\mu^+\mu^-}) > -0.97$ (0.96) for the X_1 (X_0) case in the low mass region and $\cos(\alpha_{\mu^+\mu^-}) > -0.97$ for both cases in the high mass region to suppress background from $J/\psi \rightarrow$ $\mu^+\mu^-$ and $e^+e^- \rightarrow \mu^+\mu^-$ processes. In the high mass region, the background from $J/\psi \to K^{\pm}K^{*\mp}$ with $K^{*\mp} \to$ $K_L^0 \pi^{\mp}$ decays is suppressed by requiring the muon-hypothesis recoil mass $M_{\text{recoil}}(\mu^{\pm}) = |p_{J/\psi} - p_{\mu^{\pm}}|$ to be outside $(0.858, 1.172) \text{ GeV}/c^2$.

To investigate possible signals from $X_{0,1}$, we perform a series of unbinned maximum likelihood fits to $M_{\rm recoil}^2(\mu^+\mu^-)$ for the low mass region and to $M_{\rm recoil}(\mu^+\mu^-)$ for the high mass region. The fits are performed in the mass region of $1 < M(X_{0,1}) < 1000~{\rm MeV}/c^2$, with steps of 10–20 MeV/ c^2 (about half of the signal resolution). The resulting signal efficiency obtained from signal MC samples varies between 1%–20% as a function of $M(X_{0,1})$. In the low mass region, the residual backgrounds are from $J/\psi \to \mu^+\mu^-\gamma$, $e^+e^- \to \mu^+\mu^-\gamma$, and $J/\psi \to {\rm hadrons}$ processes. The yields and probability density functions for the peaking backgrounds from $J/\psi \to \mu^+\mu^-$ and $e^+e^- \to \mu^+\mu^-$ are fixed from the corresponding MC simulation in these fits. The

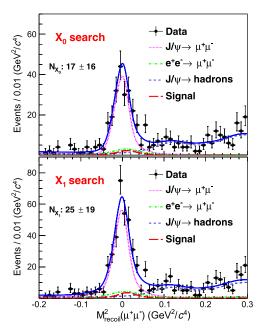


FIG. 1. Fits to the $M^2_{\rm recoil}(\mu^+\mu^-)$ distributions for the X_0 (top) and X_1 (bottom) candidates with mass $M(X_{0,1})=120~{\rm MeV}/c^2$. The red long-dashed curves are the $X_{0,1}$ signal shapes. The green dashed and magenta dotted curves are the peaking backgrounds from $J/\psi \to \mu^+\mu^-$, $e^+e^- \to \mu^+\mu^-$ processes. Dots with error bars are data, and the blue dashed curves are the backgrounds from $J/\psi \to {\rm hadrons}$ processes.

shape of non-peaking background from J/ψ hadronic decays is constructed from the corresponding MC simulation with a yield that is left as a free parameter in the fit. The signal shapes are described as a templated shape constructed from the $X_{0,1}$ signal MC simulations. As an example, Fig. 1 shows the fit results for the $X_{0,1}$ candidates with mass $M(X_{0,1}) = 120 \text{ MeV}/c^2$. For the high mass region, the signals with mass $M(X_{0.1}) > 0.4 \text{ GeV}/c^2$ are searched for in the $M_{\text{recoil}}(\mu^+\mu^-)$ distribution, and the residual backgrounds are dominated by the J/ψ decays with K_I^0 in the final state, which are described by a secondorder Chebychev function. The signal shapes are constructed from the corresponding $X_{0,1}$ signal MC simulations. The fits to the $M_{\text{recoil}}(\mu^+\mu^-)$ distributions with mass $M(X_{0.1}) = 720 \text{ MeV}/c^2$ are shown in Fig. 2. Taking into account the uncertainty from the background model, the maximum local significance among all the fits is determined to be 2.5 σ at $M(X_{0.1}) = 720 \text{ MeV}/c^2$, as shown in Fig. 2. The significances are calculated by comparing the likelihoods with and without the signal components in the fit, and considering the change of the number of degrees of freedom. We find no evidence for signals from $X_{0,1}$ invisible decays.

