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Measurement of the $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ cross sections from $\sqrt{s} = 2.000$ to 3.080 GeV



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ABSTRACT: Based on e^+e^- collision data collected at center-of-mass energies from 2.000 to 3.080 GeV by the BESIII detector at the BEPCII collider, a partial wave analysis is performed for the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$. The results allow the Born cross sections of the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, as well as its subprocesses $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ and $K_2^*(1430)^0 \bar{K}^0$ to be measured. The Born cross sections for $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ are consistent with previous measurements by BaBar, but with substantially improved precision. The Born cross section lineshape of the process $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ is consistent with a vector meson state around 2.2 GeV with a significance of 3.2σ . A Breit-Wigner fit determines its mass as $M_Y = (2164.7 \pm 9.1 \pm 3.1) \text{ MeV}/c^2$ and its width as $\Gamma_Y = (32.4 \pm 21.0 \pm 1.8) \text{ MeV}$.

KEYWORDS: e^+e^- Experiments, Particle and Resonance Production, Spectroscopy

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1 Introduction

The vector meson state $Y(2175)$, denoted as $\phi(2170)$ by the Particle Data Group [1], is one of the more interesting particles in the field of light-flavored hadron spectroscopy. It was first observed by the BaBar collaboration [2] and subsequently investigated by the Belle, BES and BESIII collaborations [3–13]. Several interpretations have been proposed for the $\phi(2170)$ state, such as a conventional 3^3S_1 or 2^3D_1 $s\bar{s}$ state [14–17], a $s\bar{s}g$ hybrid [18, 19], a tetraquark state [20–23], a $\Lambda\bar{\Lambda}(^3S_1)$ bound state [24–26], and a $\phi K\bar{K}$ resonance state [27].

Studies of the $\phi(2170)$ have been carried out using various final states such as $\phi\eta$ [7, 28], $\phi\eta'$ [8], $\phi f_0(980)$ [2–6, 9, 29], K^+K^- [10, 30, 31], $K_S^0K_L^0$ [11, 32], $K^*(892)^+K^-$ [12], $K_2^*(1430)^+K^-$ [12], $K^*(892)^+K^*(892)^-$ [13] and other charged excited $K\bar{K}$ states [13]. None of these final states is dominant, and the product of the e^+e^- partial width and the branching fraction (BF) of each final state is consistently below 100 eV. The partial decay width $\Gamma(\phi\eta)$ [7, 28] is less than $\Gamma(\phi\eta')$ [8], which disfavors the hybrid interpretation [18, 19]. This result can be explained by the hadronic transition of a strangeonium-like meson along with $\eta-\eta'$ mixing [33]. The partial width of $K^*(892)^+K^*(892)^-$ is significantly greater than that of $K_1(1400)^+K^-$, as predicted for the 2^3D_1 or 3^3S_1 state [14–17]. However, the BESIII collaboration has observed a clear structure in the cross section line shape of $K_1(1400)^+K^-$ around 2.2 GeV [13], but no enhancement in the cross section line shape for $K^*(892)^+K^*(892)^-$ [13], which disfavors the 2^3D_1 or 3^3S_1 prediction. The BESIII collaboration has also measured a larger partial width of $K_2^*(1430)^+K^-$ compared to $K^*(892)^+K^-$ at center-of-mass (c.m.) energies (\sqrt{s}) from 2.000 to 3.080 GeV [12], which contradicts the prediction that the $\phi(2170)$ is the 2^3D_1 strangeonium state [16]. More precise measurements of the decay properties of the $\phi(2170)$ are desirable to better understand the nature of the $\phi(2170)$.

The $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ [34] and $e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp$ [28] processes have been investigated by the BaBar collaboration using the initial state radiation (ISR) technique. A Dalitz amplitude analysis was performed for $e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp$, leading to the determination of the isoscalar and isovector cross sections for $K^*(892)\bar{K}$. A distinct asymmetry between neutral and charged channels is observed in the Dalitz plot for $K_S^0 \pi^\mp$ and $K^\pm \pi^\mp$ within $\sqrt{s'} = 2-3$ GeV. It may be related to a similar effect observed in the radiative decay rates of the neutral and charged $K_2^*(1430)$ [28]. The SND collaboration has studied $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ at $\sqrt{s} = 1.3 - 2.0$ GeV, and the cross sections have been measured at a statistical uncertainty level of 10%-30% [35].

In this paper, we present a partial wave analysis (PWA) of the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ based on 19 data samples collected by the BESIII experiment, ranging from $\sqrt{s} = 2.000$ to 3.080 GeV and corresponding to an integrated luminosity of 647 pb^{-1} [36, 37]. The Born cross section of the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ and its sub-processes $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ and $K_2^*(1430)^0 \bar{K}^0$ are measured. Throughout the paper charge conjugated processes are also included by default.

2 BESIII detector and Monte Carlo simulation

The BESIII detector [38] records symmetric e^+e^- collisions provided by the BEPCII storage ring [39], which operates with a peak luminosity of $1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ in the range of \sqrt{s} from 2.0 to 4.95 GeV. BESIII has collected large data samples in this energy region [40]. The cylindrical core of the BESIII detector covers 93% of the full solid angle and consists of a helium-based multilayer drift chamber (MDC), a plastic scintillator time-of-flight system (TOF), and a CsI(Tl) electromagnetic calorimeter (EMC), which are all enclosed in a superconducting solenoidal magnet providing a 1.0 T (0.9 T in 2012) magnetic field. The solenoid is supported by an octagonal flux-return yoke with resistive plate counter muon identification modules interleaved with steel. The charged-particle momentum resolution at 1 GeV/c is 0.5%, and the dE/dx resolution is 6% for electrons from Bhabha scattering. The EMC measures photon energies with a resolution of 2.5% (5%) at 1 GeV in the barrel (end cap) region. The time resolution in the TOF barrel region is 68 ps, while that in the end cap region is 110 ps.

Simulated samples produced with GEANT4 based [41] Monte Carlo (MC) software, which includes the geometric description [42] of the BESIII detector and the detector response, are used to optimize the event selection criteria, estimate backgrounds, and determine the detection efficiency. The signal MC samples for the processes $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, $K^*(892)^0 \bar{K}^0$ and $K_2^*(1430)^0 \bar{K}^0$ are generated by CONEXC [43] using an amplitude model with parameters fixed to the PWA results. For background studies, inclusive hadronic events are generated with a hybrid generator that includes CONEXC, LUARLW [44] and PHOKHARA [45].

3 Event selection and background analysis

The signal process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ is reconstructed with $K_S^0 \rightarrow \pi^+ \pi^-$, $\pi^0 \rightarrow \gamma \gamma$, and K_L^0 treated as a missing particle. Signal candidates are required to have two charged pions with zero net charge and at least two photons.

Charged tracks detected in the MDC are required to be within a polar angle (θ) range of $|\cos \theta| < 0.93$. Here, θ is defined with respect to the z -axis, which is the symmetry axis of the MDC. Each K_S^0 candidate is reconstructed from two oppositely charged tracks satisfying that the distance of closest approach to the interaction point (IP) must be less than 20 cm along the z -axis. The two charged tracks are assigned as $\pi^+\pi^-$ without imposing further particle identification criteria. They are constrained to originate from a common vertex and are required to have an invariant mass within $|M(\pi^+\pi^-) - m_{K_S^0}| < 12 \text{ MeV}/c^2$, where $M(\pi^+\pi^-)$ is the invariant mass of $\pi^+\pi^-$ pair with kinematics updated by the vertex fit and $m_{K_S^0}$ is the K_S^0 nominal mass [1]. The decay length of the K_S^0 candidate is required to be greater than twice the vertex resolution away from the IP.

Photon candidates are identified using showers in the EMC. The deposited energy of each shower must be more than 25 MeV in the barrel region ($|\cos \theta| < 0.80$) and more than 50 MeV in the end cap region ($0.86 < |\cos \theta| < 0.92$). To exclude showers that originate from charged tracks, the angle subtended by the EMC shower and the position of the closest charged track at the EMC must be greater than 10° as measured from the IP. To suppress electronic noise and showers unrelated to the event, the difference between the event start time and the EMC time of the photon candidate is required to be within $[0, 700]$ ns.

To suppress background and improve the kinematic resolution, a one-constraint (1C) kinematic fit imposing energy-momentum conservation is carried out under the $K_S^0 K_L^0 \gamma \gamma$ hypothesis with K_L^0 treated as a missing particle. If there are more than two photons in an event, the combination with the minimum χ_{1C}^2 is retained for further analysis, and candidate events are required to satisfy $\chi_{1C}^2 < 30$. To suppress the contamination from the process $e^+e^- \rightarrow \gamma_{\text{ISR}} K_S^0 K_L^0$, an additional 1C kinematic fit is performed under the hypothesis of $\gamma K_S^0 K_L^0$, and only events which satisfy $\chi_{1C}^2 < \chi_{1C}^2(\gamma K_S^0 K_L^0)$ are retained. To remove K_L^0 showers in the EMC that could be mistaken as photons, the angles between the candidate EMC shower and the K_L^0 momentum after the kinematic fit are required to be greater than 20° . Each signal candidate is required to have the invariant mass of the two photons within the π^0 mass region ($|M(\gamma\gamma) - m_{\pi^0}| < 0.015 \text{ GeV}/c^2$).

Potential background sources are studied by analyzing inclusive $e^+e^- \rightarrow$ hadrons and exclusive $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$, $K_S^0 K^\pm \pi^\mp \pi^0$ and $K_S^0 K_L^0 \pi^0 \pi^0$ MC samples after applying the same event selection criteria. The dominant background process is $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$. Exclusive $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$ events are generated by PHOKHARA [45] based on the results of the BaBar collaboration [46]. The $e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp \pi^0$ and $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0 \pi^0$ events are generated by CONEXC based on the dressed cross sections for $e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp \pi^0$ and $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0 \pi^0$ from the BaBar experiment [34, 47] with a phase space model and re-weighted to improve the agreement with BESIII data using a multidimensional gradient-boosting algorithm (HEPML) [48], respectively. The exclusive $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$, $K_S^0 K^\pm \pi^\mp \pi^0$ and $K_S^0 K_L^0 \pi^0 \pi^0$ samples, which have been normalized to the experimental integrated luminosity, are used to evaluate the numbers of background events. The contribution of K_S^0 peaking background events from $e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp \pi^0$ and $K_S^0 K_L^0 \pi^0 \pi^0$ is at a level of 0.1% – 0.4% for different energy points, which is negligible in the following fit. The background levels are summarized in table 1. Figure 1 shows distributions of the invariant masses of $\pi^+\pi^-$, $M(\pi^+\pi^-)$ and $\gamma\gamma$, $M(\gamma\gamma)$ without the K_S^0 and π^0 mass window requirements, respectively.

\sqrt{s} (GeV)	Background level	Peaking level
2.0000	5.4%	0.1%
2.0500	5.2%	0.1%
2.1000	6.9%	0.1%
2.1250	6.8%	0.1%
2.1500	6.4%	0.1%
2.1750	5.8%	0.1%
2.2000	6.1%	0.1%
2.2324	6.3%	0.1%
2.3094	6.9%	0.1%
2.3864	6.9%	0.1%
2.3960	7.1%	0.2%
2.6444	8.1%	0.2%
2.6464	8.4%	0.4%
2.9000	8.1%	0.4%
2.9500	9.4%	0.4%
2.9810	8.7%	0.2%
3.0000	7.2%	0.3%
3.0200	8.3%	0.2%
3.0800	8.4%	0.2%

Table 1. Summary of the background level for each \sqrt{s} .

Non- K_S^0 events are characterized by a flat shape in $M(\pi^+\pi^-)$ and are estimated with the events in the K_S^0 sideband, which is defined by $0.022 < |M(\pi^+\pi^-) - m_{K_S^0}| < 0.035$ GeV/ c^2 .

The signal yields of the $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ process are obtained by performing an unbinned maximum likelihood fit to the $M(\pi^+\pi^-)$ spectrum. The signal component is described by the signal MC-simulated shape convolved with a Gaussian function which describes the difference between data and MC simulation. The mean value and width of the Gaussian function are separately floated parameters at different energy points. The background function is parameterized by a first-order polynomial function. The corresponding fit results for data taken at $\sqrt{s} = 2.125$ and 2.900 GeV are shown in figure 2. The same event selection criteria and fit procedure are applied for all data samples at the nineteen c.m. energies.

In order to improve the resolution of kinematic variables, the remaining $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ events are subjected to a three-constraint (3C) kinematic fit, which, in addition to imposing energy and momentum conservation, further constrains the π^0 and K_S^0 masses to their PDG values [1]. After all above criteria, the invariant mass spectra of $K_S^0 K_L^0$, $K_S^0 \pi^0$, $K_L^0 \pi^0$ and the invariant masses squared of $K_S^0 \pi^0$ versus $K_L^0 \pi^0$ are shown in figure 3, where the $K^*(892)^0$ structure is clear. For the invariant mass spectra of $K_S^0 K_L^0$, $K_S^0 \pi^0$ and $K_L^0 \pi^0$, the

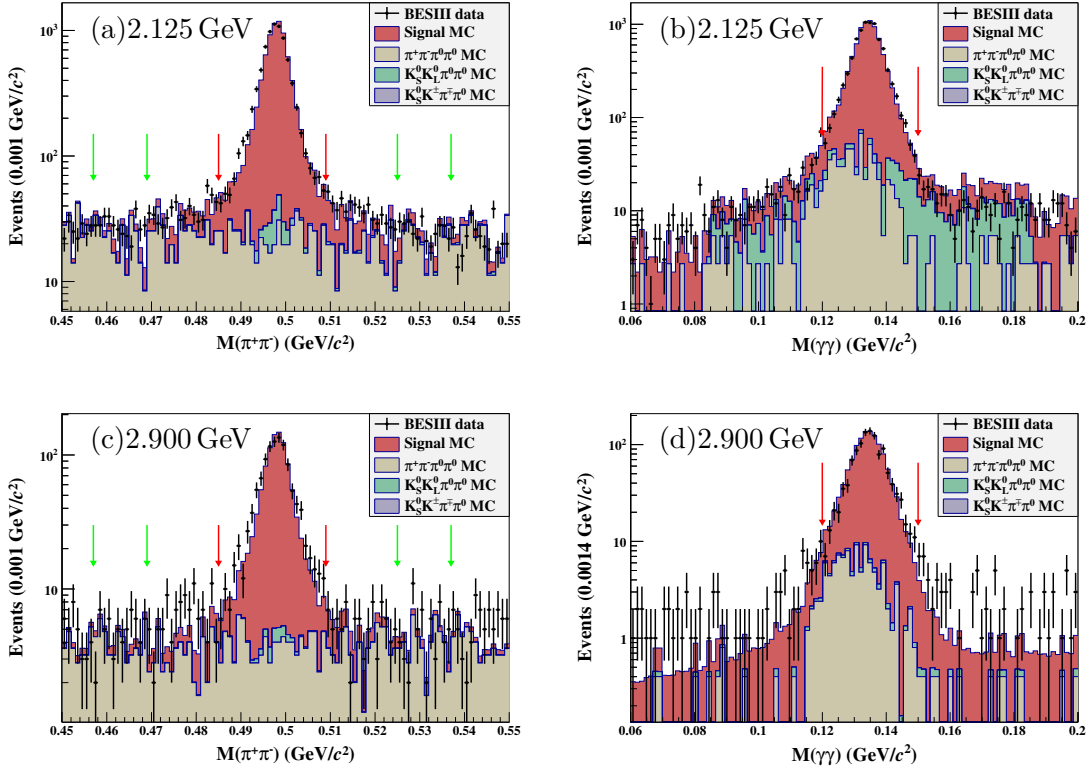


Figure 1. Distributions of (a),(c) $M(\pi^+\pi^-)$ with π^0 mass window requirement and (b),(d) $M(\gamma\gamma)$ at $\sqrt{s} = 2.125$ and 2.900 GeV, where the (black) dots with error bars are data, and the shaded histogram are the stacked MC samples of the signal process, $\pi^+\pi^-\pi^0\pi^0$, $K_S^0 K_L^0 \pi^0 \pi^0$ and $K_S^0 K^\pm \pi^\mp \pi^0$. The region between red arrows is the signal region, and the regions between the green arrows are the sideband regions.

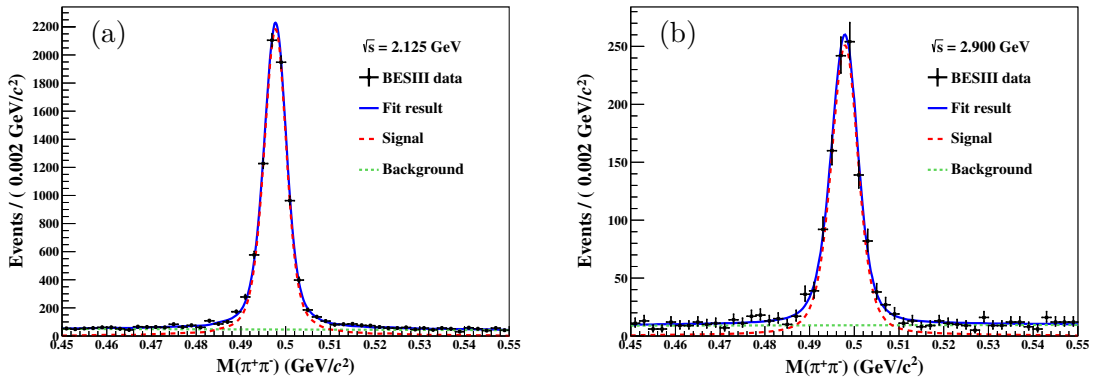


Figure 2. Fit to the $M(\pi^+\pi^-)$ distribution at $\sqrt{s} = 2.125$ and 2.900 GeV, where the black dots with error bars are data, the blue solid curve is the total fit result, the green dashed curve indicates the fitted background shape, and the red dashed curve is the fitted signal shape.