The systematic uncertainty sources for the coupling $g'_{0,1}$ measurement include the total number of J/ψ events, the signal efficiency, the signal extraction, and the J/ψ total

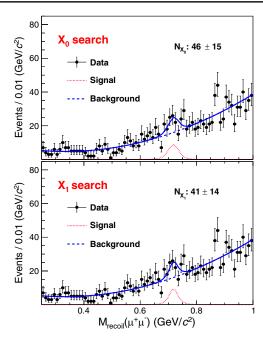


FIG. 2. Fits to the $M_{\rm recoil}(\mu^+\mu^-)$ distributions for the X_0 (top) and X_1 (bottom) candidates with mass $M(X_{0,1})=720~{\rm MeV}/c^2$. The red dotted curves are the $X_{0,1}$ signal shapes. Dots with error bars are data, and the blue dashed curves describe the combinatorial background contribution. The data points on the two plots are identical due to identical selection criteria for X_0 and X_1 .

width. The uncertainty from the total number of J/ψ events is 0.4% [31]. The uncertainty from the tracking efficiency is taken as 1.0% per track [42]. The uncertainty associated with the $E_{\rm EMC}(\mu)$ requirement is 0.2% [42]. The systematic uncertainties from the requirements on Δt_{TOF} , $E_{tot}(EMC)$ and additional tracks in the MDC are estimated with a $J/\psi \to \mu^+\mu^-$ control sample. The resulting differences in the efficiencies between data and MC simulation are 1.0% for Δt_{TOF} , 1.5% for $E_{\text{tot}}(\text{EMC})$, and negligible for the requirement on the additional tracks. The uncertainties due to the requirements on PID and MUC penetration depth are investigated with a $J/\psi \rightarrow \gamma \mu^+ \mu^-$ control sample with tagged photon. The signal MC events are weighted by the difference in efficiency between data and MC simulation. It causes 1.0% and (1.0 - 3.0)% changes in signal efficiencies for PID and penetration depth requirement depending on the mass of $X_{0,1}$. In the fits for the low mass region, the uncertainty from the simulated yields of the peaking background is estimated to be 18.8% and 16.8% for X_0 and X_1 , respectively, using the selected $J/\psi \rightarrow$ $\gamma \mu^+ \mu^-$ control sample. To account for these uncertainties, alternative fits are performed by varying the background yields upward or downward by their corresponding uncertainties. For the high mass region, the uncertainty associated with the background model is also considered by an alternative fit with the background described by a thirdorder polynomial shape. Among these fits, the one with the largest upper limit on the signal yield is treated as the final result. The systematic uncertainty from the resolution difference between data and MC simulation is determined to be 1.0% using a control sample of $J/\psi \to K_S^0 K_L^0$ events. Considering that the cross section of the $e^+e^- \rightarrow \mu^+\mu^$ process is 4.4% of the $J/\psi \rightarrow e^+e^-$ one [43], and taking into account the efficiency difference between $e^+e^- \rightarrow$ $\mu^+\mu^-X_{0,1}$ and $J/\psi \to \mu^+\mu^-X_{0,1}$, the uncertainties for the contributions from the $e^+e^- \to \mu^+\mu^- X_0$ and $e^+e^- \to$ $\mu^+\mu^-X_1$ processes are determined to be 3.5% and 3.9%, respectively. The uncertainty associated with the total width of J/ψ is 1.8% [38]. Assuming all these sources as independent, the total systematic uncertainty is obtained by adding the individual contributions in quadrature, resulting in (5.0 - 5.4)% and (5.5 - 5.8)% for X_0 and X_1 , respectively.