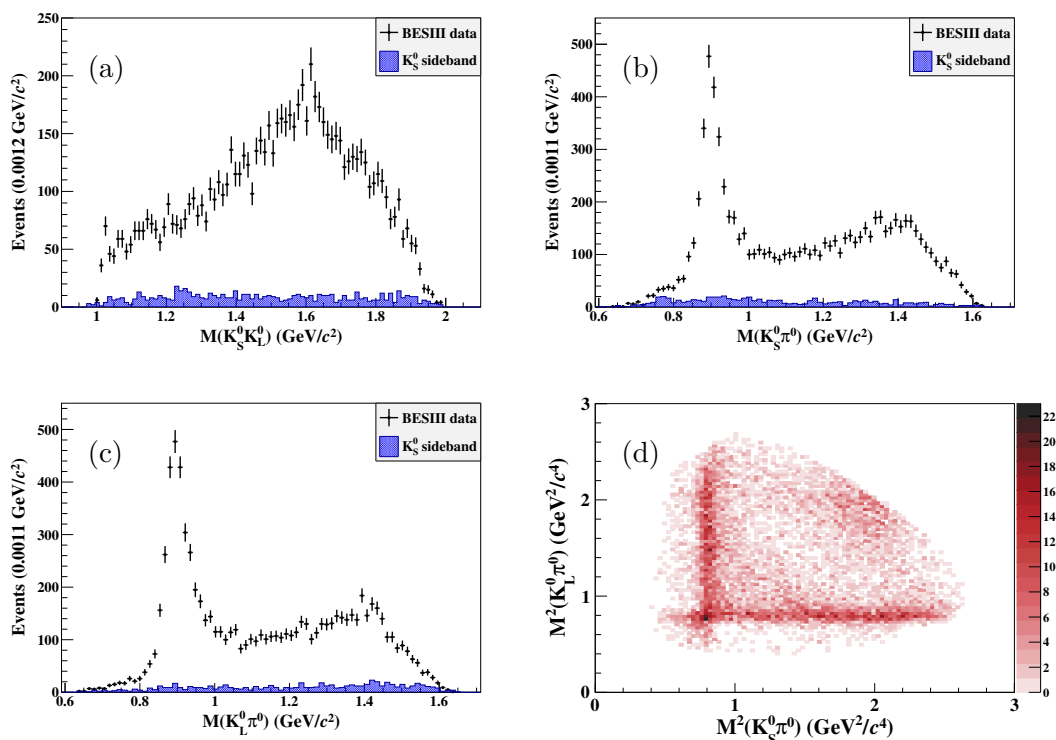


Figure 3. Distributions of (a) $M(K_S^0 K_L^0)$, (b) $M(K_S^0 \pi^0)$ and (c) $M(K_L^0 \pi^0)$, where the (black) dots with error bars are data, and the shaded histograms are non- K_S^0 events estimated by the K_S^0 sideband. (b) Distribution of $M^2(K_S^0 \pi^0)$ versus $M^2(K_L^0 \pi^0)$. All plots are based on data at $\sqrt{s} = 2.125$ GeV.

contributions of background events which are obtained by the K_S^0 sideband are smooth and confirm that there is no peaking structure. Those non- K_S^0 events are used to estimate the background contributions and those K_S^0 peaking backgrounds are negligible in the following amplitude analysis.

4 Amplitude analysis

Based on the GPUPWA framework [49], a PWA is performed on the surviving candidate events to identify the intermediate processes present in $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$. The quasi-two-body decay amplitudes in the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ with two sequential decays $e^+e^- \rightarrow R_1 \pi^0 \rightarrow K_S^0 K_L^0 \pi^0$ and $e^+e^- \rightarrow K_S^0 (K_L^0) R_2 \rightarrow K_S^0 K_L^0 \pi^0$ are considered and constructed using the covariant tensor amplitude formalism [50], where R_1 and R_2 are the intermediate states that can decay to $K_S^0 K_L^0$ and $K_S^0 (K_L^0) \pi^0$, respectively.

According to ref. [50], the general form for the decay amplitude of a 1^- state (Y) is

$$A(m) = Y_\mu(m) A^\mu = Y_\mu(m) \sum_i \Lambda_i U_i^\mu, \quad (4.1)$$

where $Y_\mu(m)$ is the polarization vector of Y , m is the spin projection of Y , and U_i^μ is the i -th partial-wave amplitude with coupling strength determined by a complex parameter Λ_i . The amplitude U_i^μ is constructed with the spin factor, Blatt-Weisskopf barrier factors

and propagators of resonances under the assumption of isobar model [50]. The differential cross-section can be written as

$$\frac{d\sigma}{d\Phi_n} = \frac{1}{2} \sum_m A^\mu A^{*\mu} = \frac{1}{2} \sum_{i,j} \Lambda_i \Lambda_j^* \sum_m U_i^\mu U_j^{*\mu}. \quad (4.2)$$

The spin factor is constructed with the covariant Zemach (Rarita-Schwinger) tensor formalism [50–53] by combining pure-orbital-angular-momentum covariant tensors $\tilde{t}_{\mu_1 \dots \mu_L}^{(L)}$ and the momenta of parent particles together with Minkowski metric $g_{\mu\nu}$ and Levi-Civita symbol $\epsilon_{\mu\nu\lambda\sigma}$. For a process $a \rightarrow bc$, the covariant tensors $\tilde{t}_{\mu_1 \dots \mu_L}^{(L)}$ for the final states of pure orbital angular momentum L are

$$\tilde{t}_{\mu_1 \dots \mu_L}^{(L)} = (-1)^L P_{\mu_1 \dots \mu_L \mu'_1 \dots \mu'_L}^{(L)}(p_a) r^{\mu'_1 \dots \mu'_L} B_L(Q_{abc}), \quad (4.3)$$

where $r = p_b - p_c$, $P_{\mu_1 \dots \mu_L \mu'_1 \dots \mu'_L}^{(L)}(p_a)$ is the spin projection operator of the particle a , Q_{abc} is the magnitude of p_b or p_c in the rest system of a . The Blatt-Weisskopf barrier factors $B_L(Q_{abc})$, are derived by assuming a square well interaction potential as

$$B_0(Q_{abc}) = 1, \quad (4.4)$$

$$B_1(Q_{abc}) = \sqrt{\frac{2}{Q_{abc}^2 + Q_0^2}}, \quad (4.5)$$

$$B_2(Q_{abc}) = \sqrt{\frac{13}{Q_{abc}^4 + 3Q_{abc}^2 Q_0^2 + 9Q_0^4}}. \quad (4.6)$$

Here $Q_0 = 0.197321/R \text{ GeV}/c$ is a hadron “scale” parameter, where R is the radius of the centrifugal barrier in fm. In this paper, the radius R is taken to be 0.7 fm.

The propagator of intermediate resonance is parameterized by a relativistic Breit-Wigner (BW) function with an invariant mass dependent width [54]

$$\text{BW}(s) = \frac{1}{m^2 - s - i\sqrt{s}\Gamma(s)}, \quad (4.7)$$

$$\Gamma(s) = \Gamma_0(m^2) \left(\frac{m^2}{s}\right) \left(\frac{p(s)}{p(m^2)}\right)^{2l+1}, \quad (4.8)$$

where s is the invariant mass squared of the daughter particle, m and Γ_0 are the mass and width of the intermediate resonance, respectively, l is the orbital angular momentum for a daughter particle, and $p(s)$ or $p(m^2)$ is the momentum of a daughter particle in the rest frame of the resonance with mass \sqrt{s} or m . To include the resolution effect for the narrow ϕ resonance, the BW function is convolved with a Gaussian function.

The relative magnitudes and phases of the individual intermediate processes are determined by performing an unbinned maximum likelihood fit using MINUIT [55], where the magnitude and phase of the reference amplitude $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ are fixed to 1 and 0, respectively, while those of other amplitudes are free parameters of the fit.

The negative log-likelihood function for observing N events in the data sample is expressed as

$$\mathcal{NLL} = - \sum_i^N \log \frac{\omega_i \epsilon_i}{\int \epsilon \omega d\Phi_3} = - \sum_i^N \log \frac{\omega_i}{\int \epsilon \omega d\Phi_3} + \text{const}, \quad (4.9)$$

Process	Significance		
	2.125 GeV	2.396 GeV	2.900 GeV
$\phi\pi^0$	13.1σ	8.6σ	9.7σ
$\phi(1680)\pi^0$	11.1σ	12.2σ	8.3σ
$K^*(892)^0\bar{K}^0$	$>30\sigma$	$>30\sigma$	$>30\sigma$
$K_2^*(1430)^0\bar{K}^0$	29.2σ	5.7σ	5.1σ
$K(1680)^0\bar{K}^0$	9.8σ	8.4σ	7.6σ

Table 2. Statistical significances of the intermediate states for data at $\sqrt{s} = 2.125, 2.396$ and 2.900 GeV.

where ω_i is the decay-amplitude squared evaluated from the four-momenta of final particles for the i -th event, ϵ_i is the detection efficiency and Φ is the standard element of phase space. The contribution of background events to the $\mathcal{N}\mathcal{L}\mathcal{L}$ is canceled out by evaluating the signal model on K_S^0 sideband events injected into the data sample with negative weights.

Conservation of J^{PC} for intermediate states, in the process $e^+e^- \rightarrow R_1\pi^0 \rightarrow K_S^0 K_L^0 \pi^0$, allows both \mathcal{P} and \mathcal{F} wave contributions both in $e^+e^- \rightarrow R_1\pi^0$ and $R_1 \rightarrow K_S^0 K_L^0$. In the case of $e^+e^- \rightarrow K_S^0(K_L^0)R_2 \rightarrow K_S^0 K_L^0 \pi^0$, the contributions of \mathcal{P} , \mathcal{D} and \mathcal{F} waves are all allowed both in the primary and secondary processes. The PWA fit procedure starts by including the $K^*(892)^0\bar{K}^0$ and $K_2^*(1430)^0\bar{K}^0$ as the initial baseline solutions, and then adds one at a time other possible intermediate states which can decay to $K_S^0(K_L^0)\pi^0$ or $K_S^0 K_L^0$. The masses and widths of possible intermediate resonances are fixed to their PDG values [1]. Intermediate states are included in the solution if the statistical significance is greater than 5σ , where the statistical significance is evaluated from the changes in likelihood and degrees of freedom with and without the corresponding amplitude included in the PWA fit. The direct decay process without an intermediate resonance is treated as a phase space distribution without a propagator [12]. The procedure is repeated until a best solution is obtained.

The above strategy is implemented individually on the experimental data sets collected at $\sqrt{s} = 2.125, 2.396$ and 2.900 GeV, which have the largest luminosities and yields among the nineteen data sets. As the c.m. energy increases, we test the significance of the process with higher threshold at $\sqrt{s} = 2.900$ GeV, such as $e^+e^- \rightarrow K_3^*(1780)^0\bar{K}^0$, which cannot be produced at $\sqrt{s} = 2.125$ GeV. But the significances of these processes are less than 5σ and they are not retained in the final best solution. The statistical significances of the intermediate states and fit fractions for $\sqrt{s} = 2.125, 2.396$ and 2.900 GeV are listed in table 2 and table 3, respectively. For the other sixteen data samples with lower luminosities and limited statistics, the intermediate components are assumed to be the same as those of the nearby c.m. energies with higher statistics. The intermediate component candidates of $\sqrt{s} = 2.000, 2.050, 2.100, 2.150, 2.175, 2.200$, and 2.232 GeV are assumed to be the same as $\sqrt{s} = 2.125$ GeV. The intermediate component candidates of $\sqrt{s} = 2.309, 2.386, 2.644$ and 2.646 GeV are assumed to be the same as $\sqrt{s} = 2.396$ GeV. The remaining datasets are assumed to use the same intermediate components as $\sqrt{s} = 2.900$ GeV. The data for each energy point is fitted individually.

Process	Fraction (%)		
	2.125 GeV	2.396 GeV	2.900 GeV
$\phi\pi^0$	0.78 ± 0.56	0.87 ± 0.61	1.82 ± 1.11
$\phi(1680)\pi^0$	2.39 ± 1.23	5.96 ± 2.10	5.22 ± 1.50
$K^*(892)^0\bar{K}^0$	79.89 ± 1.12	86.01 ± 1.38	72.65 ± 2.11
$K_2^*(1430)^0\bar{K}^0$	7.42 ± 0.83	1.93 ± 0.57	1.85 ± 0.82
$K(1680)^0\bar{K}^0$	3.00 ± 1.11	6.73 ± 1.91	5.82 ± 1.96

Table 3. Fit fractions of the intermediate states for data at $\sqrt{s} = 2.125, 2.396$ and 2.900 GeV.

The invariant mass spectra, angular distributions and fit results for $\sqrt{s} = 2.125$ GeV are shown in figure 4.

5 Born cross sections measurement

The Born cross section for $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ is obtained at each c.m. energy using

$$\sigma(\sqrt{s}) = \frac{N_{\text{sig}}}{\mathcal{L} \cdot \epsilon \cdot (1 + \delta) \cdot \frac{1}{|1 - \Pi|^2} \cdot \mathcal{B}}, \quad (5.1)$$

where N_{sig} is the number of signal events, \mathcal{L} is the integrated luminosity, ϵ is the efficiency obtained by weighting MC simulation according to the PWA results, \mathcal{B} is the product of BFs in the full decay chain $\mathcal{B} = \mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-) \cdot \mathcal{B}(\pi^0 \rightarrow \gamma\gamma) = 68.39\%$, which is taken from the PDG [1], $\frac{1}{|1 - \Pi|^2}$ is the vacuum polarization (VP) factor [56], and $1 + \delta$ is the ISR correction factor, which is obtained by a QED calculation [57]. Both ϵ and $1 + \delta$ depend on the line shape of cross sections and are determined by an iterative procedure [11, 58]. The Born cross section for an intermediate process, $e^+e^- \rightarrow K^*(892)^0\bar{K}^0$ or $K_2^*(1430)^0\bar{K}^0$, at each energy is obtained with the same approach, where N_{sig} is replaced with the product of the total number of surviving events and the corresponding fraction relative to the total obtained according to the PWA results, and \mathcal{B} is replaced with the product of the BFs of the decays $K_S^0 \rightarrow \pi^+\pi^-$, $\pi^0 \rightarrow \gamma\gamma$ and that of the intermediate state ($K^*(892)^0 \rightarrow K^0\pi^0 = 33.23\%$, $K_2^*(1430)^0 \rightarrow K^0\pi^0 = 16.60\%$) from the PDG [1], respectively. The Born cross sections are listed in tables 4, 5 and 6, separately for the processes $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, $K^*(892)^0\bar{K}^0$ and $K_2^*(1430)^0\bar{K}^0$, respectively.

The previous BESIII measurement [12] with the charged channel $e^+e^- \rightarrow K^+K^-\pi^0$ shows that $K_2^*(1430)^+K^-$ is the dominant component, with the fraction of $K^*(892)^+K^-$ at the 2-10% level. However, in this study with the neutral channel $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, $K^*(892)^0\bar{K}^0$ is dominant, while $K_2^*(1430)^0\bar{K}^0$ is at the 5% level in the BESIII c.m. energy region. The asymmetry is also observed by BaBar [28] in the production of $K^*(892)^0\bar{K}^0$, $K^*(892)^+K^-$, $K_2^*(1430)^0\bar{K}^0$ and $K_2^*(1430)^+K^-$. To quantify the effect, we define relative ratios of the Born cross sections:

$$\begin{aligned} R(K^*(892)) &= \frac{\sigma(e^+e^- \rightarrow K^*(892)^+K^-)}{\sigma(e^+e^- \rightarrow K^*(892)^0\bar{K}^0)}, \\ R(K_2^*(1430)) &= \frac{\sigma(e^+e^- \rightarrow K_2^*(1430)^+K^-)}{\sigma(e^+e^- \rightarrow K_2^*(1430)^0\bar{K}^0)}. \end{aligned} \quad (5.2)$$