Since no obvious signal is observed, the upper limits on the product branching fractions $\mathcal{B}(J/\psi \to \mu^+\mu^- X_{0.1}) \times$ $\mathcal{B}(X_{0,1} \to \text{invisible})$ in Eq. (1) are determined at the 90% credibility level (C.L.) depending on the mass $M(X_{0.1})$ with Bayesian method. We perform a likelihood scan by conducting a series of fits under different hypotheses for the number of $X_{0,1}$. The effect of the systematic uncertainty is considered by convolving the likelihood curve with a Gaussian function with its standard deviation set to the total systematic uncertainty [44,45]. The resulting 90% C.L. upper limits on $\mathcal{B}(J/\psi \to \mu^+\mu^- X_{0,1}) \times \mathcal{B}(X_{0,1} \to \text{invisible})$ are determined to be $6.2 \times 10^{-9} - 5.5 \times 10^{-7}$ and 4.5×10^{-7} $10^{-9} - 9.6 \times 10^{-7}$ for the cases of X_0 and X_1 as functions of $M(X_{0,1})$, respectively. The results on the branching fractions are used to estimate limits on the coupling $g'_{0,1}$ [20]. The excluded region in the $g'_{0,1}$ versus $M(X_1)$ parameter space at the 90% C.L. is shown in Fig. 3. For the vanilla $L_{\mu} - L_{\tau}$ model, BESIII excludes g'_1 values in the range $1.6 \times 10^{-3} - 7.9 \times 10^{-3}$ as a function of $M(X_1)$ after taking $\mathcal{B}(X_1 \to \nu \bar{\nu})$ into account. For the invisible scenario, g_1 values in the range $1.1 \times 10^{-3} - 5.5 \times 10^{-3}$ with $1 \le$ $M(X_1) \le 1000 \,\mathrm{MeV}/c^2$ are excluded. We obtain a better sensitivity in the range 200–860 MeV/ c^2 compared to the Belle II results [29,30], and a comparable upper limit in the lower mass region with a finer binning scheme. The best constraint for the mass region $M(X_1) < 10 \text{ MeV}/c^2$ is provided in the NA64-e experiment [28]. For the "scalar" X_0 case, there are no earlier experimental measurements; the 90% C.L. upper limits on the coupling g'_0 is determined to be $2.3 \times 10^{-3} - 1.0 \times 10^{-2}$ with $M(X_0)$ in the range 1–1000 MeV/ c^2 .

In summary, we have searched for a muon philic scalar X_0 or vector X_1 boson, introduced by many SM extension models, using a data sample of 9 billion J/ψ events at BESIII. No evidence of $X_{0,1}$ has been observed in the mass range $1 < M(X_{0,1}) < 1000 \text{ MeV}/c^2$, and the 90% C.L. upper limits on the coupling $g'_{0,1}$ are set to be in the range of $1.1 \times 10^{-3} - 1.0 \times 10^{-2}$ for three SM extension models.

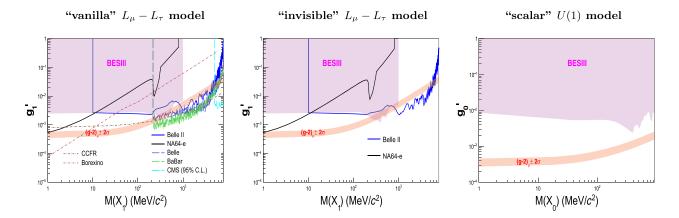


FIG. 3. The 90% C.L. upper limits on the coupling $g_{0,1}$ for the vanilla $L_{\mu}-L_{\tau}$ model, the invisible $L_{\mu}-L_{\tau}$ model, and the "scalar" U(1) model. For the "vanilla" $L_{\mu}-L_{\tau}$ model, the previous excluded regions by BABAR [21], CMS [22], and Belle [23] via the $X_1 \to \mu^+\mu^-$ decay and the constraints from neutrino experiments [24–27] are shown for comparison. For the invisible $L_{\mu}-L_{\tau}$ model, the previous searches for X_1 invisible decays by NA64-e [28] and Belle II [29,30] are also presented. The red bands represent the parameter regions favored by the $(g-2)_{\mu}$ anomaly within 2σ [20].

To date, we provide the best constraint for the X_1 mass in the range 200–860 MeV/ c^2 in the invisible $L_\mu - L_\tau$ model, and two mass regions within 320 < $M(X_1)$ < 410 MeV/ c^2 and 460 < $M(X_1)$ < 520 MeV/ c^2 are excluded to explain the $(g-2)_\mu$ anomaly at the 90% C.L. For the scalar X_0 , we have performed the first direct experiment search, and set the upper limit at the 90% C.L. on the coupling g_0 to 2.3 × $10^{-3} - 1.0 \times 10^{-2}$ for $1 < M(X_0) < 1000$ MeV/ c^2 .

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