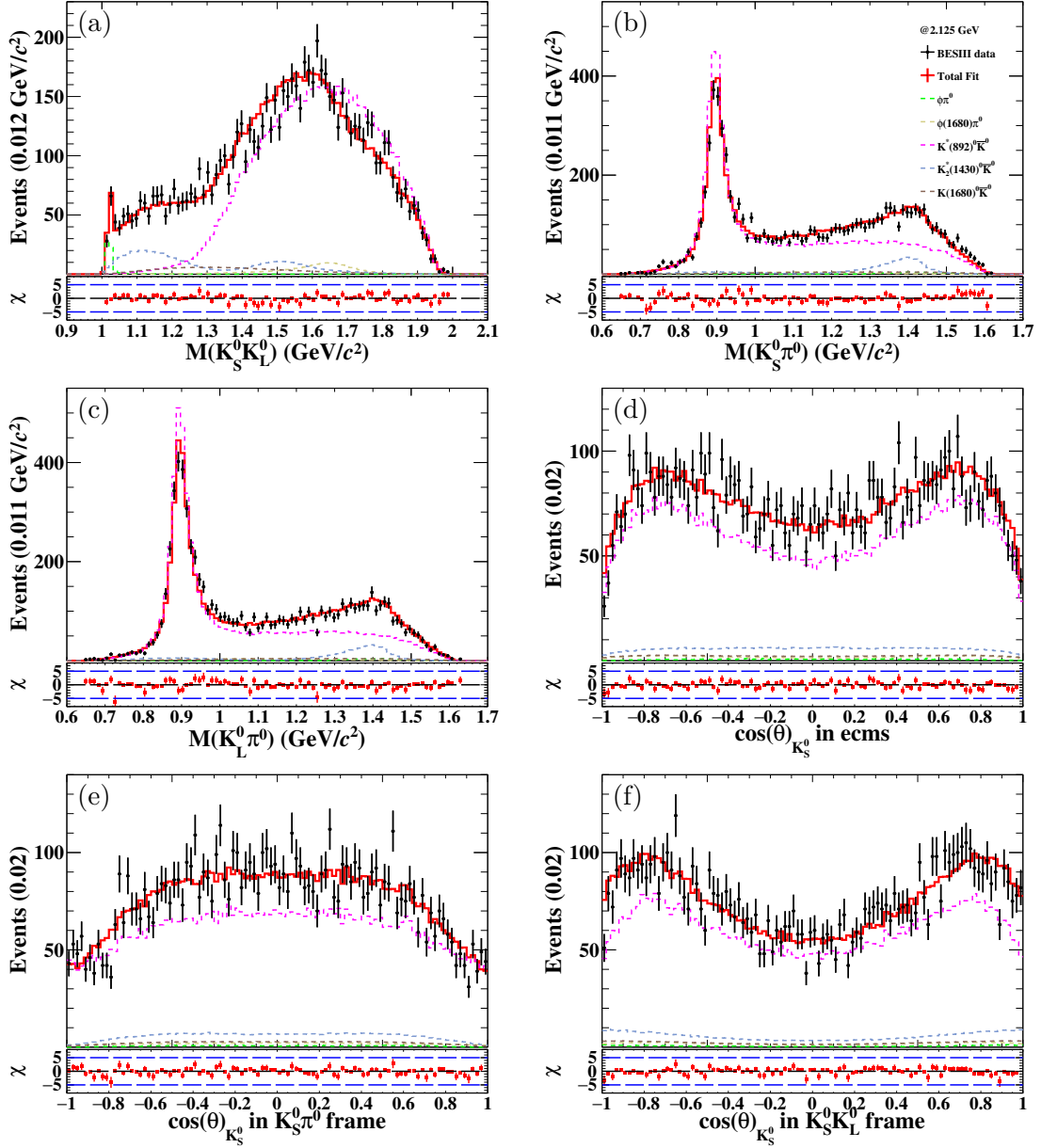


Figure 4. Superposition of data and the PWA fit projections for invariant mass distributions of (a) $K_S^0 K_L^0$, (b) $K_S^0 \pi^0$ and (c) $K_L^0 \pi^0$, and the $\cos \theta$ distributions of (d) K_S^0 in e^+e^- c.m. frame, (e) K_S^0 in $K_S^0 \pi^0$ rest frame and (f) K_S^0 in $K_S^0 K_L^0$ rest frame at $\sqrt{s} = 2.125$ GeV. The pull projection of the residuals is shown beneath each distribution correspondingly. Different styles of the curves denote different components.

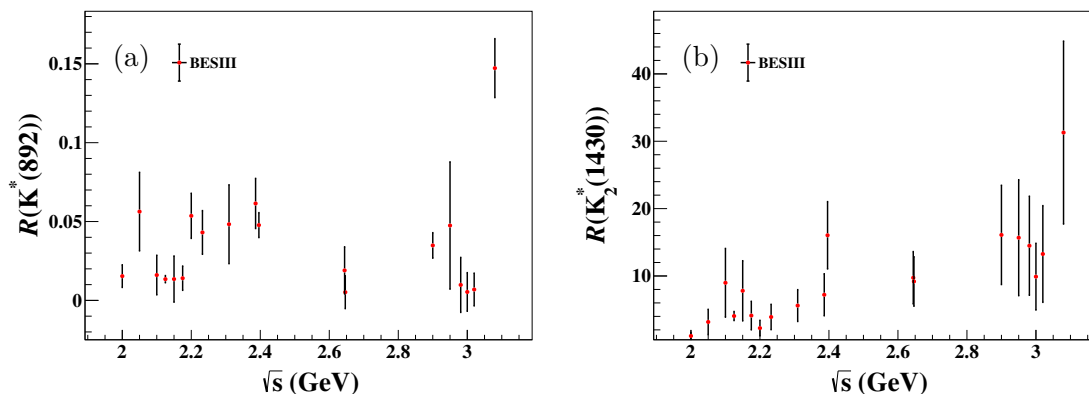


Figure 5. Relative ratio distributions for (a) $K^*(892)$ and (b) $K_2^*(1430)$.

\sqrt{s} (GeV)	N_{sig}	\mathcal{L} (pb^{-1})	ϵ	$1+\delta$	$\frac{1}{ 1-\Pi ^2}$	σ (pb)
2.0000	880.6 ± 32.3	10.1 ± 0.1	15.3%	1.22	1.037	$662.7 \pm 24.3 \pm 17.7 \pm 18.0$
2.0500	308.4 ± 19.2	3.34 ± 0.03	15.8%	1.20	1.038	$682.1 \pm 42.5 \pm 18.3 \pm 26.9$
2.1000	941.7 ± 33.8	12.2 ± 0.1	16.4%	1.18	1.039	$557.8 \pm 20.0 \pm 14.9 \pm 15.0$
2.1250	8175.0 ± 98.9	108 ± 1	16.6%	1.17	1.039	$545.4 \pm 6.6 \pm 14.6 \pm 7.2$
2.1500	228.1 ± 16.8	2.84 ± 0.02	17.1%	1.13	1.040	$582.2 \pm 42.9 \pm 15.6 \pm 23.5$
2.1750	678.7 ± 28.4	10.6 ± 0.1	16.5%	1.23	1.040	$444.5 \pm 18.6 \pm 11.9 \pm 16.0$
2.2000	772.8 ± 30.5	13.7 ± 0.1	16.2%	1.25	1.040	$391.2 \pm 15.4 \pm 10.5 \pm 12.2$
2.2324	594.1 ± 26.7	11.9 ± 0.1	16.0%	1.28	1.041	$342.9 \pm 15.4 \pm 9.2 \pm 11.1$
2.3094	846.1 ± 32.8	21.1 ± 0.1	15.5%	1.31	1.041	$277.3 \pm 10.8 \pm 7.4 \pm 10.6$
2.3864	741.3 ± 30.1	22.5 ± 0.2	15.5%	1.34	1.041	$224.2 \pm 9.1 \pm 6.0 \pm 7.9$
2.3960	2146.1 ± 51.2	66.9 ± 0.5	15.2%	1.34	1.041	$220.4 \pm 5.3 \pm 5.9 \pm 4.6$
2.6444	595.2 ± 27.7	33.7 ± 0.2	15.0%	1.45	1.039	$114.4 \pm 5.3 \pm 3.1 \pm 3.2$
2.6464	615.4 ± 27.8	34.0 ± 0.3	15.0%	1.45	1.039	$117.2 \pm 5.3 \pm 3.1 \pm 3.2$
2.9000	1100.7 ± 37.1	105 ± 1	14.0%	1.65	1.033	$64.8 \pm 2.2 \pm 1.7 \pm 1.4$
2.9500	124.0 ± 13.0	15.9 ± 0.1	13.3%	1.68	1.029	$49.6 \pm 5.2 \pm 1.3 \pm 2.3$
2.9810	146.0 ± 13.8	16.1 ± 0.1	13.9%	1.66	1.025	$56.1 \pm 5.3 \pm 1.5 \pm 2.1$
3.0000	144.5 ± 13.9	15.9 ± 0.1	13.7%	1.67	1.021	$56.6 \pm 5.4 \pm 1.5 \pm 2.7$
3.0200	143.8 ± 13.6	17.3 ± 0.1	13.7%	1.71	1.014	$51.1 \pm 4.8 \pm 1.4 \pm 1.9$
3.0800	963.8 ± 35.3	126 ± 1	12.8%	1.83	0.915	$52.3 \pm 1.9 \pm 1.4 \pm 1.2$

Table 4. The measured Born cross sections for $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, where the first uncertainties are statistical, the second ones are systematics from table 7 and the third ones are model uncertainties.

The corresponding results for the relative ratio are summarized in figure 5.

\sqrt{s} (GeV)	N_{sig}	\mathcal{L} (pb $^{-1}$)	ϵ	$1+\delta$	$\frac{1}{ 1-\Pi ^2}$	σ (pb)
2.0000	845.4 \pm 45.3	10.1 \pm 0.1	17.0%	1.07	1.037	1942.5 \pm 104.0 \pm 52.0 \pm 63.3
2.0500	225.4 \pm 22.8	3.34 \pm 0.03	17.2%	1.08	1.038	1533.4 \pm 155.4 \pm 41.0 \pm 71.1
2.1000	772.9 \pm 52.7	12.2 \pm 0.1	17.6%	1.07	1.039	1420.4 \pm 96.9 \pm 38.0 \pm 46.1
2.1250	6530.7 \pm 120.8	108 \pm 1	17.7%	1.05	1.039	1376.2 \pm 25.5 \pm 36.8 \pm 19.3
2.1500	200.6 \pm 24.4	2.84 \pm 0.02	17.1%	1.10	1.040	1585.8 \pm 193.1 \pm 42.5 \pm 63.0
2.1750	516.1 \pm 31.7	10.6 \pm 0.1	17.3%	1.13	1.040	1055.1 \pm 64.8 \pm 28.2 \pm 33.1
2.2000	575.5 \pm 33.6	13.7 \pm 0.1	16.9%	1.14	1.040	918.5 \pm 53.6 \pm 24.6 \pm 31.0
2.2324	472.0 \pm 26.9	11.9 \pm 0.1	16.9%	1.16	1.041	851.5 \pm 48.5 \pm 22.8 \pm 27.0
2.3094	637.6 \pm 32.5	21.1 \pm 0.1	16.4%	1.20	1.041	648.1 \pm 33.0 \pm 17.3 \pm 22.4
2.3864	595.6 \pm 31.5	22.5 \pm 0.2	16.2%	1.23	1.041	559.5 \pm 29.6 \pm 15.0 \pm 17.3
2.3960	1845.8 \pm 53.0	66.9 \pm 0.5	16.4%	1.23	1.041	578.4 \pm 16.6 \pm 15.5 \pm 11.4
2.6444	438.0 \pm 25.5	33.7 \pm 0.2	15.5%	1.35	1.039	262.0 \pm 15.3 \pm 7.0 \pm 8.1
2.6464	452.9 \pm 25.9	34.0 \pm 0.3	15.5%	1.35	1.039	268.5 \pm 15.3 \pm 7.2 \pm 8.2
2.9000	799.7 \pm 35.6	105 \pm 1	14.9%	1.50	1.033	145.8 \pm 6.5 \pm 3.9 \pm 3.9
2.9500	94.8 \pm 11.0	15.9 \pm 0.1	14.3%	1.54	1.029	115.5 \pm 13.4 \pm 3.1 \pm 6.9
2.9810	111.6 \pm 11.7	16.1 \pm 0.1	14.4%	1.56	1.025	132.0 \pm 13.8 \pm 3.5 \pm 7.3
3.0000	108.0 \pm 11.5	15.9 \pm 0.1	14.2%	1.58	1.021	130.5 \pm 13.9 \pm 3.5 \pm 6.9
3.0200	104.3 \pm 10.8	17.3 \pm 0.1	14.2%	1.59	1.014	115.7 \pm 12.0 \pm 3.1 \pm 6.2
3.0800	695.9 \pm 33.4	126 \pm 1	13.3%	1.73	0.915	115.1 \pm 5.5 \pm 3.1 \pm 2.4

Table 5. The measured Born cross sections for $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$, where the first uncertainties are statistical, the second ones are systematics from table 7 and the third ones are model uncertainties.

6 Systematic uncertainties

Two categories of systematic uncertainties are considered in the measurement of the Born cross sections. The first category includes systematic sources not associated with the PWA fit that are evaluated as follows:

1. The uncertainty associated with the integrated luminosity is 1% and estimated by using large angle Bhabha events [36].
2. The uncertainty concerning K_S^0 reconstruction is studied with control samples of $J/\psi \rightarrow K_S^0 K^\pm \pi^\mp$ and $J/\psi \rightarrow \phi K_S^0 K^\pm \pi^\mp$. The result shows that the difference in efficiency between data and MC simulation is 1% per K_S^0 [59].
3. The uncertainty of the requirement on the number of charged tracks (N_{charge}) is estimated with a control sample of $J/\psi \rightarrow K_S^0 K_L^0 \pi^0$. The difference in efficiency between data and MC simulation with and without this requirement is taken as the uncertainty.
4. The uncertainty concerning photon detection efficiency is studied with a control sample of $e^+e^- \rightarrow K^+ K^- \pi^+ \pi^- \pi^0$ [60]. The result shows that the difference in detection efficiency between data and MC simulation is 1% per photon.

\sqrt{s} (GeV)	N_{sig}	\mathcal{L} (pb $^{-1}$)	ϵ	$1+\delta$	$\frac{1}{ 1-\Pi ^2}$	σ (pb)
2.0000	80.1 ± 28.2	10.1 ± 0.1	20.0%	1.06	1.037	315.2 ± 111.2 ± 8.4 ± 11.2
2.0500	11.1 ± 5.0	3.34 ± 0.03	20.4%	1.07	1.038	127.5 ± 58.2 ± 3.4 ± 6.0
2.1000	27.3 ± 13.7	12.2 ± 0.1	20.7%	1.07	1.039	84.6 ± 42.4 ± 2.3 ± 3.6
2.1250	606.2 ± 68.3	108 ± 1	20.5%	1.08	1.039	214.2 ± 24.1 ± 5.7 ± 5.2
2.1500	9.7 ± 5.1	2.84 ± 0.02	23.4%	0.95	1.040	129.6 ± 68.1 ± 3.5 ± 6.1
2.1750	59.1 ± 28.6	10.6 ± 0.1	26.1%	0.88	1.040	204.1 ± 98.7 ± 5.5 ± 7.5
2.2000	113.1 ± 54.7	13.7 ± 0.1	25.8%	0.96	1.040	304.0 ± 147.0 ± 8.1 ± 12.2
2.2324	55.8 ± 25.2	11.9 ± 0.1	23.8%	1.03	1.041	171.9 ± 77.8 ± 4.6 ± 7.5
2.3094	54.5 ± 21.6	21.1 ± 0.1	22.3%	1.04	1.041	94.3 ± 37.4 ± 2.5 ± 4.3
2.3864	28.0 ± 11.5	22.5 ± 0.2	22.3%	1.07	1.041	45.3 ± 18.7 ± 1.2 ± 1.8
2.3960	41.5 ± 12.3	66.9 ± 0.5	21.7%	1.07	1.041	22.3 ± 6.6 ± 0.6 ± 0.7
2.6444	21.5 ± 8.2	33.7 ± 0.2	22.0%	1.07	1.039	22.9 ± 8.8 ± 0.6 ± 0.9
2.6464	22.3 ± 8.4	34.0 ± 0.3	22.0%	1.07	1.039	23.5 ± 8.9 ± 0.6 ± 0.9
2.9000	20.4 ± 9.1	105 ± 1	22.7%	1.08	1.033	6.7 ± 3.0 ± 0.2 ± 0.2
2.9500	2.2 ± 1.1	15.9 ± 0.1	22.5%	1.08	1.029	4.8 ± 2.4 ± 0.1 ± 0.3
2.9810	2.5 ± 1.1	16.1 ± 0.1	22.9%	1.08	1.025	5.3 ± 2.4 ± 0.1 ± 0.3
3.0000	4.7 ± 2.2	15.9 ± 0.1	22.8%	1.08	1.021	10.3 ± 4.7 ± 0.3 ± 0.6
3.0200	2.2 ± 1.1	17.3 ± 0.1	23.0%	1.08	1.014	4.5 ± 2.1 ± 0.1 ± 0.2
3.0800	8.7 ± 3.7	126 ± 1	23.6%	1.08	0.915	2.6 ± 1.1 ± 0.1 ± 0.1

Table 6. The measured Born cross sections for $e^+e^- \rightarrow K_2^*(1430)^0 \bar{K}^0$, where the first uncertainties are statistical, the second ones are systematics from table 7 and the third ones are model uncertainties.

5. The uncertainty related to the kinematic fit is studied with a control sample of $J/\psi \rightarrow K_S^0 K_L^0 \pi^0$. The difference in efficiency between data and MC simulation with and without the kinematic fit is taken as the uncertainty.
6. The uncertainty of the VP and ISR correction factors (Rad) is obtained with the accuracy of the radiation function, which is about 0.5% [56], and has an additional contribution from the cross section line shape, which is estimated by varying the model parameters of the fit to the cross section. All parameters are randomly varied within their uncertainties, and the resulting parametrization of the line shape is used to recalculate $(1 + \delta)\epsilon$ and the corresponding cross section. This procedure is repeated one thousand times, and the standard deviation of the resulting cross sections is taken as the systematic uncertainty. The systematic uncertainty associated with the VP and ISR correction factor is evaluated as the quadratic sum of contributions from the QED theory and line shape parametrization [10].

7. The uncertainty associated with the BFs from the PDG [1] is 0.08%, including both $\mathcal{B}(K_S^0 \rightarrow \pi^+\pi^-) = (69.20 \pm 0.05)\%$ and $\mathcal{B}(\pi^0 \rightarrow \gamma\gamma) = (98.823 \pm 0.034)\%$.
8. The uncertainty caused by the $M(\pi^+\pi^-)$ fit (Fit) includes the descriptions of signal shape and background shape. The nominal MC-simulated shape convolved with a Gaussian function is replaced by a MC-simulated shape convolved with a Crystal Ball function, and the nominal background shape is replaced by a second-order polynomial function, and the differences with the nominal results are taken as the uncertainties. The uncertainties from above sources are added in quadrature and taken as the total uncertainty from the $M(\pi^+\pi^-)$ fit.

The second category of uncertainties includes those associated with the PWA fit that are evaluated as follows:

1. The uncertainty from the fit parameters (FPar) is estimated by the standard deviation of re-calculated efficiencies derived from one thousand groups of randomly generated fit parameters using a correlated multi-variable Gaussian function.
2. The uncertainty related to the resonance parameters (Par) is estimated by performing alternative fits shifting the world-average parameter value by its error from the PDG [1].
3. The uncertainty concerning the extra additional resonances (Extra) is estimated by performing alternative fits with all components whose significances are greater than 3σ . In the alternative fit $K^*(1410)^0 \rightarrow K^0\pi^0$ is added for the data sample at $\sqrt{s} = 2.125$ GeV, $K^*(1410)^0 \rightarrow K^0\pi^0$ and $\rho(1450) \rightarrow K^0\bar{K}^0$ are added at $\sqrt{s} = 2.396$ GeV, $\rho(1450)/\rho(1700) \rightarrow K^0\bar{K}^0$ and $K^*(1410)^0/K_3^*(1780)^0 \rightarrow K^0\pi^0$ are added at $\sqrt{s} = 2.900$ GeV.
4. The uncertainty of the background estimation in the PWA fit (Bkg) is estimated by using only the lower or higher sideband.
5. The uncertainty from the Blatt-Weisskopf barrier factor (BWf) is estimated by varying the radius of the centrifugal barrier from 0.7 to 1.0 fm.

Assuming all the sources of systematic uncertainties as independent, the total systematic uncertainty is obtained by adding them in quadrature. The 100% correlated uncertainties for the Born cross sections of $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, $K^*(892)^0 \bar{K}^0$ and $K_2^*(1430)^0 \bar{K}^0$ are listed in table 7. The other uncorrelated and total systematic uncertainties are listed in tables 8–10.

7 Fit to the lineshape

The Born cross sections for the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ are shown in figure 6(a). The results are consistent with the previous results from BaBar. The Born cross sections for the intermediate process $e^+e^- \rightarrow K_2^*(1430)^0 \bar{K}^0$ and $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ are shown in figures 6(b) and 7, respectively.

A χ^2 fit, incorporating the correlated and uncorrelated uncertainties among different energy points, is performed to determine the resonance parameters for the Born cross sections

Source	Uncertainty(%)
Luminosity	1.00
K_S^0 reconstruction	1.00
Requirement on N_{charge}	0.70
Photon reconstruction	2.00
Kinematic fit	0.70
BF	0.08
Total	2.63

Table 7. The 100% correlated systematic uncertainties for the Born cross section of $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$.

\sqrt{s} (GeV)	Rad	Fit	FPar	Par	Extra	Bkg	BWf	Total
2.0000	0.50	0.91	2.40	0.70	0.41	0.26	0.21	2.76
2.0500	0.50	2.13	2.50	2.11	0.40	0.30	0.21	3.97
2.1000	0.50	0.36	2.40	1.02	0.40	0.30	0.17	2.73
2.1250	0.50	0.94	0.80	0.22	0.38	0.07	0.13	1.41
2.1500	0.50	2.83	2.60	1.10	0.43	0.30	0.31	4.07
2.1750	0.50	1.14	3.00	1.53	0.40	0.24	0.40	3.64
2.2000	0.50	1.39	2.50	1.11	0.41	0.30	0.22	3.16
2.2324	0.50	2.11	2.20	1.02	0.32	0.30	0.17	3.29
2.3094	0.50	2.71	2.40	1.10	0.31	0.28	0.22	3.84
2.3864	0.50	1.44	3.00	1.10	0.30	0.30	0.21	3.57
2.3960	0.50	1.36	1.40	0.60	0.30	0.15	0.21	2.14
2.6444	0.50	2.12	1.41	1.02	0.30	0.18	0.40	2.84
2.6464	0.50	2.05	1.40	1.02	0.30	0.18	0.40	2.78
2.9000	0.50	1.50	1.30	0.68	0.29	0.20	0.13	2.19
2.9500	0.51	3.20	2.57	2.10	0.33	0.30	0.31	4.67
2.9810	0.50	2.50	2.20	1.69	0.31	0.30	0.30	3.80
3.0000	0.50	3.75	2.20	2.06	0.30	0.28	0.25	4.86
3.0200	0.50	2.58	1.70	1.91	0.30	0.30	0.30	3.70
3.0800	0.50	0.98	1.70	1.02	0.31	0.20	0.20	2.30

Table 8. Systematic uncertainties (%) for the Born cross section of $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ at each c.m. energy associated with the ISR and VP correction factors (Rad), the $M(\pi^+\pi^-)$ fit (Fit), the fit parameters in PWA (FPar), the resonance parameters (Par), the extra additional resonances (Extra), the background estimation (Bkg) and the Blatt-Weisskopf barrier factor (BWf).

\sqrt{s} (GeV)	Rad	Fit	Par	Extra	Bkg	BWf	Total
2.0000	0.50	0.91	1.90	0.71	1.43	1.91	3.30
2.0500	0.50	2.13	1.22	0.70	2.32	3.10	4.67
2.1000	0.50	0.36	1.71	0.70	1.72	2.01	3.29
2.1250	0.50	0.94	0.21	0.68	0.20	0.73	1.49
2.1500	0.50	2.83	1.23	0.73	1.30	2.01	4.00
2.1750	0.50	1.14	1.01	0.70	1.12	2.40	3.17
2.2000	0.50	1.39	1.32	0.71	1.52	2.22	3.42
2.2324	0.50	2.11	1.10	0.52	1.15	1.67	3.21
2.3094	0.50	2.71	1.05	0.51	1.09	1.42	3.49
2.3864	0.50	1.44	1.04	0.51	1.14	2.20	3.13
2.3960	0.50	1.36	0.53	0.50	0.50	1.13	2.03
2.6444	0.50	2.12	0.72	0.51	1.20	1.70	3.14
2.6464	0.50	2.05	0.72	0.51	1.17	1.70	3.08
2.9000	0.50	1.50	0.38	0.69	1.57	1.32	2.71
2.9500	0.51	3.20	3.01	0.73	2.31	3.18	5.96
2.9810	0.50	2.50	3.01	0.71	2.11	3.17	5.53
3.0000	0.50	3.75	1.53	0.70	2.01	2.68	5.33
3.0200	0.50	2.58	1.22	0.70	1.42	4.20	5.34
3.0800	0.50	0.98	0.50	0.71	0.97	1.27	2.13

Table 9. Systematic uncertainties (%) for the Born cross section of $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ at each c.m. energy associated with the ISR and VP correction factors (Rad), the $M(\pi^+\pi^-)$ fit (Fit), the fit parameters in PWA (FPar), the resonance parameters (Par), the extra additional resonances (Extra), the background estimation (Bkg) and the Blatt-Weisskopf barrier factor (BWf).

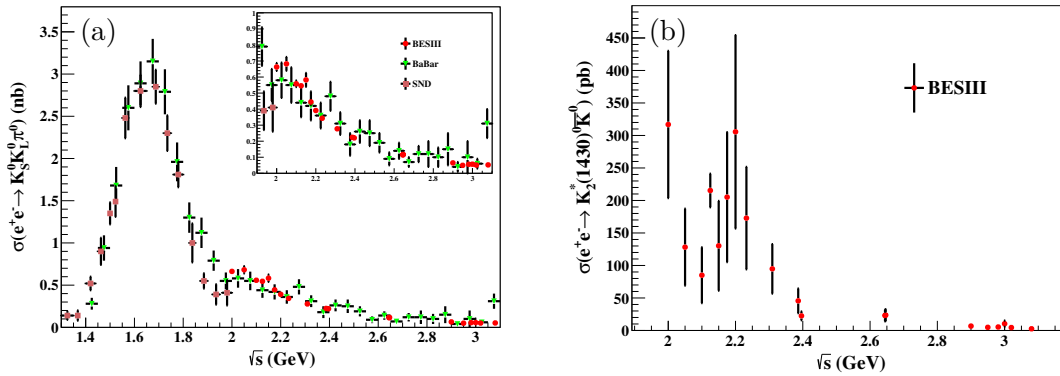


Figure 6. The Born cross sections for (a) the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ and (b) the process $e^+e^- \rightarrow K_2^*(1430)^0 \bar{K}^0$. The red dots are the measured results from BESIII, where errors include both statistical and systematic uncertainties. The green triangles and brown squares are the results from BaBar and SND, respectively.

\sqrt{s} (GeV)	Rad	Fit	Par	Extra	Bkg	BWf	Total
2.0000	0.50	0.91	2.02	1.00	1.50	2.07	3.56
2.0500	0.50	2.13	2.10	1.00	2.70	2.21	4.73
2.1000	0.50	0.36	2.27	1.00	2.58	2.21	4.25
2.1250	0.50	0.94	1.01	1.00	1.05	1.29	2.43
2.1500	0.50	2.83	1.82	1.00	2.22	2.08	4.67
2.1750	0.50	1.14	2.10	1.00	1.50	2.10	3.69
2.2000	0.50	1.39	2.10	1.00	1.92	2.21	4.02
2.2324	0.50	2.11	2.12	1.31	2.00	2.01	4.35
2.3094	0.50	2.71	2.10	1.30	1.50	2.10	4.51
2.3864	0.50	1.44	2.10	1.30	1.62	2.10	3.93
2.3960	0.50	1.36	1.49	1.31	1.31	1.70	3.26
2.6444	0.50	2.12	1.70	1.31	1.67	2.00	4.02
2.6464	0.50	2.05	1.70	1.31	1.70	2.00	3.99
2.9000	0.50	1.50	1.38	1.50	1.20	1.92	3.43
2.9500	0.51	3.20	2.50	1.53	2.00	2.20	5.28
2.9810	0.50	2.50	2.72	1.52	2.03	2.11	4.98
3.0000	0.50	3.75	2.51	1.52	2.11	2.20	5.68
3.0200	0.50	2.58	2.51	1.52	2.12	2.00	4.90
3.0800	0.50	0.98	1.70	1.51	1.20	1.92	3.39

Table 10. Systematic uncertainties (%) for the Born cross section of $e^+e^- \rightarrow K_2^*(1430)^0 \bar{K}^0$ at each c.m. energy associated with the ISR and VP correction factors (Rad), the $M(\pi^+\pi^-)$ fit (Fit), the resonance parameters (Par), the extra additional resonances (Extra), the background estimation (Bkg) and the Blatt-Weisskopf barrier factor (BWf).

of $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$. The fit probability density function is a coherent sum of a continuum component and a resonant component. The cross section is modeled as:

$$\sigma = \left| \frac{\sqrt{12\pi\Gamma_Y\Gamma_Y^{e^+e^-}\mathcal{B}}}{M_Y^2 - s - iM_Y\Gamma(\sqrt{s})} \sqrt{\frac{P(\sqrt{s})}{P(M_Y)}} e^{i\phi_Y} + c_1 \frac{\sqrt{P(\sqrt{s})}}{s^{c_2}} \right|^2, \quad (7.1)$$

where M_Y and Γ_Y are the mass and width of the resonance; ϕ_Y is the relative phase between the continuum component and the resonance; $\Gamma_Y^{e^+e^-}$ is its partial width to e^+e^- ; \mathcal{B} is the BF of $Y \rightarrow K^*(892)^0 \bar{K}^0$; and c_1 and c_2 are additional parameters of the fit. $\Gamma(\sqrt{s})$ is defined as $\Gamma_Y \left(\frac{P(\sqrt{s})}{P(M_Y)} \right)$, where $P(\sqrt{s}) = \int \sum_m |A_{K^*(892)^0 \bar{K}^0}(m)|^2 d\Phi_3$ is the phase-space factor for the relative orbital angular momentum $L = 1$ of the process $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0 \rightarrow K_S^0 K_L^0 \pi^0$ and Φ_3 is three-body phase space [1]. The amplitude A is the partial wave amplitude in the covariant Rarita-Schwinger tensor formalism [50] and is described as:

$$A_{K^*(892)^0 \bar{K}^0}(m) = -Y^\mu(m) \epsilon_{\mu\nu\lambda\sigma} p_{(K_S^0 K_L^0 \pi^0)}^\sigma \tilde{T}_{K^*(892)^0 \bar{K}^0}^{(1)\nu} \cdot f_{K^0 \pi^0}^{K^*(892)^0} \cdot \tilde{T}_{K^0 \pi^0}^{(1)\lambda}, \quad (7.2)$$

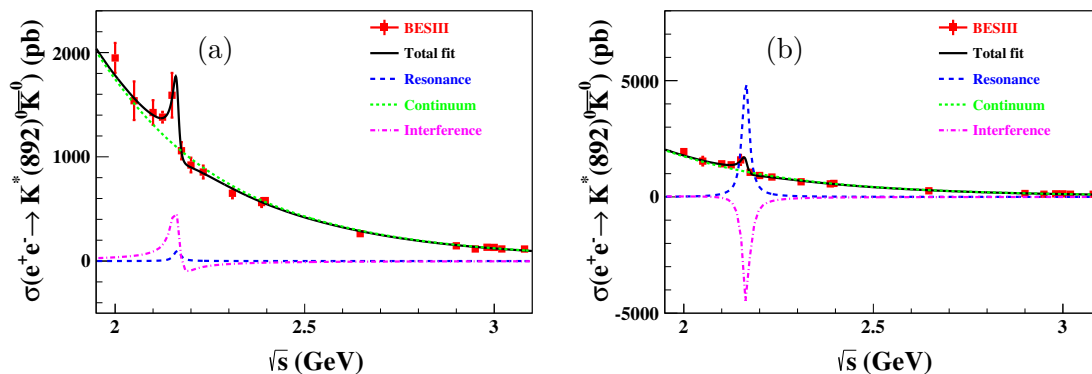


Figure 7. The Born cross section and fit curves for $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$, (a) and (b), corresponding to the two solutions in table 11. Rectangles with error bars are BESIII data, where errors include both statistical and systematic uncertainties. The solid black curves represent the total fit result, the dashed blue curves for the resonance and the dashed green curves for the continuum component, and the dash-dotted pink curves for the interference between the resonance and continuum components.

where \tilde{T} is the covariant tensor, f is the Breit-Wigner propagator, $\epsilon_{\mu\nu\lambda\sigma}$ is the Levi-Civita symbol, and the other operators can be found in ref. [50].

In total, there are six free parameters in the fit: $M_Y, \Gamma_Y, \phi_Y, c_1, c_2$ and the product of $\Gamma_Y^{e^+e^-} \mathcal{B}$. The fit results are shown in figure 7, and the resonance parameters are listed in table 11. The fit has $\chi^2/\text{ndf} = 18.95/13$ ($p = 0.125$) with two solutions for the resonance with identical mass and width, but different relative phase ϕ_Y and $\Gamma_Y^{e^+e^-} \mathcal{B}$. The mass and width of the resonance are $M_Y = (2164.1 \pm 9.6) \text{ MeV}/c^2$ and $\Gamma_Y = (32.4 \pm 21.1) \text{ MeV}$, respectively, including all sources of uncertainties from cross section measurement. The significance of the resonance is determined to be 3.2σ by comparing the change of χ^2 ($\Delta\chi^2 = 18.27$) and the change of ndf ($\Delta\text{ndf} = 4$) between the nominal fit and the fit without the resonance. As both solutions are mathematically equivalent, we do not prefer one over the other, but list them in order of increasing interference fraction. Figure 7(b) shows a large interference between resonance and continuum components. The uncertainties (statistical and systematic) of the measured Born cross sections have been included when fitting the line shape, determining the resonance parameters and estimating the significance of the resonance.

Besides the uncertainties of individual cross-section measurements, the fit to the lineshape is also affected by the uncertainty of the BEPCII c.m. energy and the description of the continuum. The uncertainty of the c.m. energy calibration is estimated as 0.1% and is ignored in the determination of resonance parameters [36]. To evaluate the systematic uncertainty associated with the lineshape model, the continuum term $c_1 \frac{\sqrt{P(\sqrt{s})}}{s^{c_2}}$ is replaced with an exponential function of the form $c_0 \cdot e^{-p_0(\sqrt{s}-M_{th})}$, where c_0 and p_0 are free parameters and $M_{th} = m_{K^*(892)^0} + m_{\bar{K}^0}$ is the mass threshold for $K^*(892)^0 \bar{K}^0$ production [1, 12]. The difference of the parameters from the nominal results are taken as the systematic uncertainties.

Parameter	Solution 1	Solution 2
$M_Y(\text{MeV}/c^2)$	$2164.7 \pm 9.1 \pm 3.1$	
$\Gamma_Y(\text{MeV})$	$32.4 \pm 21.0 \pm 1.8$	
$\Gamma_Y^{e^+e^-} \mathcal{B}(\text{eV})$	$1.0 \pm 0.2 \pm 0.1$	$73.6 \pm 4.4 \pm 2.0$
$\phi_Y(\text{rad})$	$2.5 \pm 0.5 \pm 0.1$	$-1.7 \pm 0.1 \pm 0.1$
Significance	3.2σ	

Table 11. Result of the fit to the $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ Born cross sections, where the first uncertainties originate from the cross section measurement and the second from the line shape fit methodology, respectively.

8 Summary

In summary, a partial wave analysis of the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ is performed for nineteen data samples collected in the BESIII experiment with center-of-mass energies ranging from 2.000 to 3.080 GeV corresponding to a total integrated luminosity of 647 pb⁻¹. The Born cross sections of the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$, as well as those for the intermediate processes $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ and $K_2^*(1430)^0 \bar{K}^0$ are measured by performing partial wave analysis on each data sample individually, where the charge conjugated processes are also included. The measured Born cross sections of the process $e^+e^- \rightarrow K_S^0 K_L^0 \pi^0$ are consistent with earlier results by BaBar [34], while the precision is significantly improved. The Born cross section lineshape of the process $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ hints at a resonant structure around 2.2 GeV with a significance of 3.2 σ . A Breit-Wigner fit yields its mass $M_Y = (2164.7 \pm 9.1 \pm 3.1)$ MeV/ c^2 and width $\Gamma_Y = (32.4 \pm 21.0 \pm 1.8)$ MeV. The resonance parameters, especially the very narrow width, are very close to the BESIII results measured through the $\phi\eta$ channel [7] of the $\phi(2170)$ meson [1].

The ratio of Born cross section measurements of the process $e^+e^- \rightarrow K^*(892)^+ K^-$ to the process $e^+e^- \rightarrow K^*(892)^0 \bar{K}^0$ is less than 0.2 and that for $K_2^*(1430)$ is in the region of 0-40, where the statistical and systematic uncertainties are included. If we apply the isospin decomposition for the decay from isospin vector (ρ^*) or isospin scalar (ω^*, ϕ^*) state to the final state $K^* \bar{K}$, the ratio of the yields in the neutral and charged $K^* \bar{K}$ should be 1. On the other hand, the electromagnetic interaction also contributes to the production of $e^+e^- \rightarrow K^* \bar{K}$, and it does not require isospin conservation. Future experimental and theoretical studies are needed to understand the observed phenomenon.

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- ^g Also at State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing 100871, People's Republic of China
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